

FITJEE

Solutions to JEE (Main)-2020

JEE–Main–2020 –Sept–5–First–Shift
PHYSICS, CHEMISTRY & MATHEMATICS

PART –A (PHYSICS)

1. **D**

Sol. As it just floats $B = mg$

$$\left(\frac{4\pi R^3}{3}\right)(\rho_l)(g) = \left(\frac{4\pi R^3}{3} - \frac{4\pi r^3}{3}\right)(\rho_s)(g)$$

$$R^3 = (R^3 - r^3)\left(\frac{27}{8}\right)$$

On solving we get,

$$r = \frac{8}{9}R \text{ (approx)}$$

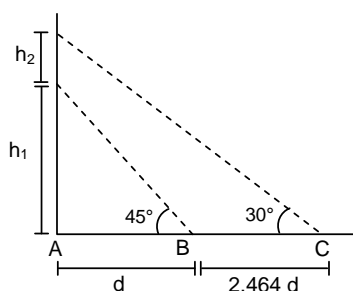
2. **D**

Sol. $\frac{h_1}{d} = 1$

$$\frac{h_1 + h_2}{3.464d} = \frac{1}{\sqrt{3}}$$

$$d + h_2 = \frac{3.464d}{\sqrt{3}}$$

$$h_2 = 2d - d = d$$



3. **D**

4. **No option.**

5. **A**

Sol. As $\text{Torque}_{\text{net}} = 0$

Hence, $L = \text{constant}$

$$l\omega = (3l + l)\omega'$$

$$\omega' = \frac{\omega}{4}$$

$$\text{Loss in K.E.} = \frac{1}{2}l\omega^2 - \frac{1}{2}(l + 3l)\frac{\omega^2}{16}$$

$$= \frac{1}{2} l \omega^2 \left(1 - \frac{1}{4}\right)$$

$$\text{Fractional loss} = \frac{\frac{1}{2} l \omega^2 \frac{3}{4}}{\frac{1}{2} l \omega^2} = \frac{3}{4}$$

6. **B**

Sol. $f = \frac{V(n)}{4 \left(1 - \frac{17}{100}\right)}$ (as closed from end)

$$f = \frac{(n-2)(v)}{4 \left(1 - \frac{24.5}{100}\right)}$$

$$\frac{nV(100)}{4(83)} = \frac{(n-2)(v)(100)}{(4)(75.5)}$$

$$75.5 n = 83 (n - 2)$$

$$75.5 n = 83 (M - 2)$$

$$7.5 n = 166$$

$$n = 22 \text{ (approx)}$$

$$f = \frac{(330)(22)(100)}{4(83)} = 2200 \text{ Hz}$$

7. **D**

Sol. $\frac{E_0}{B_0} = C$

$$B_0 = \frac{E_0}{C}$$

Force, $F_{\max} = QVB$

8. **D**

Sol. Photodiode operate in reverse bias. The photocurrent increases initially and saturates finally.

9. **C**

Sol. $\frac{1}{4} m(210)^2 = m(0.03) \times (4.2) \times 1000 \times \Delta T$; $Q = mS\Delta t$

$$\Delta T = \frac{(210)(210)}{(4)(4.2)(0.03)(1000)} = 87.5^\circ\text{C}$$

10. **C**

Sol. $g' = g \left(\frac{R}{R+h}\right)^2$ above

$$g' = g \left(\frac{2}{3} \right)^2 \quad h = \frac{R}{2}$$

$$g' = g \left(1 - \frac{d}{R} \right) \quad \text{above}$$

$$1 - \frac{d}{R} = \frac{4}{9} \quad \frac{d}{R} = \frac{5}{9}$$

11. **B**

Sol. V is always less than u .

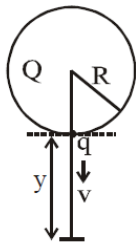
$$\frac{1}{v} - \frac{1}{u} = \frac{1}{F}$$

$$\frac{1}{v} = \frac{1}{u} + \frac{1}{F}$$

$$V = \frac{uF}{u+F} = \frac{u}{\left(\frac{u}{F} + 1 \right)}$$

12. **B**

Sol.

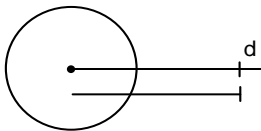


$$dw_{ef} = Eqdx$$

$$\int du_{et} = \int \frac{kQ}{x^2} dxq$$

$$= kQq \left(-\frac{1}{x} \right)_R^{R+y}$$

$$W_{ef} = \frac{kQq(y)}{(R)(R+y)}$$



$$W_{all} = \Delta k$$

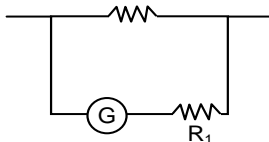
$$W_{mg} + W_{ef} = \frac{1}{2} mv^2$$

$$V^2 = \frac{2}{m} \left(\frac{kQqy}{(R)(R+y)} + mgy \right)$$

$$V^2 = 2y \left(\frac{kQq}{m(R)(R+y)} + g \right) ; k = \frac{1}{4\pi\epsilon_0}$$

13. **A**

Sol.



$$V = I_G (G + R_1)$$

$$1 = I_G (G + R_1) \quad \dots(1)$$

$$2 = I_G (G + R_1 + R_2)$$

$$2 = 1 + I_G R_2$$

$$I_G R_2 = 1$$

$$R_2 = G + R_1$$

14. **D**

Sol. Use the equation to find 'N':

$$P = \frac{2}{3} \left(\frac{N}{V} \right) \left(\frac{1}{2} m u^2 \right)$$

15. **D**

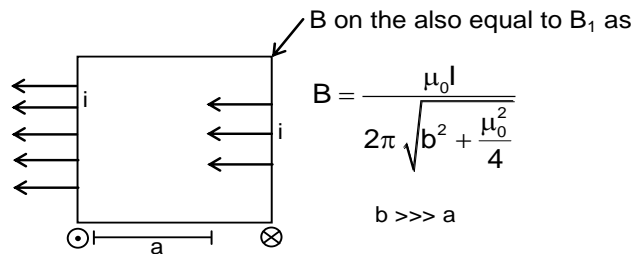
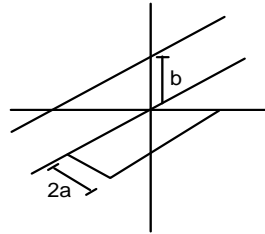
Sol.
$$\vec{B}_1 = \frac{\mu_0 I}{2\pi(\ell)}$$

$$|\vec{\tau}| = |\vec{r} \times \vec{F}|$$

$$\tau = 2aF$$

$$\tau = 2(a) (I) (2a) \left(\frac{\mu_0 I}{2\pi b} \right)$$

$$\tau = \frac{2\mu_0 I^2 a^2}{\pi b}$$



16. **C**

Sol.
$$\text{disp} = \left(\frac{\text{kg}}{\text{ms}^2} \right) \left(\frac{\text{s}}{\text{m}} \right) (\text{s}) \left(\frac{\text{m}^3}{\text{kg}} \right)$$

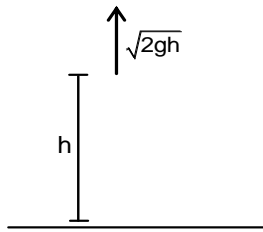
$$\text{disp} = (1) (16) \left(\frac{1}{300} \right) \left(\frac{1}{1000} \right) (1)$$

$$\text{disp in mm} = \frac{1000}{300 \times 100} = 0.03333$$

$$\Rightarrow \frac{3}{100}$$

17. **C**

Sol.



$$V^2 = 2gh$$

$$V = \sqrt{2gh}$$

$$h = -\sqrt{2gh}t + \frac{gt^2}{2}$$

$$gt^2 - 2\sqrt{2gh}t - 2h = 0$$

$$t = \frac{2\sqrt{2gh} \pm \sqrt{8gh + 8gh}}{2g}$$

$$t = \frac{2\sqrt{2gh} + 4\sqrt{gh}}{2g} \quad \text{as cannot be negative.}$$

$$\therefore t = (2 + \sqrt{2})\sqrt{\frac{h}{g}} \Rightarrow 3.4\sqrt{\frac{h}{g}}$$

18. **B**

Sol. $\ln|R| = \ln|R_0| - \lambda t$

and $T_{1/2} \propto \frac{1}{\lambda}$

where 'N' is slope

$$T_{1/2} (A) : T_{1/2} (B) : T_{1/2} (C) = \frac{10}{6} : \frac{5}{6} : \frac{5}{2}$$

$$= 2 : 1 : 3$$

19. **A**

Sol. Power delivered = 1000 W

Voltage = 220 V

$$\text{Transmission 'I'} = \frac{1000}{220}$$

Power loss = I^2R

$$\text{Efficiency} = \frac{1000 \times 100}{1000 + I^2R}$$

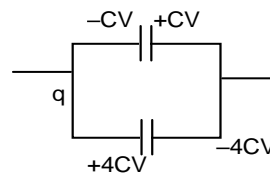
20. **A**

Sol. $\frac{4cV - q}{2\ell} = \frac{-cV + q}{c}$ (as same point)

$$4cV - q = -2cV + 2q$$

$$q = 2cV$$

$$\text{Energy} = \frac{(2cV)^2}{4c} + \frac{(cV)^2}{2c} \Rightarrow \frac{3cV^2}{2}$$



21. **195.00**

Sol. $\vec{F} = (\hat{i} + 2\hat{j} + 3\hat{k})N$

$$\vec{r} = ((4-1)\hat{i} + (3-2)\hat{j} + (-1-1)\hat{k})$$

$$\vec{\tau} = \vec{r} \times \vec{F}$$

$$= (3\hat{i} + \hat{j} - 2\hat{k}) \times (\hat{i} + 2\hat{j} + 3\hat{k})$$

$$\hat{i} \quad \hat{j} \quad \hat{k}$$

$$3 \quad 1 \quad -2 \Rightarrow \hat{i}(3+4) - \hat{j}(11) + (6-1)\hat{k}$$

$$1 \quad 2 \quad 3 \quad \quad \quad 7\hat{i} - 11\hat{j} + 5\hat{k}$$

$$|\vec{\tau}| = \sqrt{121 + 25 + 49}$$

$$|\vec{\tau}| = \sqrt{195} \quad ; \quad x = 195$$

22. **51.00**

Sol. $M_0 = 200 \text{ MeV}/C^2$, $m = 1 \text{ GeV}/C^2$

Initial velocity of particle is ' V_0 '.

Final velocity of hydrogen atom is ' V '

$$M_0 V_0 = mV$$

$$V = \frac{M_0 V_0}{m} \quad \dots(1)$$

$$\text{Also, } \frac{1}{2} M_0 V_0^2 = \frac{1}{2} mV^2 + \frac{3}{4} \times 13.6$$

Put (1) and get answer

$$\frac{1}{2} M_0 V_0^2 = \frac{51}{4} \text{ eV}$$

Hence, $N = 51$.

23. **5.00**

Sol. $\vec{B} = \frac{\mu_0 I (200)}{2R_2} \quad R_2 = 20 \text{ cm} ; R_1 = 1 \text{ cm}$

$$e = -\frac{d\phi}{dt} = \pi(R_1)^2 (500) \frac{dB}{dt}$$

$$= \pi(R_1^2) (500) \left(\frac{\mu_0 I}{2R_2} \right) (200) (10t - 2)$$

$$= \pi \left(\frac{1}{10000} \right) \frac{(500)(200) (\mu_0) (8) (5)}{(2)}$$

$$= 16\pi^2 \times 10 \times 5 \times 10^{-7}$$

$$= 800\pi^2 \times 10^{-7}$$

$$e = 0.7887 \text{ mV}$$

$$\frac{4}{x} = 0.8 \quad ; \quad x = 5.$$

24. **50.47**

Sol. We know, $P = \sqrt{2Em}$ and $\lambda = \frac{h}{\sqrt{2Em}} \quad \dots(1)$

For 1st maxima, $2^{\text{nd}} \sin \theta = \lambda$

Put (1) and get the answer

$$E = 50.47 \text{ eV.}$$

25. **50.00**

Sol. Image by objective must be at focus of eye piece.

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f_o}$$

$$\frac{1}{5} - \frac{1}{u} = \frac{1}{1} ; u = -\frac{5}{4} \text{ cm}$$

Hence, $N = 50$.

PART –B (CHEMISTRY)

26. A

Sol. In solid state PCl_5 exists as an ionic solid with constituent ions PCl_4^+ (Tetrahedral) and PCl_6^- (Octahedral)

27. C

Sol. According to Aufbau's principal, the increasing energy of atomic orbitals for sixth period element follows the order $6s < 4f < 5d < 6p$

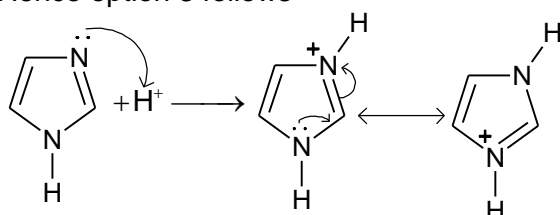
28. C

Sol. B is least basic as lone pair of electron is present in resonance so as to make the system aromatic in nature

D is most basic as it results in formation of equivalent resonating structures upon attack of H^+
Among A and C, the former is less basic as sp^2 hybridisation of nitrogen decrease its basic strength.

Hence option 3 follows

Sol.



29. D

Sol. At CMC, the particles cluster together through lyophobic end to form associated colloid called micelle. Further all lyophilic ends (polar head) get projected towards water.

30. B

Sol. Tyrosine is a non essential amino acid.

31. C

Sol. For A

$$\frac{0.693}{300} = \frac{2.303}{t} \log \frac{A_0}{A_t}$$

For B

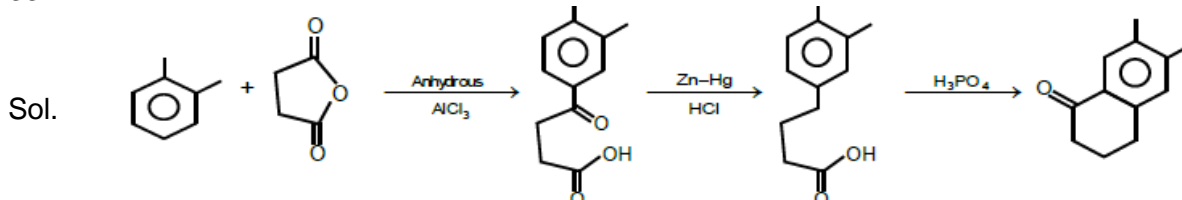
$$\frac{0.693}{180} = \frac{2.303}{t} \log \frac{B_0}{B_t}$$

Given $A_0 = B_0$ & $A_t = 4B_t$ Substituting & solving we get $t = 900$ s

32. A

Sol. In water gas shift reaction carbon monoxide is oxidized into carbon dioxide by treating it with steam in presence of catalyst.

33. B



34. D

Sol. $\rho = \frac{M}{V}$

$$\therefore 6.17 = \frac{2}{N_A} \times \frac{M_{X_2}}{(300 \times 10^{-10})^3}$$

Solving $M_{X_2} = 50 \text{ g}$

$$\begin{aligned} \therefore \text{No. of molecules in 200 g} \\ = \frac{200}{50} \times N_A = 4N_A \end{aligned}$$

35. A

Sol. Among its different uses noradrenaline is used as an anti-depressant.

36. D

Sol. With decrease in inter-nuclear distance, the potential energy of the system decreases, reaches a minimum value and then sharply increases due to rise in inter-electronic as well as inter-nuclear repulsions

37. B

Sol. In endothermic reaction formation of reactants is favoured upon decrease in temperature. Addition of inert gas at constant volume and temperature has no effect on equilibrium.

38. C

Sol. LiAlH_4 is a versatile reducing agent which can be used for reduction of cyanide into 1° amine.

39. C

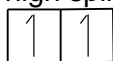
Sol. Esters are susceptible to reaction in basic medium.

40. C

Sol. Excess of nitrogen and phosphorus is primarily responsible for eutrophication and hence an indicator of polluted environment.

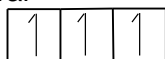
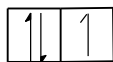
41. C

Sol. Octahedral high spin

 d^6 

$$\therefore \text{CFSE} = 4(-0.4\Delta_0) + 2(0.6\Delta_0) = -0.44\Delta_0$$

Tetrahedral

 d^6 

$$\therefore \text{CFSE} = 3(-0.6\Delta_t) + 3(0.4\Delta_t) = -0.6\Delta_0$$

42. B

Sol. $\Delta R_1 = \frac{a_0}{3}(16-9)$

$$\Delta R_2 = \frac{a_0}{2}(16-9)$$

$$\therefore \frac{\Delta R_1}{\Delta R_2} = \frac{2}{3}$$

43. C

Sol. B is the most acidic as it is active methylene group. D is least acidic due to cross-conjugation in conjugate base.

∴ Option 3 follows

44. A

Sol. Gd : [Xe]4f⁷5d¹6s²

∴ Gd³⁺ is [Xe]4f⁷

Also $\mu = \sqrt{n(n+2)}$ B.M

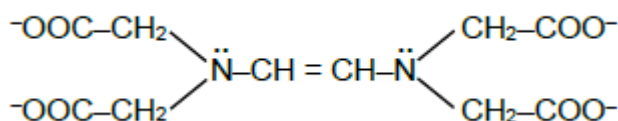
= $\sqrt{7 \times 9}$ B.M = 7.9 B.M

45. B

Sol. Ellingham diagram provides information on Gibb's free energy for formation of oxides as a function of temperature.

46. 6

Sol. EDTA as shown is hexadentate



47. 18

Sol. $C_3H_8 + 5O_2 \longrightarrow 3CO_2 + 4H_2O$

$C_4H_{10} + \frac{13}{2}O_2 \longrightarrow 4CO_2 + 5H_2O$

∴ 2 mol C₄H₁₀ is given

∴ 13 mol O₂ is required for combustion of Butane

∴ Total mol of O₂ = 5 + 13 = 18

48. -6

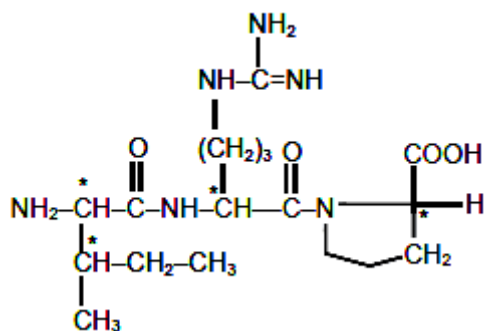
Sol. $\Delta G^\circ = -nFE^\circ$

∴ $17.37 \times 10^3 = -3 \times 96500 \times E^\circ$

∴ $E^\circ = -6 \times 10^{-2}$ V

49. 4

Sol. The structure of the given compound is as show below



50. 37

Sol. Mass of CO₂ dissolve at 3 bar pressure in 1 kg water(which is same as 1 litre since density is 1 gm/mL) = 4.4 gm = 0.1 mol.

For weak electrolytes of Ostwald's dilution law we have $pH = \frac{1}{2}(pK_a - \log C)$

∴ $pH = \frac{1}{2}[6.4 + 1] = 3.7 = 37 \times 10^{-1}$

PART-C (MATHEMATICS)

51. A

Sol. \therefore length of side = 4

$$\text{then } |z - \bar{z}| = 4$$

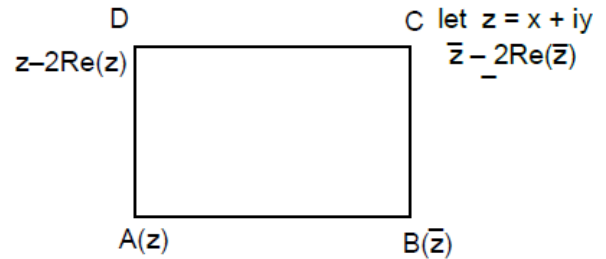
$$|2iy| = 4$$

$$|y| = 2$$

$$\text{also } |z - (z - 2\text{Re}(z))| = 4$$

$$|2x| = 4 \Rightarrow |x| = 2$$

$$|z| = \sqrt{x^2 + y^2} = 2\sqrt{2}$$



52. D

Sol. Negation of $x \leftrightarrow \sim y$

$$\equiv \sim (x \leftrightarrow \sim y)$$

$$\equiv x \leftrightarrow \sim (\sim (y))$$

$$\equiv x \leftrightarrow y$$

$$\equiv (x \wedge y) \vee (\sim x \wedge \sim y)$$

53. D

Sol. $S' = 2^{10} + 2^9 \cdot 3 + 2^8 \cdot 3^2 + \dots + 2 \cdot 3^9 + 3^{10}$

$$\text{G.P.} \rightarrow a = 2^{10}, r = \frac{3}{2}, n = 11$$

$$S' = 2^{10} \cdot \frac{\left(\left(\frac{3}{2}\right)^{11} - 1\right)}{\frac{3}{2} - 1} = 2^{11} \left(\frac{3^{11}}{2^{11}} - 1\right)$$

$$= 3^{11} - 2^{11}$$

54. B

Sol. Here $D = \begin{vmatrix} 2 & -4 & \lambda \\ 1 & -6 & 1 \\ \lambda & -10 & 4 \end{vmatrix} = (\lambda - 3)(3\lambda + 2)$

$$D = 0 \Rightarrow \lambda = 3, -\frac{2}{3}$$

$$D_1 = \begin{vmatrix} 1 & -4 & \lambda \\ 2 & -6 & 1 \\ 3 & -10 & 4 \end{vmatrix} = 2(3 - \lambda)$$

$$\text{For } \lambda = -\frac{2}{3}, D_1 \neq 0$$

55. B

Sol. $I = \int (e^{2x} + 2e^x - e^{-x} - 1)e^{(e^x + e^{-x})} dx$
 $I = \int (e^{2x} + e^x - 1)e^{(e^x + e^{-x})} dx + \int (e^x - e^{-x})e^{e^x + e^{-x}} dx$
 $I = \int (e^x + 1 - e^{-x})e^{e^x + e^{-x}} dx + e^{e^x + e^{-x}}$
 $e^x + e^{-x} + x = du$
 $(e^x - e^{-x} + 1)dx = du$
 $I = e^{e^x + e^{-x}} + e^{e^x + e^{-x}} = e^{e^x + e^{-x}} (e^x + 1)$ then $g(x) = e^x + 1$
 $g(0) = 2$

56. C

Sol. a, b, c are in AP then

$$2b = a + c$$

$$28 = 3^{2\sin 2\theta - 1} + 3^{4 - 2\sin 2\theta}$$

Put $3^{2\sin 2\theta} = x$

$$28 = \frac{x}{3} + \frac{81}{x} \Rightarrow x^2 - 84x + 243 = 0$$

$$(x - 3)(x - 81) = 0$$

$$3^{2\sin 2\theta} = 3 \text{ or } 3^4$$

$$2\sin 2\theta = 1 \text{ or } 4$$

$$\sin 2\theta = \frac{1}{2}$$

terms are 1, 14, 27,.....then $T_6 = 1 + 5(13)$

57. D

Sol. $n(C) = 73, \quad n(T) = 65, \quad n(C \cap T) = x$

$$n(C \cup T) \leq 100$$

$$\Rightarrow n(C) + n(T) - n(C \cap T) \leq 100$$

$$\Rightarrow x \geq 38$$

$$n(C \cap T) \leq \min(n(C), n(T)) \Rightarrow x \leq 65$$

$$\Rightarrow 38 \leq x \leq 65$$

58. B

Sol. $y^2 = 4x$ and $x^2 = 4y$

any tangent of $y^2 = 4x$ is $y = mx + \frac{1}{m}$

it also tangent for $x^2 = 4y$

$$\therefore \frac{1}{m} = -m^2 \Rightarrow m = -1$$

$$\therefore \text{common tangent is } y = -x - 1, \text{ it also touches } x^2 + y^2 = c^2$$

$$\therefore 1 = c^2 \cdot (1 + 1) \Rightarrow c^2 = \frac{1}{2}$$

59. D

Sol. $\therefore x^2 = |x|^2 = t$ let
 $9t^2 - 18t + 5 = 0$
 $(3t - 1)(3t - 5) = 0$
 $|x| = \frac{1}{3}, \frac{5}{3}$
 Product of roots $= \frac{1}{3} \left(-\frac{1}{3}\right) \left(\frac{5}{3}\right) \left(\frac{-5}{3}\right) = \frac{25}{81}$

60. B

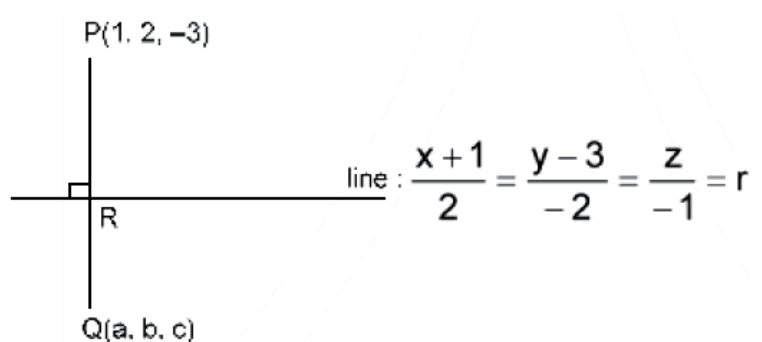
Sol. $I = \int_{-\pi/2}^{\pi/2} \frac{1}{1 + e^{\sin x}} dx$. $I = \int_{-\pi/2}^{\pi/2} \frac{1}{1 + e^{\sin x}} dx$
 $I = \int_{-\pi/2}^{\pi/2} \frac{e^{\sin x}}{e^{\sin x} + 1} dx$ $\left\{ \begin{array}{l} \text{Replace} \\ x \rightarrow (a + b + x) \end{array} \right.$
 $\int_a^b (f(x)) dx = \int_c^b f(a + b + x) dx$
 $2I = \int_{-\pi/2}^{\pi/2} 1 dx \Rightarrow I = \frac{1}{2} \int_{-\pi/2}^{\pi/2} dx$
 $I = \frac{1}{2} [x]_{-\pi/2}^{\pi/2} \Rightarrow I = \frac{\pi}{2}$

61. A

Sol. $S = \tan^{-1} \frac{1}{3} + \tan^{-1} \frac{1}{7} + \tan^{-1} \frac{1}{13} + \dots$ upto 10 term
 $S = \tan^{-1} \left(\frac{2-1}{1+1.2}\right) + \tan^{-1} \left(\frac{3-2}{1+2.3}\right) + \tan^{-1} \left(\frac{4-3}{1+3.4}\right) + \dots + \tan^{-1} \left(\frac{11-10}{1+11.10}\right)$
 $S = (\tan^{-1} 2 - \tan^{-1} 1) + (\tan^{-1} 3 - \tan^{-1} 2) + \dots + (\tan^{-1} 11 - \tan^{-1} 10)$
 $S = \tan^{-1} 11 - \tan^{-1} 1$
 $S = \tan^{-1} (11) - \frac{\pi}{4}$
 $\tan(S) = \frac{5}{6}$

62. C

Sol. $R(-1 + 2r, 3 - 2r, -r)$
 dir's of PR are $(2 - 2r, -1 + 2r, -3 + r)$
 Then
 $2(2 - 2r) + 2(1 - 2r) + 1(3 - r) = 0$
 $9 - 9r = 0 \Rightarrow r = 1$
 $R(1, 1, -1)$
 then $a + 1 = 2$ $b + 2 = 2$
 $c - 3 = -2$
 $a = 1$ $b = 0$
 $c = 1$
 $\therefore a + b + c = 2$



63. C

Sol. Given $\frac{dy}{2+y} = \frac{-e^x dx}{5+e^x}$

$$\ln(2+y) = -\ln(5+e^x) + \ln C$$

$$y = \frac{C}{5+e^x} - 2$$

$$y(0) = 1 \quad \therefore \quad C = 18$$

$$y = \frac{18}{5+e^x} - 2$$

$$\therefore y = (\log_e 13) = -1$$

64. C

Sol. $P(x) = 0$

$$x^2 - x - 2 = 0$$

$$(x-2)(x+1) = 0$$

$$x = 2, -1 \quad \therefore \quad \alpha = 2$$

$$\begin{aligned} \text{Now } \lim_{x \rightarrow 2^+} \frac{\sqrt{1 - \cos(x^2 - x - 2)}}{x - 2} &\Rightarrow \lim_{x \rightarrow 2^+} \frac{\sqrt{2 \sin^2 \left(\frac{x^2 - x - 2}{2} \right)}}{x - 2} \\ \Rightarrow \lim_{x \rightarrow 2^+} \frac{\left| \sin \left(\frac{x^2 - x - 2}{2} \right) \right|}{x - 2} &\Rightarrow \text{for } x \rightarrow 2^+, \frac{x^2 - x - 2}{2} \rightarrow 0^+ \\ \lim_{x \rightarrow 2^+} \frac{\sqrt{2} \sin \left(\frac{x^2 - x - 2}{2} \right) \cdot \frac{x^2 - x - 2}{2}}{\left(\frac{x^2 - x - 2}{2} \right) \cdot (x - 2)} &\Rightarrow \lim_{x \rightarrow 2^+} \frac{1}{\sqrt{2}} \cdot \frac{(x-2)(x+1)}{(x-2)} = \frac{3}{\sqrt{2}} \end{aligned}$$

65. A

Sol. For ellipse $\frac{x^2}{16} + \frac{y^2}{9} = 1$, $a = 4$, $b = 3$, $e = \sqrt{1 - \frac{9}{16}} = \frac{\sqrt{7}}{4}$

A and B are foci then $PA + PB = 2a = 2(4) = 8$

66. D

Sol. $f(x)$ is differentiable then will also continuous then $f(\pi) = -1$, $f(\pi^+) = -k_2$

$$k_2 = 1$$

$$\text{Now } f'(x) = \begin{cases} 2k_1(x - \pi) & x \leq \pi \\ -k_2 \sin x & x > \pi \end{cases} \text{ then } f'(\pi^-) = f'(\pi^+) = 0$$

$$f''(x) = \begin{cases} 2k_1 & x \leq \pi \\ -k_2 \cos x & x > \pi \end{cases} \text{ then } 2k_1 = k_2$$

$$k_1 = \frac{1}{2}$$

67. D

Sol. $C_3 \rightarrow C_2 - C_1$

$$f(\theta) = \begin{vmatrix} -\sin^2 \theta & -1 & 1 \\ -\cos^2 \theta & -1 & 1 \\ 12 & -2 & -2 \end{vmatrix} = 4(\cos^2 \theta - \sin^2 \theta) = 4(\cos 2\theta), \theta \in \left[\frac{\pi}{4}, \frac{\pi}{2} \right]$$

$$f(\theta)_{\max} = M = 0$$

$$f(\theta)_{\min} = m = -4$$

68. A

Sol. $\bar{x} = \frac{2+4+10+12+14+x+y}{7} = 8$

$$\Rightarrow 42 + x + y = 56 \quad \Rightarrow \quad x + y = 14$$

$$\sigma^2 = \frac{\sum x_i^2}{n} - \left(\frac{\sum x_i}{n} \right)^2$$

$$16 = \frac{4 + 16 + 100 + 144 + 196 + x^2 + y^2}{7} - (8)^2$$

$$\Rightarrow 16 + 64 = \frac{460 + x^2 + y^2}{7}$$

$$\Rightarrow 560 = 460 + x^2 + y^2 \quad \Rightarrow \quad x^2 + y^2 = 100 \quad \dots\dots\dots(2)$$

$$\Rightarrow xy = 48$$

$$(x - y)^2 = (x + y)^2 - 4xy = 4$$

$$|x - y| = 2$$

69. C

Sol. Equation $\frac{x^2}{5} + \frac{y^2}{4} = 1$ then $P(\sqrt{5} \cos \theta, 2 \sin \theta)$

$$(PQ)^2 = 5 \cos^2 \theta + 4(\sin \theta + 2)^2 = \cos^2 \theta + 16 \sin \theta + 20$$

$$= -\sin^2 \theta + 16 \sin \theta + 21$$

$$= 85 - (\sin \theta - 8)^2$$

$$= (PQ)_{\max}^2 = 85 - 49 = 36,$$

$$\therefore (\sin \theta - 8)^2 \in [49, 81]$$

70. C

Sol. Volume of parallelepiped $v = \left| \begin{bmatrix} \vec{a} & \vec{b} & \vec{c} \end{bmatrix} \right|$

$$v = \begin{vmatrix} 1 & 1 & n \\ 2 & 4 & -n \\ 1 & n & 3 \end{vmatrix} = \pm 158$$

$$1(12+n^2) - 1(6+n) + n(2n-4) = \pm 158$$

$$3n^2 - 5n - 152 = 0 \quad \text{or} \quad 3n^2 - 5n + 164 = 0$$

$D < 0$ (no real roots)

$$n = 8, -\frac{19}{3} \Rightarrow n = 8$$

then $\vec{b} \cdot \vec{c} = 2 + 4n - 3n = 10$
 $\vec{a} \cdot \vec{c} = 1 + n + 3n = 33$

71. 13.00

Sol. $T_{r+1} = {}^{22}C_r (x^m)^{22-r} x^{-2r}$

$$T_{r+1} = {}^{22}C_r x^{m(22-r)-2r}$$

$$22m - mr - 2r = 1$$

$$22m - 1 = r(m+2)$$

$$r = \frac{22m-1}{m+2}$$

$$r = \frac{22m+44-45}{m+2}$$

$$r = 22 - \frac{3.3.5}{m+2}$$

So possible value of $m = 1, 3, 7, 13, 43$

but ${}^{20}C_r = 1540$

only possible condition is $m = 13$

72. 08.00

Sol. $-5 < \frac{x}{2} < 5$

$$|\Rightarrow \left[\frac{x}{2} \right] = -5, -4, -3, -2, -1, 0, 1, 2, 3, 4$$

Hence, function is discontinues at $= -4, -3, -2, -1, 1, 2, 3, 4$

Number of values is 8.

73. 30.00

Sol. $2x - y + 3 = 0$ (i)

$$4x - 2y + \alpha = 0 \Rightarrow 2x - y + \frac{\alpha}{2} = 0 \quad \text{.....(ii)}$$

$$6x - 3y + \beta = 0 \Rightarrow 2x - y + \frac{\beta}{3} = 0 \quad \text{.....(iii)}$$

$$d_1 = \frac{\left| \frac{\alpha}{2} - 3 \right|}{\sqrt{2^2 + 1^2}} = \frac{1}{\sqrt{5}} \Rightarrow |\alpha - 6| = 2 \Rightarrow \alpha - 6 = 2, -2 \Rightarrow \alpha = 8, 4$$

$$d_2 = \frac{\left| \frac{\beta}{3} - 3 \right|}{\sqrt{2^2 + 1^2}} = \frac{2}{\sqrt{5}} \Rightarrow |\beta - 9| = 6 \Rightarrow \beta - 9 = 6, -6 \Rightarrow \beta = 15, 3$$

Sum of all value of α and $\beta = 30$.

74. 11.00

$$\text{Sol. } P(\text{at least 2 show 3 or 5}) = {}^4C_2 \cdot \left(\frac{2}{6}\right)^2 \left(\frac{4}{6}\right)^2 + {}^4C_3 \left(\frac{2}{6}\right)^3 \left(\frac{4}{6}\right) + {}^4C_4 \left(\frac{2}{6}\right)^4$$

$$= \frac{384 + 128 + 16}{6^4} = \frac{11}{27}$$

$$n = 27$$

\therefore expectation of number of times = np

$$= 27 \cdot \frac{11}{27} = 11$$

75. 240.00

Sol. SYLLABUS

S - 2, L - 2, A, B, Y, U

$$\text{Required} = {}^2C_1 \cdot {}^5C_2 \cdot \frac{4!}{2!} = 2 \cdot 10 \cdot \frac{24}{2} = 240$$