

FIITJEE

Solutions to JEE (Main)-2019

JEE–Main–2019 –Apr–9–First–Shift
PHYSICS, CHEMISTRY & MATHEMATICS

Time Allotted: 3 Hours

Maximum Marks: 360

- Do not open this Test Booklet until you are asked to do so.
- Please read the instructions carefully. You are allotted 5 minutes specifically for this purpose.

Important Instructions:

1. Immediately fill in the particulars on this page of the Test Booklet with *Blue / Black Ball Point Pen*. Use of pencil is strictly prohibited.
2. The Answer Sheet is kept inside this Test Booklet. When you are directed to open the Test Booklet, take out the Answer Sheet and fill in the particulars carefully.
3. The test is of **3 hours** duration.
4. The Test Booklet consists of **90** questions. The maximum marks are **360**.
5. There are **three** parts in the question paper A, B, C consisting of **Physics, Chemistry and Mathematics** having 30 questions in each part of equal weightage. Each question is allotted **4 (four)** marks for correct response.
6. *Candidates will be awarded marks as stated above in instruction No.5 for correct response of each question. One mark will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.*
7. There is only one correct response for each question. Filling up more than one response in any question will be treated as wrong response and marks for wrong response will be deducted accordingly as per instruction 6 above.
8. Use **Blue / Black Ball Point Pen only** for writing particulars / marking responses on **Side-1** and **Side-2** of the Answer Sheet. **Use of pencil is strictly prohibited.**
9. No candidate is allowed to carry any textual material, printed or written, bits of papers, pager, mobile phone, any electronic device, etc. except the Admit Card inside the examination hall / room.
10. On completion of the test, the candidate must hand over the Answer Sheet to the Invigilator on duty in the Room / Hall. **However, the candidates are allowed to take away this Test Booklet with them.**
11. **Do not fold or make any stray marks on the Answer Sheet.**

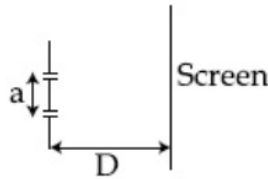
Name of the Candidate (in Capital Letters) : _____

Roll Number : _____

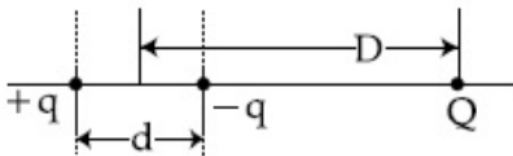
Candidate's Signature: _____

PART –A (PHYSICS)

- In the density measurement of a cube, the mass and edge length are measured as (10.00 ± 0.10) kg and (0.10 ± 0.01) m, respectively. The error in the measurement of density is:
 (A) 0.10 kg/m^3 (B) 0.31 kg/m^3
 (C) 0.07 kg/m^3 (D) 0.01 kg/m^3
- The total number of turns and cross-section area in solenoid is fixed. However, its length L is varied by adjusting the separation between windings. The inductance of solenoid will be proportional to:
 (A) $1/L$ (B) L
 (C) $1/L^2$ (D) L^2
- The figure shows a Young's double slit experimental setup. It is observed that when a thin transparent sheet of thickness t and refractive index μ is put in front of one of the slits, the central maximum gets shifted by a distance equal to n fringe widths. If the wavelength of light used is λ , t will be:



- | | |
|---|---|
| (A) $\frac{2nD\lambda}{a(\mu-1)}$
(C) $\frac{2D\lambda}{a(\mu-1)}$ | (B) $\frac{nD\lambda}{a(\mu-1)}$
(D) $\frac{D\lambda}{a(\mu-1)}$ |
|---|---|
- A system of three charges are placed as shown in the figure:



If $D \gg d$, the potential energy of the system is best given by:

- | | |
|---|---|
| (A) $\frac{1}{4\pi\epsilon_0} \left[-\frac{q^2}{d} - \frac{qQd}{D^2} \right]$
(C) $\frac{1}{4\pi\epsilon_0} \left[-\frac{q^2}{d} + \frac{2qQd}{D^2} \right]$ | (B) $\frac{1}{4\pi\epsilon_0} \left[-\frac{q^2}{d} - \frac{qQd}{2D^2} \right]$
(D) $\frac{1}{4\pi\epsilon_0} \left[+\frac{q^2}{d} - \frac{qQd}{D^2} \right]$ |
|---|---|
- A moving coil galvanometer has resistance 50Ω and it indicates full deflection at 4mA current. A voltmeter is made using this galvanometer and a $5 \text{ k}\Omega$ resistance. The maximum voltage, that can be measured using this voltmeter, will be close to:
 (A) 15 V (B) 20 V
 (C) 10 V (D) 40 V
- If 'M' is the mass of water that rises in a capillary tube of radius 'r', then mass of water which will rise in a capillary tube of radius '2r' is:
 (A) $4 M$ (B) $\frac{M}{2}$
 (C) M (D) $2 M$

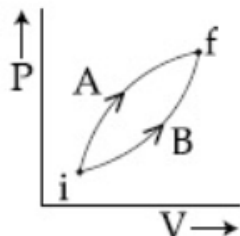
7. An NPN transistor is used in common emitter configuration as an amplifier with $1\text{ k}\Omega$ load resistance. Signal voltage of 10 mV is applied across the base-emitter. This produces a 3 mA change in the collector current and $15\text{ }\mu\text{A}$ change in the base current of the amplifier. The input resistance and voltage gain are:
 (A) $0.67\text{ k}\Omega, 300$ (B) $0.67\text{ k}\Omega, 200$
 (C) $0.33\text{ k}\Omega, 1.5$ (D) $0.33\text{ k}\Omega, 300$

8. An HCl molecule has rotational, translational and vibrational motions. If the rms velocity of HCl molecules in its gaseous phase is \bar{v} , m is its mass and k_B is Boltzmann constant, then its temperature will be:

(A) $\frac{m\bar{v}^2}{3k_B}$ (B) $\frac{m\bar{v}^2}{7k_B}$
 (C) $\frac{m\bar{v}^2}{5k_B}$ (D) $\frac{m\bar{v}^2}{6k_B}$

9. The electric field of light wave is given as $\vec{E} = 10^{-3} \cos\left(\frac{2\pi x}{5 \times 10^{-7}} - 2\pi \times 6 \times 10^{14} t\right) \times \frac{\text{N}}{\text{C}}$. This light falls on a metal plate of work function 2 eV . The stopping potential of the photo-electrons is:
 (A) 0.48 V (B) 2.48 V
 (C) 0.72 V (D) 2.0 V

10. Following figure shows two processes A and B for a gas. If ΔQ_A and ΔQ_B are the amount of heat absorbed by the system in two cases, and ΔU_A and ΔU_B are changes in internal energies, respectively, then:



(A) $\Delta Q_A = \Delta Q_B; \Delta U_A = \Delta U_B$ (B) $\Delta Q_A > \Delta Q_B; \Delta U_A = \Delta U_B$
 (C) $\Delta Q_A < \Delta Q_B; \Delta U_A < \Delta U_B$ (D) $\Delta Q_A > \Delta Q_B; \Delta U_A > \Delta U_B$

11. A uniform cable of mass 'M' and length 'L' is placed on a horizontal surface such that its $\left(\frac{1}{n}\right)^{\text{th}}$ part is hanging below the edge of the surface. To lift the hanging part of the cable upto the surface, the work done should be:

(A) $nMgL$ (B) $\frac{MgL}{2n^2}$
 (C) $\frac{2MgL}{n^2}$ (D) $\frac{MgL}{n^2}$

12. The following bodies are made to roll up (without slipping) the same inclined plane from a horizontal place: (i) a ring of radius R, (ii) a solid cylinder of radius $\frac{R}{2}$ and (iii) a solid sphere of radius $\frac{R}{4}$. If, in each case, the speed of the center of mass at bottom of the incline is same, the ratio of the maximum heights they climb is:

(A) $10 : 15 : 7$ (B) $14 : 15 : 20$
 (C) $4 : 3 : 2$ (D) $2 : 3 : 4$

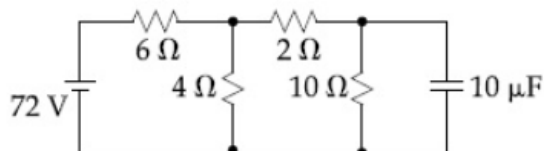
13. A signal $A \cos \omega t$ is transmitted using $v_0 \sin \omega_0 t$ as carrier wave. The correct amplitude modulated (AM) signal is:

(A) $v_0 \sin[\omega_0(1 + 0.01A \sin \omega t)t]$ (B) $v_0 \sin \omega_0 t + \frac{A}{2} \sin(\omega_0 - \omega)t + \frac{A}{2} \sin(\omega_0 + \omega)t$
 (C) $v_0 \sin \omega_0 t + A \cos \omega t$ (D) $(v_0 + A) \cos \omega t \sin \omega_0 t$

14. A concave mirror for face viewing has focal length of 0.4 m. The distance at which you hold the mirror from your face in order to see your image upright with a magnification of 5 is:

(A) 0.16 m (B) 1.60 m
 (C) 0.24 m (D) 0.32 m

15. Determine the charge on the capacitor in the following circuit:



(A) 200 μC (B) 60 μC
 (C) 10 μC (D) 2 μC

16. A rectangular coil (Dimension 5 cm \times 2 cm) with 100 turns, carrying a current of 3 A in the clock-wise direction, is kept centered at the origin and in the X-Z plane. A magnetic field of 1 T is applied along X-axis. If the coil is tilted through 45° about Z-axis, then the torque on the coil is:

(A) 0.42 Nm (B) 0.55 Nm
 (C) 0.27 Nm (D) 0.38 Nm

17. A stationary horizontal disc is free to rotate about its axis. When a torque is applied on it, its kinetic energy as a function of θ , where θ is the angle by which it has rotated, is given as $k\theta^2$. If its moment of inertia is I then the angular acceleration of the disc is:

(A) $\frac{k}{I} \theta$ (B) $\frac{k}{2I} \theta$
 (C) $\frac{k}{4I} \theta$ (D) $\frac{2k}{I} \theta$

18. A simple pendulum oscillating in air has period T . The bob of the pendulum is completely immersed in a non-viscous liquid. The density of the liquid is $\frac{1}{16}$ th of the material of the bob.

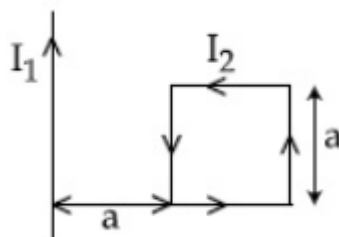
If the bob is inside liquid all the time, its period of oscillation in this liquid is:

(A) $2T \sqrt{\frac{1}{10}}$ (B) $2T \sqrt{\frac{1}{14}}$
 (C) $4T \sqrt{\frac{1}{15}}$ (D) $4T \sqrt{\frac{1}{14}}$

19. For a given gas at 1 atm pressure, rms speed of the molecules is 200 m/s at 127°C. At 2 atm pressure and at 227°C, the rms speed of the molecules will be:

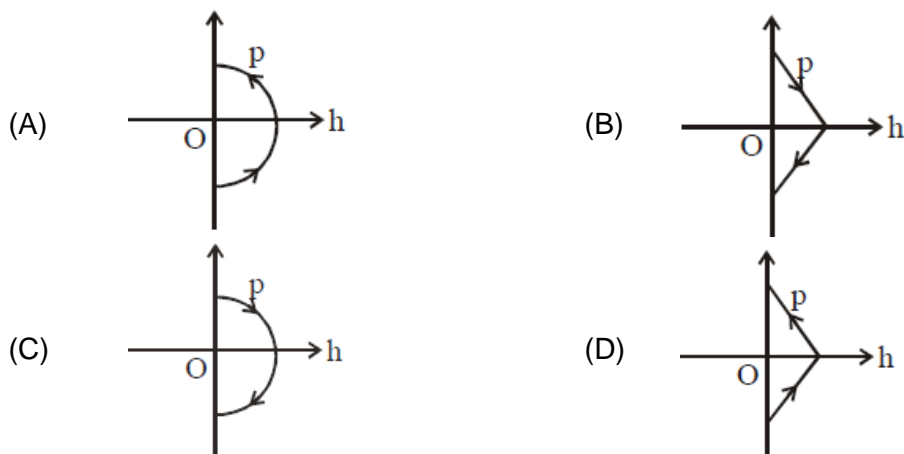
(A) 80 m/s (B) $80\sqrt{5}$ m/s
 (C) 100 m/s (D) $100\sqrt{5}$ m/s

20. The magnetic field of a plane electromagnetic wave is given by:
 $\vec{B} = B_0 \hat{i} [\cos(kz - \omega t)] + B_1 \hat{j} \cos(kz - \omega t)$ where $B_0 = 3 \times 10^{-5} \text{T}$ and $B_1 = 2 \times 10^{-6} \text{T}$. The rms value of the force experienced by a stationary charge $Q = 10^{-4} \text{C}$ at $z = 0$ is closet to:
 (A) 0.9 N (B) 0.6 N
 (C) 0.1 N (D) $3 \times 10^{-2} \text{N}$
21. The stream of a river is flowing with a speed of 2 km/h. A swimmer can swim at a speed of 4 km/h. What should be the direction of the swimmer with respect to the flow of the river to cross the river straight?
 (A) 60° (B) 90°
 (C) 120° (D) 150°
22. A rigid square loop of side 'a' and carrying current I_2 is laying on a horizontal surface near a long current I_1 wire in the same plane as shown in figure. The net force on the loop due to the wire will be:

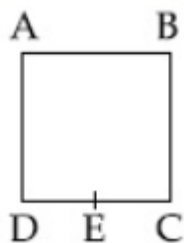


- (A) Repulsive and equal to $\frac{\mu_0 I_1 I_2}{2\pi}$ (B) Attractive and equal to $\frac{\mu_0 I_1 I_2}{3\pi}$
 (C) Zero (D) Repulsive and equal to $\frac{\mu_0 I_1 I_2}{4\pi}$
23. Taking the wavelength of first Balmer line in hydrogen spectrum ($n = 3$ to $n = 2$) as 660 nm , the wavelength of the 2nd Balmer line ($n = 4$ to $n = 2$) will be
 (A) 889.2 nm (B) 642.7 nm
 (C) 448.9 nm (D) 388.9 nm
24. A solid sphere of mass 'M' and radius 'a' is surrounded by a uniform concentric spherical shell of thickness 2a and mass 2M. The gravitational field at distance '3a' from the centre will be:
 (A) $\frac{2GM}{3a^2}$ (B) $\frac{2GM}{9a^2}$
 (C) $\frac{GM}{9a^2}$ (D) $\frac{GM}{3a^2}$
25. A string is clamed at both the ends and it is vibrating in its 4th harmonic. The equation of the stationary wave is $Y = 0.3 \sin(0.157x) \cos(200\pi t)$. The length of the string is: (all quantities are in SI units)
 (A) 80 m (B) 60 m
 (C) 40 m (D) 20 m

26. A ball is thrown vertically up (taken as +z-axis) from the ground. The correct momentum-height (p-h) diagram is:



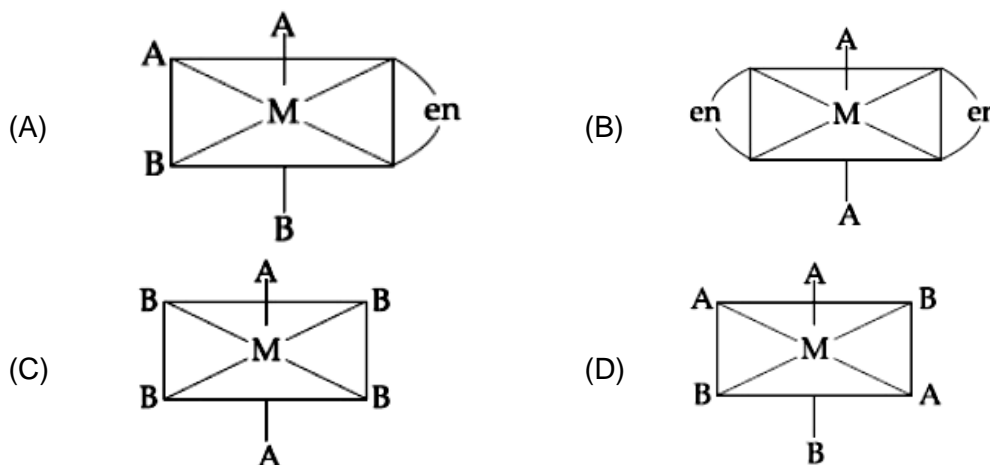
27. A capacitor with capacitance $5 \mu\text{F}$ is charged to $5 \mu\text{C}$. If the plates are pulled apart to reduce the capacitance to $2 \mu\text{F}$, how much work is done?
 (A) $3.75 \times 10^{-6} \text{ J}$ (B) $2.55 \times 10^{-6} \text{ J}$
 (C) $6.25 \times 10^{-6} \text{ J}$ (D) $2.16 \times 10^{-6} \text{ J}$
28. A body of mass 2 kg makes an elastic collision with a second body at rest and continues to move in the original direction but with one fourth of its original speed. What is the mass of the second body?
 (A) 1.5 kg (B) 1.2 kg
 (C) 1.8 kg (D) 1.0 kg
29. The pressure wave, $P = 0.01 \sin[1000t - 3x] \text{ NM}^{-2}$, corresponds to the sound produced by a vibrating blade on a day when atmospheric temperature is 0°C . On some other day when temperature is T , the speed of sound produced by the same blade and at the same frequency is found to be 336 ms^{-1} . Approximate value of T is:
 (A) 12°C (B) 11°C
 (C) 15°C (D) 4°C
30. A wire of resistance R is bent to form a square ABCD as shown in the figure. The effective resistance between E and C is: (E is mid-point of arm CD)



- (A) $\frac{1}{16}R$ (B) $\frac{7}{64}R$
 (C) $\frac{3}{4}R$ (D) R

PART – B (CHEMISTRY)

31. Magnesium powder burns in air to give:
 (A) MgO and $Mg(NO_3)_2$ (B) MgO and Mg_3N_2
 (C) MgO only (D) $Mg(NO_3)_2$ and Mg_3N_2
32. The number of water molecule(s) not coordinated to copper ion directly in $CuSO_4 \cdot 5H_2O$, is:
 (A) 1 (B) 3
 (C) 2 (D) 4
33. The one that will show optical activity is: (en = ethane-1, 2-diamine)



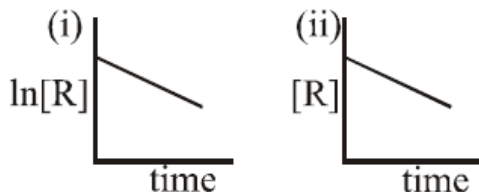
34. Consider the van der Waals constants, a and b, for the following gases.

Gas	Ar	Ne	Kr	Xe
$a/(\text{atm dm}^6\text{mol}^{-2})$	1.3	0.2	5.1	4.1
$b/(10^{-2}\text{dm}^3\text{mol}^{-1})$	3.2	1.7	1.0	5.0

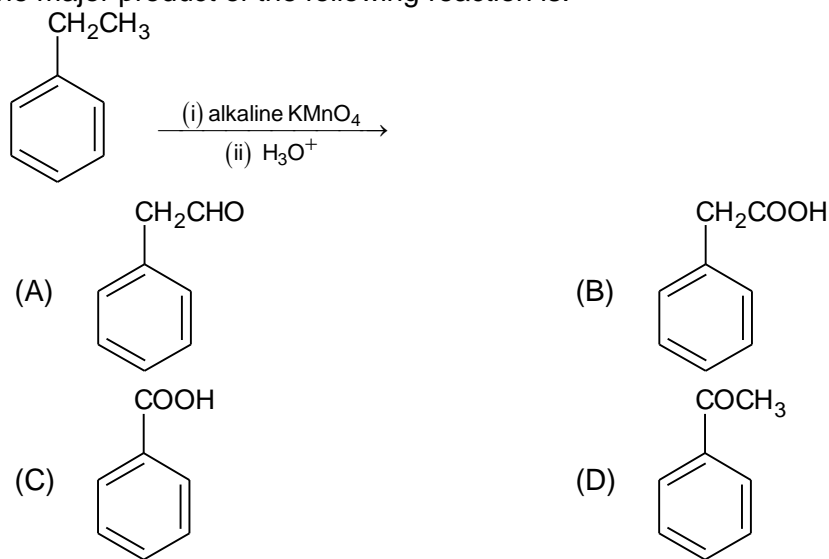
Which gas is expected to have the highest critical temperature?

- (A) Ar (B) Xe
 (C) Kr (D) Ne
35. Among the following, the molecule expected to be stabilized by anion formation is:
 (A) F_2 (B) C_2
 (C) O_2 (D) NO
36. Liquid 'M' and liquid 'N' form an ideal solution. The vapour pressures of pure liquids 'M' and 'N' are 450 and 700 mm Hg, respectively at the same temperature. Then correct statement is:
 (x_M = mole fraction of 'M' in solution; x_N = mole fraction of 'N' in solution;
 y_M = mole fraction of 'M' in vapour phase; y_N = mole fraction of 'M' in vapour phase)
- (A) $\frac{x_M}{x_N} > \frac{y_M}{y_N}$ (B) $\frac{x_M}{x_N} = \frac{y_M}{y_N}$
 (C) $(x_M - y_M) < (x_N - y_N)$ (D) $\frac{x_M}{x_N} < \frac{y_M}{y_N}$
37. Among the following the set of parameters that represents path functions, is:
 (a) q + w (b) q
 (c) w (d) H – TS
 (A) (b) and (c) (B) (b), (c) and (d)
 (C) (a), (b) and (c) (D) (a) and (d)

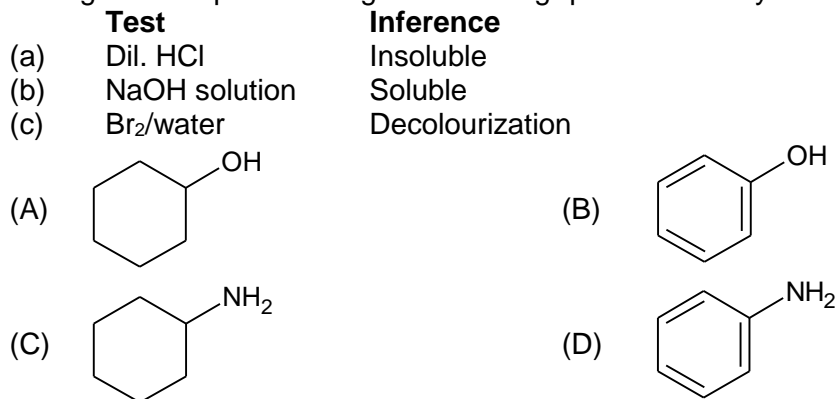
38. The degenerate orbitals of $[\text{Cr}(\text{H}_2\text{O})_6]^{3+}$ are:
 (A) d_{xz} and d_{yz} (B) $d_{x^2-y^2}$ and d_{xy}
 (C) d_{yz} and d_{z^2} (D) d_{z^2} and d_{xz}
39. The aerosol is a kind of colloid in which:
 (A) solid is dispersed in gas (B) gas is dispersed in solid
 (C) liquid is dispersed in water (D) gas is dispersed in liquid
40. The given plots represent the variation of the concentration of a reactant R with time for two different reactions (i) and (ii). The respective orders of the reactions are:



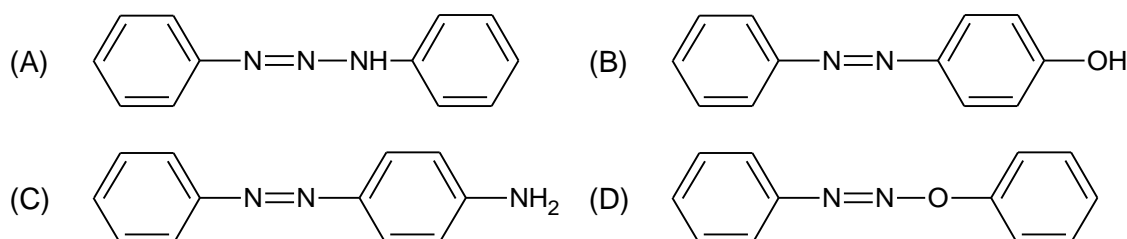
- (A) 1, 1 (B) 0, 2
 (C) 0, 1 (D) 1, 0
41. The major product of the following reaction is:



42. The organic compound that gives following qualitative analysis is:

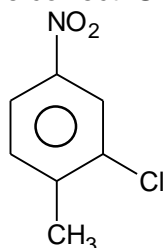


43. Aniline dissolved in dilute HCl is reacted with sodium nitrite at 0°C. This solution was added dropwise to a solution containing equimolar mixture of aniline and phenol in dil. HCl. The structure of the major product is:



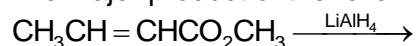
44. Excessive release of CO₂ into the atmosphere results in:
 (A) formation of smog (B) depletion of ozone
 (C) global warming (D) polar vortex
45. The ore that contains the metal in the form of fluoride is:
 (A) saphalerite (B) malachite
 (C) magnetite (D) cryolite

46. The correct IUPAC name of the following compound is



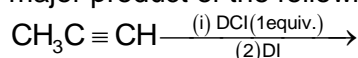
- (A) 5-chloro-4-methyl-1-nitrobenzene (B) 2-methyl-5-nitro-1-chlorobenzene
 (C) 3-chloro-4-methyl-1-nitrobenzene (D) 2-chloro-1-methyl-4-nitrobenzene

47. The major product of the following reaction is :



- (A) CH₃CH₂CH₂CHO (B) CH₃CH = CHCH₂OH
 (C) CH₃CH₂CH₂CO₂CH₃ (D) CH₃CH₂CH₂CH₂OH
48. The element having greatest difference between its first and second ionization energies, is
 (A) Ca (B) K
 (C) Ba (D) Sc
49. For a reaction,
 N₂(g) + 3H₂(g) → 2NH₃(g); identify dihydrogen (H₂) as a limiting reagent in the following reaction mixtures.
 (A) 14g of N₂ + 4g of H₂ (B) 28g of N₂ + 6g of H₂
 (C) 56g of N₂ + 10g of H₂ (D) 35g of N₂ + 8g of H₂

50. The major product of the following reaction is :

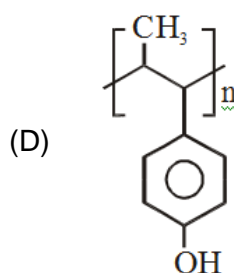
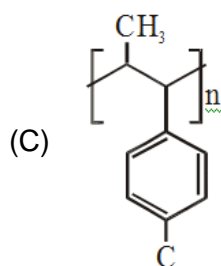
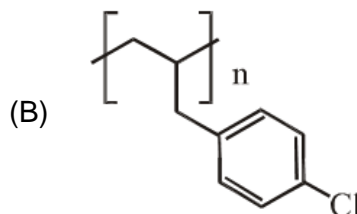
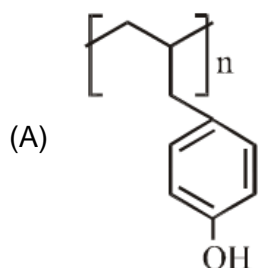
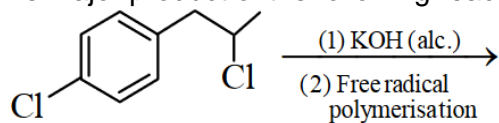


- (A) CH₃CD(I)CHD(Cl) (B) CH₃C(I)(Cl)CHD₂
 (C) CH₃CD₂CH(Cl)(I) (D) CH₃CD(Cl)CHD(I)
51. The osmotic pressure of a dilute solution of an ionic compound XY in water is four times that of a solution of 0.01 M BaCl₂ in water. Assuming complete dissociation of the given ionic compounds in water, the concentration of XY (in mol L⁻¹) in solution is
 (A) 4 × 10⁻⁴ (B) 6 × 10⁻²
 (C) 16 × 10⁻⁴ (D) 4 × 10⁻²

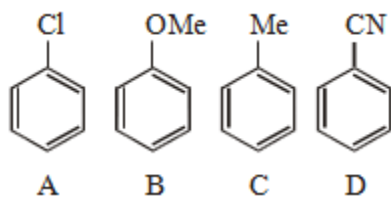
52. For any given series of spectral lines of atomic hydrogen, let $\Delta\bar{\nu} = \Delta\bar{\nu}_{\max} - \Delta\bar{\nu}_{\min}$ be the difference in maximum and minimum frequencies in cm^{-1} . the ration $\Delta\bar{\nu}_{\text{Lyman}} / \Delta\bar{\nu}_{\text{Balmer}}$ is

- (A) 5 : 4 (B) 4 : 1
(C) 9 : 4 (D) 27 : 5

53. The major product of the following reaction is:



54. The increasing order of reactivity of the following compounds towards aromatic electrophilic substitution reaction is



- (A) $D < B < A < C$ (B) $A < B < C < D$
(C) $D < A < C < B$ (D) $B < C < A < D$

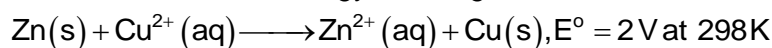
55. C_{60} , an allotrope of carbon contains:

- (A) 20 hexagons and 12 pentagons. (B) 12 hexagons and 20 pentagons.
(C) 18 hexagons and 14 pentagons. (D) 16 hexagons and 16 pentagons

56. The correct order of the oxidation states of nitrogen in NO , N_2O , NO_2 and N_2O_3 is:

- (A) $\text{N}_2\text{O} < \text{N}_2\text{O}_3 < \text{NO} < \text{NO}_2$ (B) $\text{NO}_2 < \text{NO} < \text{N}_2\text{O}_3 < \text{N}_2\text{O}$
(C) $\text{NO}_2 < \text{N}_2\text{O}_3 < \text{NO} < \text{N}_2\text{O}$ (D) $\text{N}_2\text{O} < \text{NO} < \text{N}_2\text{O}_3 < \text{NO}_2$

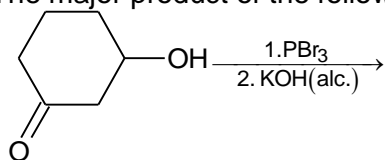
57. The standard Gibbs energy for the given cell reaction in kJ mol^{-1} at 298 K is:



[Faraday's constant $F = 96500 \text{ C mol}^{-1}$]

- (A) -192 (B) 384
(C) -384 (D) 192

58. The major product of the following reaction is:



- (A)
- (B)
- (C)
- (D)

59. Which of the following statements is not true about sucrose?

- (A) The glycosidic linkage is present between C_1 of α -glucose and C_1 of β -fructose
 (B) It is a non-reducing sugar
 (C) It is also named as invert sugar
 (D) On hydrolysis it produces glucose and fructose

60. Match the catalysis (Column – I) with products (Column-II)

- | Column-I
Catalyst | Column-II
Product |
|--|--|
| (a) V_2O_5 | (i) Polyethylene |
| (b) $\text{TiCl}_4/\text{Al}(\text{Me})_3$ | (ii) Ethanal |
| (c) PdCl_2 | (iii) H_2SO_4 |
| (d) Iron oxide | (iv) NH_3 |
| (A) (a)-(iii); (b)-(iv); (c)-(i); (d)-(ii) | (B) (a)-(iv); (b)-(iii); (c)-(ii); (d)-(i) |
| (C) (a)-(ii); (b)-(iii); (c)-(i); (d)-(iv) | (D) (a)-(iii); (b)-(i); (c)-(ii); (d)-(iv) |

PART-C (MATHEMATICS)

61. If the function $f: \mathbb{R} - \{1, -1\} \rightarrow A$ defined by $f(x) = \frac{x^2}{1-x^2}$, is surjective, then A is equal to:
 (A) $\mathbb{R} - [-1, 0)$ (B) $\mathbb{R} - (-1, 0)$
 (C) $\mathbb{R} - \{-1\}$ (D) $[0, \infty]$
62. Let $p, q \in \mathbb{R}$. if $2 - \sqrt{3}$ is a root of the quadratic equation, $x^2 + px + q = 0$, then:
 (A) $q^2 + 4p + 14 = 0$ (B) $p^2 - 4q + 12 = 0$
 (C) $p^2 - 4q - 12 = 0$ (D) $q^2 - 4p - 16 = 0$
63. Let $\vec{\alpha} = 3\hat{i} + \hat{j}$ and $\vec{\beta} = 2\hat{i} - \hat{j} + 3\hat{k}$. If $\vec{\beta} = \vec{\beta}_1 - \vec{\beta}_2$, where $\vec{\beta}_1$ is parallel to $\vec{\alpha}$ and $\vec{\beta}_2$ is perpendicular to $\vec{\alpha}$, then $\vec{\beta}_1 \times \vec{\beta}_2$ is equal to:
 (A) $\frac{1}{2}(-3\hat{i} + 9\hat{j} + 5\hat{k})$ (B) $\frac{1}{2}(3\hat{i} - 9\hat{j} + 5\hat{k})$
 (C) $-3\hat{i} + 9\hat{j} + 5\hat{k}$ (D) $3\hat{i} - 9\hat{j} - 5\hat{k}$
64. The integral $\int \sec^{2/3} x \cos \sec^{4/3} x \, dx$ is equal to: (Here C is a constant of integration)
 (A) $3 \tan^{-1/3} x + C$ (B) $-\frac{3}{4} \tan^{-4/3} x + C$
 (C) $-3 \cot^{-1/3} x + C$ (D) $-3 \tan^{-1/3} x + C$
65. A plane passing through the points $(0, -1, 0)$ and $(0, 0, 1)$ and making an angle $\frac{\pi}{4}$ with plane $y - z + 5 = 0$, also passes through the point:
 (A) $(\sqrt{2}, 1, 4)$ (B) $(-\sqrt{2}, -1, -4)$
 (C) $(-\sqrt{2}, 1, -4)$ (D) $(\sqrt{2}, -1, 4)$
66. If the tangent to the curve, $y = x^3 + ax - b$ at the point $(1, -5)$ is perpendicular to the line, $-x + y + 4 = 0$, then which one of the following, points lies on the curve?
 (A) $(2, -2)$ (B) $(-2, 2)$
 (C) $(-2, 1)$ (D) $(2, -1)$
67. If the standard deviation of the numbers $-1, 0, 1, k$ is $\sqrt{5}$ where $k > 0$, then k is equal to:
 (A) $4\sqrt{\frac{5}{3}}$ (B) $\sqrt{6}$
 (C) $2\sqrt{6}$ (D) $2\sqrt{\frac{10}{3}}$
68. Let $f(x) = 15 - |x - 10|$; $x \in \mathbb{R}$. then the set of all values of x, at which the function, $g(x) = f(f(x))$ is not differentiable, is:
 (A) $\{5, 10, 15\}$ (B) $\{10\}$
 (C) $\{5, 10, 15, 20\}$ (D) $\{10, 15\}$
69. If the fourth term in the Binomial expansion of $\left(\frac{2}{x} + x^{\log_8 x}\right)^6$ ($x > 0$) is 20×8^7 , then a value of x is:
 (A) 8^3 (B) 8^{-2}
 (C) 8 (D) 8^2

70. If $f(x)$ is a non-zero polynomial of degree four, having local extreme points at $x = -1, 0, 1$; then the set $S = \{x \in \mathbb{R}; f(x) = f(0)\}$ contains exactly:
 (A) four irrational numbers (B) four rational numbers
 (C) two irrational and one rational number (D) two irrational and two rational numbers
71. For any two statements p and q , the negation of the expression $p \vee (\sim p \wedge q)$ is:
 (A) $p \leftrightarrow q$ (B) $\sim p \vee \sim q$
 (C) $\sim p \wedge \sim q$ (D) $p \wedge q$
72. A committee of 11 members is to be formed from 8 males and 5 females. If m is the number of ways the committee is formed with at least 6 males and n is the number of ways the committee is formed with at least 3 females, then:
 (A) $n = m - 8$ (B) $m + n = 68$
 (C) $m = n = 78$ (D) $m = n = 68$
73. If the line, $\frac{x-1}{2} = \frac{y+1}{3} = \frac{z-2}{4}$ meets the plane, $x + 2y + 3z = 15$ at a point P , then the distance of P from the origin is:
 (A) $\frac{\sqrt{5}}{2}$ (B) $2\sqrt{5}$
 (C) $\frac{9}{2}$ (D) $\frac{7}{2}$
74. The value of $\cos^2 10^\circ - \cos 10^\circ \cos 50^\circ + \cos^2 50^\circ$ is:
 (A) $\frac{3}{2}(1 + \cos 20^\circ)$ (B) $\frac{3}{4}$
 (C) $\frac{3}{2}$ (D) $\frac{3}{4} + \cos 20^\circ$
75. If $\begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 3 \\ 0 & 1 \end{bmatrix} \dots \begin{bmatrix} 1 & n-1 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 78 \\ 0 & 1 \end{bmatrix}$, then the inverse of $\begin{bmatrix} 1 & n \\ 0 & 1 \end{bmatrix}$ is:
 (A) $\begin{bmatrix} 1 & -12 \\ 0 & 1 \end{bmatrix}$ (B) $\begin{bmatrix} 1 & 0 \\ 13 & 1 \end{bmatrix}$
 (C) $\begin{bmatrix} 1 & 0 \\ 12 & 1 \end{bmatrix}$ (D) $\begin{bmatrix} 1 & -13 \\ 0 & 1 \end{bmatrix}$
76. All the points in the set $S = \left\{ \frac{\alpha + i}{\alpha - i} : \alpha \in \mathbb{R} \right\}$ ($i = \sqrt{-1}$) lie on a:
 (A) straight line whose slope is 1 (B) circle whose radius is $\sqrt{2}$
 (C) straight line whose slope is -1 (D) circle whose radius is 1
77. Let the sum of the first n terms of a non-constant A.P., a_1, a_2, a_3, \dots be $50n + \frac{n(n-7)}{2}A$, where A is a constant. If d is the common difference of this A.P., then the ordered pair (d, a_{50}) is equal to:
 (A) $(A, 50 + 46A)$ (B) $(A, 50 + 45A)$
 (C) $(50, 50 + 45A)$ (D) $(50, 50 + 46A)$

78. The value of $\int_0^{\pi/2} \frac{\sin^3 x}{\sin x + \cos x} dx$ is:
- (A) $\frac{\pi-2}{4}$ (B) $\frac{\pi-1}{2}$
 (C) $\frac{\pi-1}{4}$ (D) $\frac{\pi-2}{8}$
79. If the line $y = mx + 7\sqrt{3}$ is normal to the hyperbola $\frac{x^2}{24} - \frac{y^2}{18} = 1$, then a value of m is:
- (A) $\frac{2}{\sqrt{5}}$ (B) $\frac{\sqrt{5}}{2}$
 (C) $\frac{\sqrt{15}}{2}$ (D) $\frac{3}{\sqrt{5}}$
80. The solution of the differential equation $x \frac{dy}{dx} + 2y = x^2$ ($x \neq 0$) with $y(1) = 1$, is:
- (A) $y = \frac{x^3}{5} + \frac{1}{5x^2}$ (B) $y = \frac{x^2}{4} + \frac{3}{4x^2}$
 (C) $y = \frac{4}{5}x^3 + \frac{1}{5x^2}$ (D) $y = \frac{3}{4}x^2 + \frac{1}{4x^2}$
81. If one end of a focal chord of the parabola, $y^2 = 16x$ is at $(1, 4)$, then the length of this focal chord is:
- (A) 25 (B) 24
 (C) 22 (D) 20
82. Let S be the set of all values of x for which the tangent to the curve $y = f(x) = x^3 - x^2 - 2x$ at (x, y) is parallel to the line segment joining the points $(1, f(1))$ and $(-1, f(-1))$, then S is equal to:
- (A) $\left\{\frac{1}{3}, -1\right\}$ (B) $\left\{-\frac{1}{3}, -1\right\}$
 (C) $\left\{\frac{1}{3}, 1\right\}$ (D) $\left\{-\frac{1}{3}, 1\right\}$
83. Slope of a line passing through $P(2, 3)$ and intersecting the line, $x + y = 7$ at a distance of 4 units from P , is:
- (A) $\frac{\sqrt{5}-1}{\sqrt{5}+1}$ (B) $\frac{1-\sqrt{5}}{1+\sqrt{5}}$
 (C) $\frac{\sqrt{7}-1}{\sqrt{7}+1}$ (D) $\frac{1-\sqrt{7}}{1+\sqrt{7}}$
84. Let $\sum_{k=1}^{10} f(a+k) = 16(2^{10} - 1)$, where the function f satisfies $f(x+y) = f(x)f(y)$ for all natural numbers x, y and $f(1) = 2$. Then the natural number 'a' is:
- (A) 4 (B) 16
 (C) 2 (D) 3

85. Let $S = \{\theta \in [-2\pi, 2\pi] : 2 \cos^2\theta + 3 \sin\theta = 0\}$. Then the sum of the elements of S is:
 (A) $\frac{13\pi}{6}$ (B) 2π
 (C) π (D) $\frac{5\pi}{3}$
86. If a tangent to the circle $x^2 + y^2 = 1$ intersects the coordinate axes at distinct points P and Q , then the locus of the mid-point of PQ is:
 (A) $x^2 + y^2 - 16x^2y^2 = 0$ (B) $x^2 + y^2 - 2x^2y^2 = 0$
 (C) $x^2 + y^2 - 4x^2y^2 = 0$ (D) $x^2 + y^2 - 2xy = 0$
87. Four persons can hit a target correctly with probabilities $\frac{1}{2}, \frac{1}{3}, \frac{1}{4}$ and $\frac{1}{8}$ respectively. If all hit at the target independently, then the probability that the target would be hit, is:
 (A) $\frac{25}{32}$ (B) $\frac{25}{192}$
 (C) $\frac{7}{32}$ (D) $\frac{1}{192}$
88. The area (in sq. units) of the region $A = \{(x, y) : x^2 \leq y \leq x + 2\}$ is:
 (A) $\frac{31}{6}$ (B) $\frac{13}{6}$
 (C) $\frac{9}{2}$ (D) $\frac{10}{3}$
89. Let α and β be the roots of the equation $x^2 + x + 1 = 0$. Then for $y \neq 0$ in \mathbb{R} ,

$$\begin{vmatrix} y+1 & \alpha & \beta \\ \alpha & y+\beta & 1 \\ \beta & 1 & y+\alpha \end{vmatrix}$$
 is equal to:
 (A) $y(y^2 - 3)$ (B) $y^3 - 1$
 (C) y^3 (D) $y(y^2 - 1)$
90. If the function f defined on $\left(\frac{\pi}{6}, \frac{\pi}{3}\right)$ by $f(x) = \begin{cases} \frac{\sqrt{2} \cos x - 1}{\cot x - 1}, & x \neq \frac{\pi}{4} \\ k, & x = \frac{\pi}{4} \end{cases}$ is continuous, then k is equal to:
 (A) 1 (B) 2
 (C) $\frac{1}{2}$ (D) $\frac{1}{\sqrt{2}}$

JEE (Mains) – 2019

ANSWERS

PART A – PHYSICS

1.	Bonus	2.	A	3.	D	4.	D
5.	B	6.	D	7.	A	8.	A
9.	A	10.	B	11.	B	12.	B
13.	B	14.	D	15.	A	16.	B
17.	D	18.	C	19.	B	20.	D
21.	C	22.	B	23.	C	24.	A
25.	B	26.	A	27.	A	28.	B
29.	D	30.	B				

PART B – CHEMISTRY

31.	B	32.	A	33.	A	34.	C
35.	B	36.	A	37.	A	38.	A
39.	A	40.	D	41.	C	42.	B
43.	C	44.	C	45.	D	46.	D
47.	B	48.	B	49.	B	50.	B
51.	B	52.	C	53.	C	54.	C
55.	A	56.	D	57.	C	58.	B
59.	A	60.	D				

PART C – MATHEMATICS

61.	A	62.	B or Bonus	63.	A	64.	D
65.	A	66.	A	67.	C	68.	A
69.	D	70.	C	71.	C	72.	C
73.	C	74.	B	75.	D	76.	D
77.	A	78.	C	79.	A	80.	B
81.	A	82.	D	83.	D	84.	D
85.	B	86.	C	87.	A	88.	C
89.	C	90.	C				

HINTS AND SOLUTIONS

PART A – PHYSICS

1. $\rho = \frac{m}{v}$

Maximum % error in ρ will be given by

$$\frac{\Delta\rho}{\rho} \times 100\% = \left(\frac{\Delta m}{m}\right) \times 100\% + 3\left(\frac{\Delta L}{L}\right) \times 100\% \dots (i)$$

This is not applicable as error is big.

$$\rho_{\min} = \frac{m_{\min}}{v_{\max}} = \frac{9.9}{(0.11)^3} = 7438 \text{ kg/m}^3$$

$$\& \rho_{\max} = \frac{m_{\max}}{v_{\min}} = \frac{10.1}{(0.09)^3} = 13854.6 \text{ kg/m}^3$$

$$\Delta\rho = 6416.6 \text{ kg/m}^3$$

No option is matching. Therefore this question should be awarded bonus.

2. $\phi = NBA = LI$

$$N \mu_0 n I \pi R^2 = LI$$

$$N \mu_0 \frac{N}{\ell} I \pi R^2 = LI$$

N and R constant

$$\text{Self inductance (L)} \propto \frac{1}{\ell} \propto \frac{1}{\text{length}}$$

3. Path difference at central maxima $\Delta x = (\mu - 1)t$, whole pattern will shift by same amount which will be given by

$$(\mu - 1)t \frac{D}{d} = n \frac{\lambda D}{d}, \text{ according to eh question } t = \frac{n\lambda}{(\mu - 1)}$$

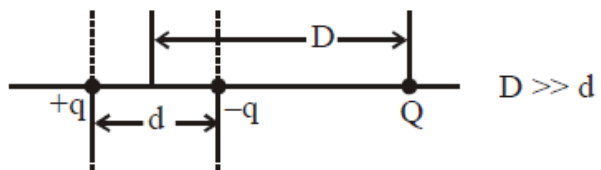
No option is matching, therefore question should be award bonus.

\therefore Correct option should be (Bonus)

4. $U_{\text{total}} = U_{\text{self of dipole}} + U_{\text{interaction}}$

$$= -\frac{kq^2}{d} - \left(\frac{kQ}{D^2}\right)qd$$

$$= -k \left[\frac{q^2}{d} + \frac{qQd}{D^2} \right]$$



5. $G = 50 \Omega$

$$S = 5000 \Omega$$

$$I_g = 4 \times 10^{-3}$$

$$V = I_g (G + S)$$

$$V = 4 \times 10^{-3} (50 + 5000)$$

$$= 4 \times 10^{-3} (5050) = 20.2 \text{ volt}$$

6. Height of liquid rise in capillary tube $h = \frac{2T \cos \theta_c}{\rho g}$

$$\Rightarrow h \propto \frac{1}{r}$$

When radius becomes double height become half

$$\therefore h' = \frac{h}{2}$$

Now, $M = \pi r^2 h \times \rho$ and $M' = \pi(2r)^2 (h/2) \times \rho = 2M$.

7. Input current = 15×10^{-6}
 Output current = 3×10^{-3}
 Resistance out put = 1000
 $V_{\text{input}} = 10 \times 10^{-3}$
 Now $V_{\text{input}} = r_{\text{input}} \times i_{\text{input}}$
 $10 \times 10^{-3} = r_{\text{input}} \times 15 \times 10^{-6}$
 $r_{\text{input}} = \frac{2000}{3} = 0.67 \text{ K}\Omega$.

$$\text{Voltage gain} = \frac{V_{\text{output}}}{V_{\text{input}}} = \frac{1000 \times 3 \times 10^{-3}}{10 \times 10^{-3}} = 300$$

8. According to equipartition energy theorem

$$\frac{1}{2} m(v_{\text{rms}}^2) = 3 \times \frac{1}{2} K_b T$$

$$T = \frac{m v_{\text{rms}}^2}{3k}$$

9. $\omega = 6 \times 10^{14} \times 2\pi$
 $f = 6 \times 10^{14}$
 $C = f \lambda$
 $\lambda = \frac{C}{f} = \frac{3 \times 10^8}{6 \times 10^{14}} = 5000 \text{ \AA}$

$$\text{Energy of photon} \Rightarrow \frac{12375}{5000} = 2.475 \text{ eV}$$

From Einstein's equation

$$KE_{\text{max}} = E - \phi$$

$$eV_s = E - \phi$$

$$eV_s = 2.475 - 2$$

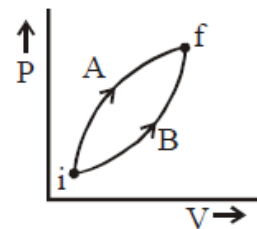
$$eV_o = 0.475 \text{ eV}$$

$$V_o = 0.48 \text{ V}$$

10. Initial and final states for both the processes are same,

$$\therefore \Delta U_A = \Delta U_B$$

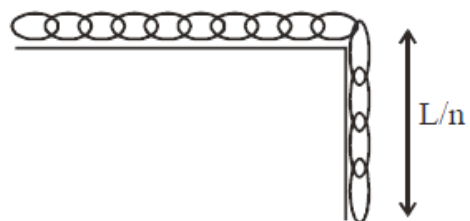
Work done during process A is greater than in process B. Because area is more
 By First law of thermodynamics
 $\Delta Q = \Delta U + W$
 $\Rightarrow \Delta Q_A > \Delta Q_B$



11. Mass of the hanging part = $\frac{M}{n}$

$$h_{\text{COM}} = \frac{L}{2n}$$

$$\text{Work done } W = mgh_{\text{COM}} = \left(\frac{M}{n}\right)g\left(\frac{L}{2n}\right) = \frac{MgL}{2n^2}$$



12. $\frac{1}{2} \left(m + \frac{1}{R^2} \right) v^2 = mgh$

If radius of gyration is k, then

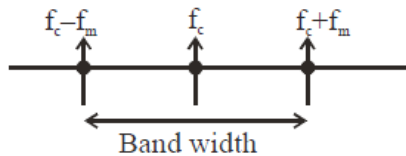
$$h = \frac{\left(1 + \frac{k^2}{R^2}\right)v^2}{2g}; \quad \frac{k_{\text{ring}}}{R_{\text{ring}}} = 1, \quad \frac{k_{\text{solid cylinder}}}{R_{\text{solid cylinder}}} = \frac{1}{\sqrt{2}}$$

$$\frac{k_{\text{solid sphere}}}{R_{\text{solid sphere}}} = \sqrt{\frac{2}{5}}$$

$$H_1 : h_2 : h_3 :: (1 + 1) : \left(1 + \frac{1}{2}\right) : \left(1 + \frac{2}{5}\right) :: 20 : 15 : 14$$

Therefore most appropriate option is (B)
Although which is not in correct sequence.

13.



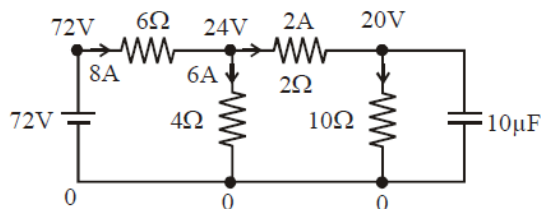
14.

$$m = \frac{f}{f - u}$$

$$5 = \frac{-40}{-40 - u} ; \quad u = -32 \text{ cm}$$

15.

Different potential is shown at different points.



$$q = eV$$

$$q = 10\mu\text{F} \times 20 = 200 \mu\text{C}$$

16.

$$|\vec{\tau}| = |\vec{M} \times \vec{B}|$$

$$\tau = NI \times A \times B \times \sin 45^\circ$$

$$\tau = 0.27 \text{ Nm}$$

17.

$$\text{Kinetic energy } KE = \frac{1}{2}I\omega^2 = k\theta^2$$

$$\Rightarrow \omega^2 = \frac{2k\theta^2}{I} \Rightarrow \omega = \sqrt{\frac{2k}{I}} \theta \quad \dots(A)$$

Differentiate (A) wrt time \rightarrow

$$\frac{d\omega}{dt} = \alpha = \sqrt{\frac{2k}{I}} \left(\frac{d\theta}{dt}\right)$$

$$\Rightarrow \alpha = \sqrt{\frac{2k}{I}} \cdot \sqrt{\frac{2k}{I}} \theta \quad \{\text{by (1)}\}$$

$$\Rightarrow \alpha = \frac{2k}{I} \theta$$

18.

$$\text{For a simple pendulum } T = 2\pi \sqrt{\frac{L}{g_{\text{eff}}}}$$

Situation 1: when pendulum is in air $\rightarrow g_{\text{eff}} = g$

Situation 2: when pendulum is in liquid

$$\rightarrow g_{\text{eff}} = g \left(1 - \frac{\rho_{\text{liquid}}}{\rho_{\text{body}}} \right) = g \left(1 - \frac{1}{16} \right) = \frac{15g}{16}$$

$$\text{So, } \frac{T'}{T} = \frac{2\pi \sqrt{\frac{L}{15g/16}}}{2\pi \sqrt{\frac{L}{g}}}$$

$$\Rightarrow T' = \frac{4T}{\sqrt{15}}$$

19. $V_{\text{rms}} = \sqrt{\frac{3RT}{M_w}}$

$$\Rightarrow v_{\text{rms}} \propto \sqrt{T}$$

$$\text{Now, } \frac{v}{200} = \sqrt{\frac{500}{400}} \Rightarrow \frac{v}{200} = \frac{\sqrt{5}}{2}$$

$$\Rightarrow v = 100\sqrt{5} \text{ m/s}$$

20. Maximum electric field $E = (B) (C)$

$$\vec{E}_0 = (3 \times 10^{-5})c (-\hat{j})$$

$$\vec{E}_1 = (2 \times 10^{-6})c (-\hat{i})$$

Maximum force

$$\vec{F}_{\text{net}} = 10^{-4} \times 3 \times 10^8 \sqrt{(3 \times 10^{-5})^2 + (2 \times 10^{-6})^2} = 0.9 \text{ N}$$

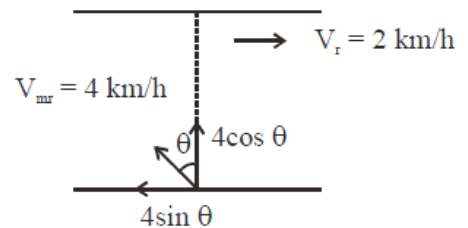
$$F_{\text{rms}} = \frac{F_0}{\sqrt{2}} = 0.6 \text{ N (approx)}$$

21. For swimmer to cross the river straight

$$\Rightarrow 4 \sin \theta = 2$$

$$\Rightarrow \sin \theta = \frac{1}{2} \Rightarrow \theta = 30^\circ$$

So, angle with direction of river flow = $90^\circ + \theta = 120^\circ$.



22. F_3 & F_4 cancel each other.

Force on PQ will be $F_1 = 2B_1 a$

$$= I_2 \frac{\mu_0 I_1}{2\pi a} a$$

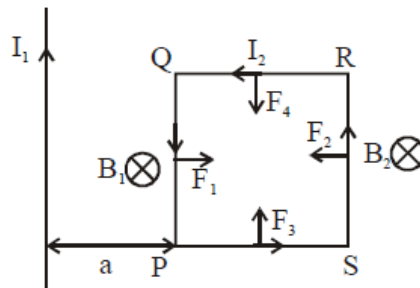
$$= \frac{\mu_0 I_1 I_2}{2\pi a} a = \frac{\mu_0 I_1 I_2}{2\pi}$$

Force on RS will be $F_2 = I_2 B_2 a$

$$= I_2 \frac{\mu_0 I_1}{2\pi 2a} a$$

$$= \frac{\mu_0 I_1 I_2}{4\pi}$$

$$\text{Net force} = F_1 - F_2 = \frac{\mu_0 I_1 I_2}{4\pi} \text{ repulsion}$$



23. $\frac{1}{660} = R \left(\frac{1}{2^2} - \frac{1}{3^2} \right) = \frac{5R}{36} \quad \dots(1)$

$\frac{1}{\lambda} = R \left(\frac{1}{2^2} - \frac{1}{4^2} \right) = \frac{3R}{16} \quad \dots(B)$

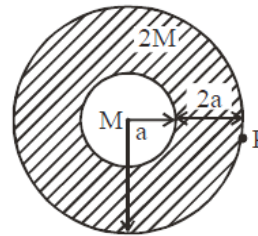
Divide equation (1) with (B)

$\frac{\lambda}{660} = \frac{5 \times 16}{36 \times 3}$

$\lambda = \frac{4400}{9} = 488.88 = 488.9 \text{ nm}$

24. We use Gauss's Law for gravitation
 $g \cdot 4\pi r^2 = (\text{Mass enclosed}) 4\pi G$

$g = \frac{3M4\pi G}{4\pi(3a)^2} = \frac{GM}{3a^2}$

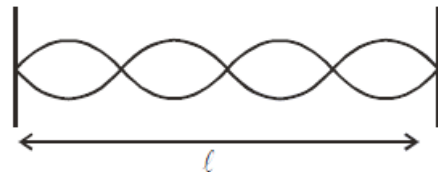


25. 4th harmonic

$4 \frac{\lambda}{2} = l ; 2\lambda = l$

From equation $\frac{2\pi}{\lambda} = 0.157$

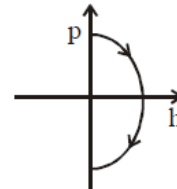
$\lambda = 40 ; l = 2\lambda = 80 \text{ m}$



26. Momentum $p = mv \quad \dots(1)$

and for motion under gravity $h = \frac{u^2 - v^2}{2g} \quad \dots(2)$

$h = \frac{u^2 - p^2 / m}{2g}$



27. Work done = ΔU

$= U_f - U_i$

$= \frac{q^2}{2C_f} - \frac{q^2}{2C_i}$

$= \frac{(5 \times 10^{-6})^2}{2} \left(\frac{1}{2 \times 10^{-6}} - \frac{1}{5 \times 10^{-6}} \right)$

$= \frac{15}{4} \times 10^{-6}$

$= 3.75 \times 10^{-6} \text{ J}$

28. By conservation of linear momentum:

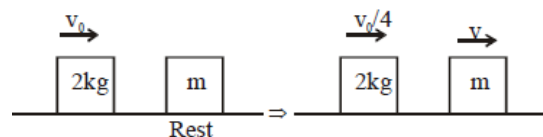
$2v_0 = 2 \left(\frac{v_0}{4} \right) + mv \Rightarrow 2v_0 = \frac{v_0}{2} + mv$

$\Rightarrow \frac{3v_0}{2} = mv \quad \dots(1)$

Since collision is elastic \rightarrow

$V_{\text{separation}} = V_{\text{approach}}$

$\Rightarrow v - \frac{v_0}{4} = v_0 \Rightarrow m = \frac{6}{5} = 1.2 \text{ kg}$



29. Speed of wave from wave equation

$$v = - \frac{(\text{coefficient of } t)}{(\text{coefficient of } x)}$$

$$v = - \frac{1000}{(-3)} = \frac{1000}{3}$$

Since speed of wave $\propto \sqrt{T}$

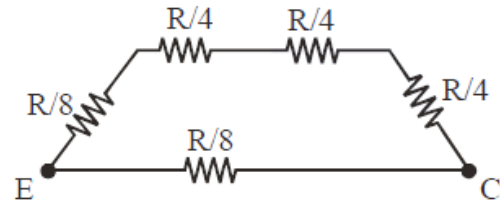
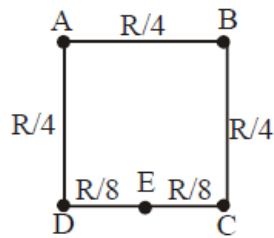
$$So = \frac{1000}{3} = \sqrt{\frac{273}{T}}$$

$$336$$

$$\Rightarrow T = 277.41 \text{ K}$$

$$T = 4.41^\circ\text{C}$$

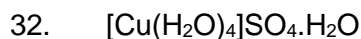
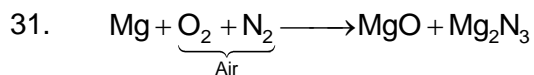
30.



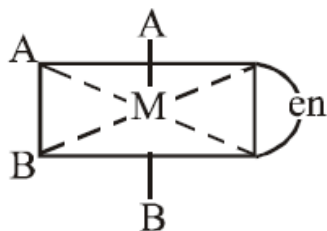
$$\frac{1}{R_{eq}} = \frac{8}{7R} + \frac{8}{R}$$

$$\frac{1}{R_{eq}} = \frac{8+56}{7R} ; R_{eq} = \frac{7R}{64}$$

PART B – CHEMISTRY



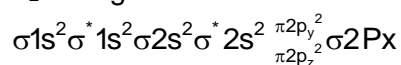
33.



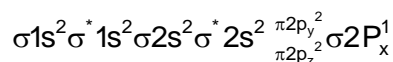
No plane of symmetry

34. $T_C = \frac{8a}{27Rb}$

35. C_2 configuration



C_2^- configuration



36. $P_M^0 = 450$

$P_N^0 = 700$

$P_M = x_M 450$

$P_N = x_N 700$

$Y_M P_T = P_M$

$Y_N P_T = P_N$

$\frac{Y_M P_T}{Y_N P_T} = \frac{x_M 450}{x_N 700}$

$\frac{Y_M}{Y_N} = \frac{x_M}{x_N} (0:64)$

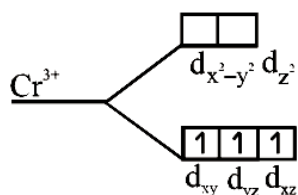
$\frac{Y_M}{Y_N} = \frac{x_M}{x_N} (0:64)$

$\frac{x_M}{x_N} > \frac{Y_M}{Y_N}$

37. $\Delta U = q + w$

$\Delta G = \Delta H - T\Delta S$

38. Degenerate orbitals of $[\text{Cr}(\text{H}_2\text{O})_6]^{3+}$



39. Fact based (Given in NCERT)

40. For first order reaction

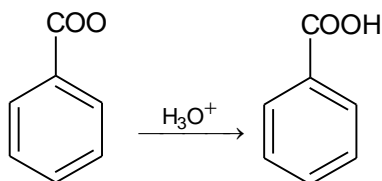
$$\ln[R]_t = -Kt + \ln[R]_0$$

For zero order reaction

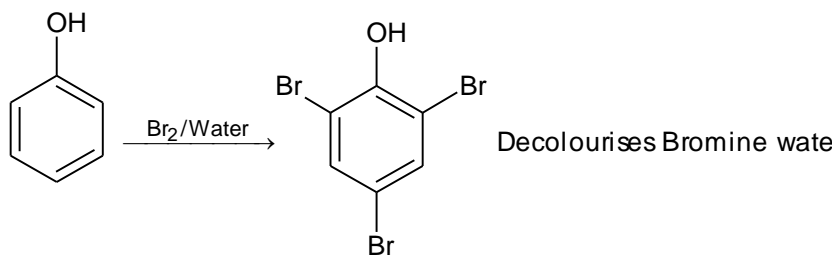
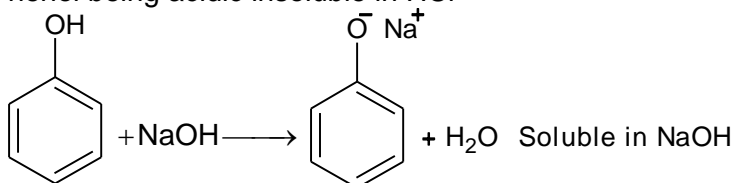
$$[R]_t = -Kt + [R]_0$$

Where 'R' is reactant.

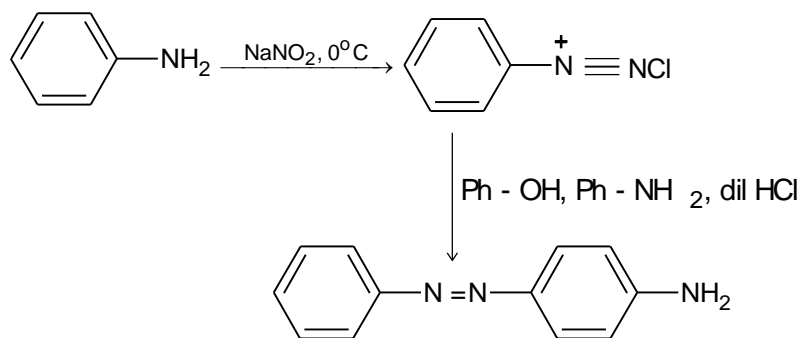
41.



42. Phenol being acidic insoluble in HCl



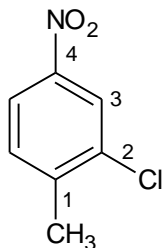
43.



44. Fact based (Given in NCERT)

45. Cryolite is $\text{Na}_3[\text{AlF}_6]$

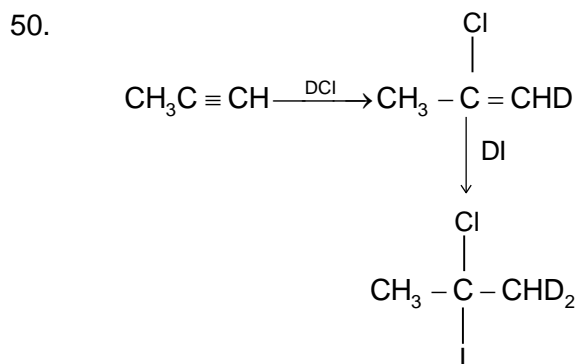
46.



47. LiAlH_4 does not reduce double bond it reduces ester in alcohol.

48. After losing one electron 'K' acquires noble gas configuration.

49. 56 g of N_2 means 2 mole
 2 mole of N_2 requires 6 mole of H_2 for complete reaction but available H_2 is 10 g i.e. 5 mole
 hence H_2 is limiting reagent.



51.

$$\pi_{xy} = 4\pi_{BaCl_2}$$

$$\pi_{xy} = iCRT$$

$$\pi_{xy} = 2CRT$$

$$\pi_{BaCl_2} = 3 \times 0.01 RT$$

$$RT = 12 \times 0.01 RT$$

$$\frac{12 \times 0.01}{2} = 0.06$$

52.

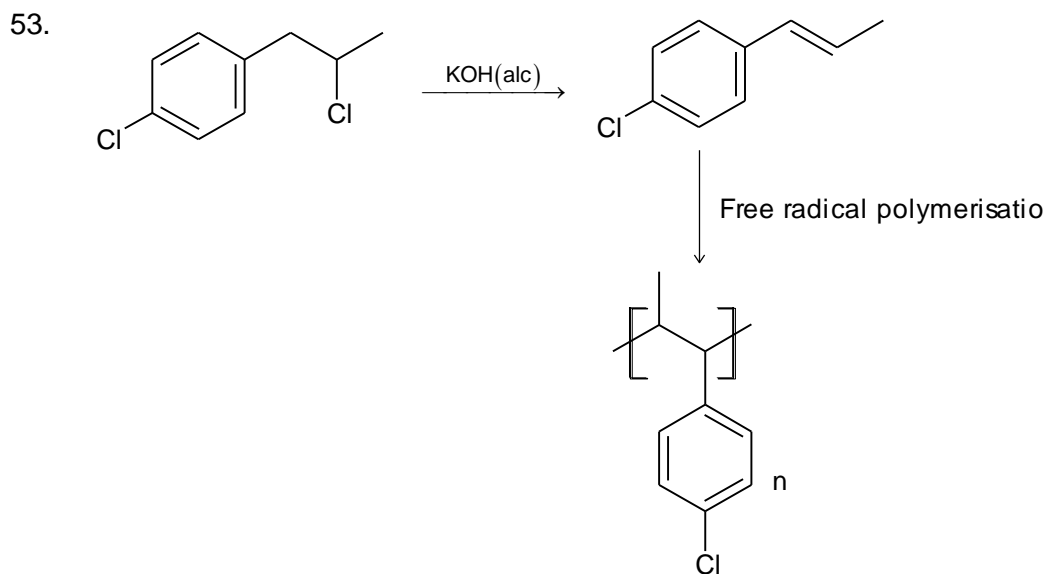
$$\Delta \bar{V}_{Lyman} = \frac{R_H}{4}$$

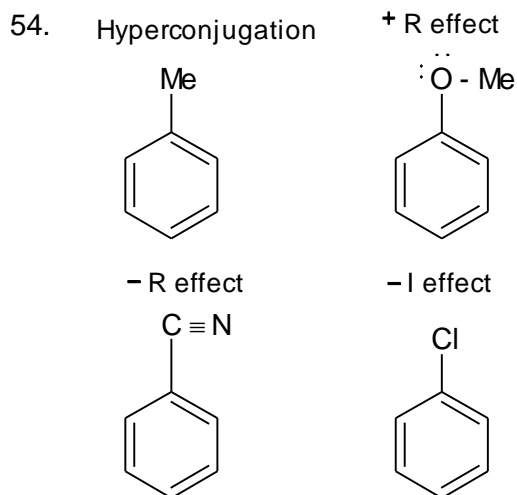
$$\Delta \bar{V}_{Balmer} = \frac{R_H}{9}$$

$$\Rightarrow \frac{\Delta \bar{V}_{Lyman}}{\Delta \bar{V}_{Balmer}} = \frac{9}{4}$$

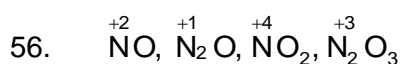
Formula

$$\bar{V} = R_H \left[\frac{1}{n_1^2} - \frac{1}{n_2^2} \right]$$

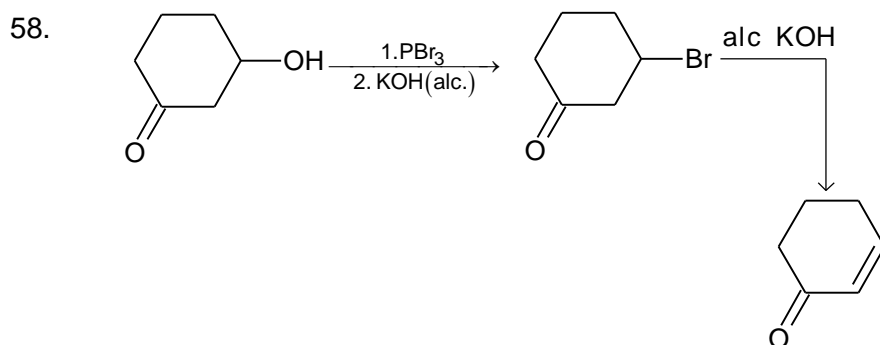




55. Fact based (Given in NCERT)



57. $\Delta G = -2 \times 96000 \times 2$
 $\Delta G = -nFE^\circ$
 $\Delta G = -2 \times 96000 \times 2 \text{ J}$
 $\Delta G = -384 \text{ kJ mol}^{-1}$



59. C_1 of α -glucose and C_2 of β -fructose

60. V_2O_5 is used in contact process for H_2SO_4
 $\text{TiCl}_4/\text{Al}(\text{Me})_3$ Ziegler natal catalyst used fin polymerization
 PdCl_2 is used in ethanol formation
 Iron oxide is used in Haber process for NH_3

PART C – MATHEMATICS

61. $y = \frac{x^2}{1-x^2}$

Range of $y : \mathbb{R} - [-1, 0)$ for surjective function, A must be same as above range.

62. In given question $p, q \in \mathbb{R}$. If we take other root as any real number α , then quadratic equation will be $x^2 - (\alpha + 2 - \sqrt{3})x + \alpha(2 - \sqrt{3}) = 0$

Now, we can have none or any of the options can be correct depending upon ' α '.

Instead of $p, q \in \mathbb{R}$ it should be $p, q \in \mathbb{Q}$ then other root will be $2 + \sqrt{3}$

$$\Rightarrow p = -(2 + \sqrt{3} - 2 - \sqrt{3}) - 4 \text{ and } q = (2 + \sqrt{3})(2 - \sqrt{3}) = 1$$

$$\Rightarrow p^2 - 4q - 12 = (-4)^2 - 4 - 12$$

$$= 16 - 16 = 0$$

Option (B) is correct.

63. $\vec{\alpha} = 3\hat{i} + \hat{j}$

$$\vec{\beta} = 2\hat{i} - \hat{j} + 3\hat{k}$$

$$\vec{\beta} = \vec{\beta}_1 - \vec{\beta}_2$$

$$\vec{\beta}_1 = \lambda(3\hat{i} + \hat{j}), \vec{\beta}_2 = \lambda(3\hat{i} + \hat{j}) - 2\hat{i} + \hat{j} - 3\hat{k}$$

$$\vec{\beta}_2 \cdot \vec{\alpha} = 0$$

$$(3\lambda - 2) \cdot 3 + (\lambda + 1) = 0$$

$$9\lambda - 6 + \lambda + 1 = 0$$

$$\lambda = \frac{1}{2}$$

$$\Rightarrow \vec{\beta}_1 = \frac{3}{2}\hat{i} + \frac{1}{2}\hat{j}$$

$$\Rightarrow \vec{\beta}_2 = -\frac{1}{2}\hat{i} + \frac{3}{2}\hat{j} - 3\hat{k}$$

$$\text{Now, } \vec{\beta}_1 \times \vec{\beta}_2 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{3}{2} & \frac{1}{2} & 0 \\ -\frac{1}{2} & \frac{3}{2} & -3 \end{vmatrix}$$

$$= \hat{i} \left(-\frac{3}{2} - 0 \right) - \hat{j} \left(-\frac{9}{2} - 0 \right) + \hat{k} \left(\frac{9}{4} + \frac{1}{4} \right)$$

$$= \frac{3}{2}\hat{i} + \frac{9}{2}\hat{j} + \frac{5}{2}\hat{k}$$

$$= \frac{1}{2}(-3\hat{i} + 9\hat{j} + 5\hat{k})$$

64. $I = \int \frac{dx}{(\sin x)^{4/3} \cdot (\cos x)^{2/3}}$

$$I = \int \frac{dx}{\left(\frac{\sin x}{\cos x} \right)^{4/3} \cdot \cos^2 x}$$

$$\Rightarrow I = \int \frac{\sec^2 x}{(\tan x)^{4/3}} dx$$

put $\tan x = t \Rightarrow \sec^2 x dx = dt$

$$\therefore I = \int \frac{dt}{t^{4/3}} \Rightarrow I = \frac{-3}{t^{1/3}} + c$$

$$\Rightarrow I = \frac{-3}{(\tan x)^{1/3}} + c$$

65. Let $ax + by + cz = 1$ be the equation of the plane

$$\Rightarrow 0 - b + 0 = 1$$

$$\Rightarrow b = -1$$

$$0 + 0 + c = 1$$

$$\Rightarrow c = 1$$

$$\cos \theta = \frac{\left| \begin{matrix} \vec{a} \cdot \vec{b} \\ |\vec{a}| |\vec{b}| \end{matrix} \right|}{\left| \begin{matrix} \vec{a} \\ |\vec{a}| \end{matrix} \right| \left| \begin{matrix} \vec{b} \\ |\vec{b}| \end{matrix} \right|}$$

$$\frac{1}{\sqrt{2}} = \frac{|0 - 1 - 1|}{\sqrt{(a^2 + 1 + 1)} \sqrt{0 + 1 + 1}}$$

$$\Rightarrow a^2 + 2 = 4$$

$$\Rightarrow a = \pm \sqrt{2}$$

$$\Rightarrow \pm \sqrt{2}x - y + z = 1$$

Now for - sign

$$-\sqrt{2}, \sqrt{2} - 1 + 4 = 1$$

Hence option (A)

66. $y = x^3 + ax - b$

(1, -5) lies on the curve

$$\Rightarrow -5 = 1 + a - b \Rightarrow a - b = -6 \quad \dots\dots(i)$$

Also, $y' = 3x^2 + a$

$$y'(1, -5) = 3 + a \quad (\text{slope of tangent})$$

\therefore this tangent is \perp to $-x + y + 4 = 0$

$$\Rightarrow (3 + a)(1) = -1$$

$$\Rightarrow a = -4 \quad \dots\dots(ii)$$

By (i) and (ii) : $a = -4, b = 2$

$$\therefore y = x^3 - 4x - 2$$

(2, -2) lies on this curve.

67. $S.D. = \sqrt{\frac{\sum (x - \bar{x})^2}{n}}$

$$\bar{x} = \frac{\sum x}{4} = \frac{-1 + 0 + 1 + k}{4} = \frac{k}{4}$$

$$\text{Now } \sqrt{5} = \sqrt{\frac{\left(-1 - \frac{k}{4}\right)^2 + \left(0 - \frac{k}{4}\right)^2 + \left(1 - \frac{k}{4}\right)^2 + \left(k - \frac{k}{4}\right)^2}{4}}$$

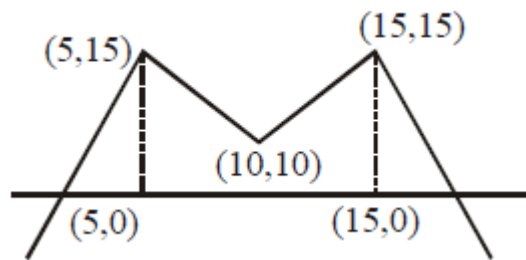
$$\Rightarrow 5 \times 4 = 2 \left(1 + \frac{k}{16}\right)^2 + \frac{5k^2}{8}$$

$$\Rightarrow 18 = \frac{3k^2}{4}$$

$$\Rightarrow k^2 = 24$$

$$\Rightarrow k = 2\sqrt{6}$$

68. $f(x) = 15 - |x - 10|, x \in \mathbb{R}$
 $f(f(x)) = 15 - |f(x) - 10|$
 $= 15 - |15 - |x - 10| - 10|$
 $= 15 - |5 - |x - 10||$
 $x = 5, 10, 15$ are point of non differentiability



69. $T_4 = T_{3+1} = \binom{6}{3} \left(\frac{2}{x}\right)^3 \cdot (x^{\log_8 x})^3$
 $20 \times 8^7 = \frac{160}{x^3} \cdot x^{3 \log_8 x}$
 $8^6 = x^{\log_2 x - 3}$
 $2^{18} = x^{\log_2 x - 3}$
 $\Rightarrow 18 = (\log_2 x - 3)(\log_2 x)$
 Let $\log_2 x = t$
 $\Rightarrow t^2 - 3t - 18 = 0$
 $\Rightarrow (t - 6)(t + 3) = 0$
 $\Rightarrow t = 6, -3$
 $\log_2 x = 6 \Rightarrow x = 2^6 = 8^2$
 $\log_2 x = -3 \Rightarrow x = 2^{-3} = 8^{-1}$

70. $f'(x) = \lambda(x+1)(x-0)(x-1) = \lambda(x^3 - x)$
 $\Rightarrow f(x) = \lambda \left(\frac{x^4}{4} - \frac{x^2}{2} \right) + \mu$
 Now $f(x) = f(0)$
 $\Rightarrow \lambda \left(\frac{x^4}{4} - \frac{x^2}{2} \right) + \mu = \mu$
 $\Rightarrow x = 0, 0, \pm \sqrt{2}$
 Two irrational and one rational number

71. $\sim(p \vee (\sim p \wedge q))$
 $= \sim p \wedge \sim(\sim p \wedge q)$
 $= \sim p \wedge (p \vee \sim q)$
 $= (\sim p \wedge p) \vee (\sim p \wedge \sim q)$
 $= c \vee (\sim p \wedge \sim q)$
 $= (\sim p \wedge \sim q)$

72. Since there are 8 males and 5 females. Out of these 13, if we select 11 persons, then there will be at least 6 males and at least 3 females in the selection.
 $m = n = \binom{13}{11} = \binom{13}{2} = \frac{13 \times 12}{2} = 78$

73. Any point on the given line can be

$$(1+2\lambda, -1+3\lambda, 2+4\lambda); \lambda \in \mathbb{R}$$

Put in plane

$$1+2\lambda + (-2+6\lambda) + (6+12\lambda) = 15$$

$$20\lambda + 5 = 15$$

$$20\lambda = 10$$

$$\lambda = \frac{1}{2}$$

$$\therefore \text{Point} \left(2, \frac{1}{2}, 4 \right)$$

$$\text{Distance from origin} = \sqrt{4 + \frac{1}{4} + 16} = \frac{\sqrt{16+1+64}}{2} = \frac{\sqrt{81}}{2}$$

$$= \frac{9}{2}$$

74. $\frac{1}{2}(2\cos^2 10^\circ - 2\cos 10^\circ \cos 50^\circ + 2\cos^2 50^\circ)$

$$\Rightarrow \frac{1}{2}(1 + \cos 20^\circ - (\cos 60^\circ + \cos 40^\circ) + 1 + \cos 100^\circ)$$

$$\Rightarrow \frac{1}{2}\left(\frac{3}{2} + \cos 20^\circ + 2\sin 70^\circ \sin(-30^\circ)\right)$$

$$\Rightarrow \frac{1}{2}\left(\frac{3}{2} + \cos 20^\circ - \sin 70^\circ\right)$$

$$\Rightarrow \frac{3}{4}$$

75. $\begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 3 \\ 0 & 1 \end{bmatrix} \dots \begin{bmatrix} 1 & n-1 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 78 \\ 0 & 1 \end{bmatrix}$

$$\Rightarrow \begin{bmatrix} 1 & 1+2+3+\dots+n-1 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 78 \\ 0 & 1 \end{bmatrix}$$

$$\Rightarrow \frac{n(n-1)}{2} = 78 \Rightarrow n = 13, -12 \text{ (reject)}$$

$$\therefore \text{we have to find inverse of } \begin{bmatrix} 1 & 13 \\ 0 & 1 \end{bmatrix}$$

$$\therefore \begin{bmatrix} 1 & -13 \\ 0 & 1 \end{bmatrix}$$

76. Let $\frac{\alpha+i}{\alpha-1} = z$

$$\Rightarrow \left| \frac{\alpha+i}{\alpha-1} \right| = |z|$$

$$\Rightarrow 1 = |z|$$

\Rightarrow circle of radius 1

77. $S_n = 50n + \frac{n(n-7)}{2} A$

$$T_n = S_n - S_{n-1}$$

$$\begin{aligned}
 &= 50n + \frac{n(n-7)}{2}A - 50(n-1) - \frac{(n-1)(n-8)}{2}A \\
 &= 50 + \frac{A}{2}[n^2 - 7n - n^2 + 9n - 8] \\
 &= 50 + A(n-4) \\
 d &= T_n - T_{n-1} \\
 &= 50 + A(n-4) - 50 - A(n-5) \\
 &= A \\
 T_{50} &= 50 + 46A \\
 (d, A_{50}) &= (A, 50 + 46A)
 \end{aligned}$$

78.
$$I = \int_0^{\pi/2} \frac{\sin^3 x}{\sin x + \cos x} dx$$

$$\Rightarrow I = \int_0^{\pi/4} \frac{\sin^3 x + \cos^3 x}{\sin x + \cos x} dx$$

$$= \int_0^{\pi/4} (1 - \sin x \cos x) dx$$

$$= \left(x - \frac{\sin^2 x}{2} \right)_0^{\pi/4}$$

$$= \frac{\pi}{4} - \frac{1}{4}$$

$$= \frac{\pi - 1}{4}$$

79.
$$\frac{x^2}{24} - \frac{y^2}{18} = 1 \Rightarrow a = \sqrt{24} : b = \sqrt{18}$$

Parametric normal:

$$\sqrt{24} \cos \theta \cdot x + \sqrt{18} \cdot y \cot \theta = 42$$

At $x = 0$; $y = \frac{42}{\sqrt{18}} \tan \theta = 7\sqrt{3}$ (from given equation)

$$\Rightarrow \tan \theta = \sqrt{\frac{3}{2}} \Rightarrow \sin \theta = \pm \sqrt{\frac{3}{5}}$$

slope of parametric normal $= \frac{-\sqrt{24} \cos \theta}{\sqrt{18} \cot \theta} = m$

$$\Rightarrow m = -\sqrt{\frac{4}{3}} \sin \theta = -\frac{2}{\sqrt{5}} \text{ or } \frac{2}{\sqrt{5}}$$

80.
$$x \frac{dy}{dx} + 2y = x^2 : y(1) = 1$$

$$\frac{dy}{dx} + \left(\frac{2}{x}\right)y = x \text{ (LDE in } y)$$

$$IF = e^{\int \frac{2}{x} dx} = e^{2 \ln x} = x^2$$

$$y \cdot (x^2) = \int x \cdot x^2 dx = \frac{x^4}{4} + C$$

$$y(1) = 1$$

$$1 = \frac{1}{4} + C \Rightarrow C = 1 - \frac{1}{4} = \frac{3}{4}$$

$$yx^2 = \frac{x^4}{4} + \frac{3}{4}$$

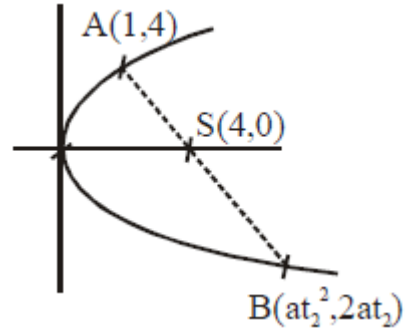
$$y = \frac{x^2}{4} + \frac{3}{4x^2}$$

81. $y^2 = 4ax = 16x \Rightarrow a = 4$

$$A(1,4) \Rightarrow 2 \cdot 4 \cdot t_1 = 4 \Rightarrow t_1 = \frac{1}{2}$$

$$\therefore \text{length of focal chord} = a \left(t + \frac{1}{t} \right)^2$$

$$= 4 \left(\frac{1}{2} + 2 \right)^2 = 4 \cdot \frac{25}{4} = 25$$



82. $f(1) = 1 - 1 - 2 = -2$

$$f(-1) = -1 - 1 + 2 = 0$$

$$m = \frac{f(1) - f(-1)}{1 - (-1)} = \frac{-2 - 0}{2} = -1$$

$$\frac{dy}{dx} = 3x^2 - 2x - 2$$

$$3x^2 - 2x - 2 = -1$$

$$\Rightarrow 3x^2 - 2x - 1 = 0$$

$$\Rightarrow (x - 1)(3x + 1) = 0$$

$$\Rightarrow x = 1, -\frac{1}{3}$$

83. $x = 2 + r \cos \theta$

$$y = 3 + r \sin \theta$$

$$\Rightarrow 2 + r \cos \theta + 3 + r \sin \theta = 7$$

$$\Rightarrow r(\cos \theta + \sin \theta) = 2$$

$$\Rightarrow \sin \theta + \cos \theta = \frac{2}{r} = \frac{2}{\pm 4} = \pm \frac{1}{2}$$

$$\Rightarrow 1 + \sin 2\theta = \frac{1}{4}$$

$$\Rightarrow \sin 2\theta = -\frac{3}{4}$$

$$\Rightarrow \frac{2m}{1 + m^2} = -\frac{3}{4}$$

$$\Rightarrow 3m^2 + 8m + 3 = 0$$

$$\Rightarrow m = \frac{-4 \pm \sqrt{7}}{1 - 7}$$

$$\frac{1 - \sqrt{7}}{1 + \sqrt{7}} = \frac{(1 - \sqrt{7})^2}{1 - 7} = \frac{8 - 2\sqrt{7}}{-6} = \frac{-4 + \sqrt{7}}{3}$$

84. From the given functional equation:

$$f(x) = 2^x \quad \forall x \in \mathbb{N}$$

$$2^{a+1} + 2^{a+2} + \dots + 2^{a+10} = 16(2^{10} - 1)$$

$$2^a(2 + 2^2 + \dots + 2^{10}) = 16(2^{10} - 1)$$

$$2^a \cdot \frac{2 \cdot (2^{10} - 1)}{1} = 16(2^{10} - 1)$$

$$2^{a+1} = 16 = 2^4$$

$$a = 3$$

85. $2(1 - \sin^2 \theta) + 3 \sin \theta = 0$

$$\Rightarrow 2 \sin^2 \theta - 3 \sin \theta - 2 = 0$$

$$\Rightarrow (2 \sin \theta + 1)(\sin \theta - 2) = 0$$

$$\Rightarrow \sin \theta = -\frac{1}{2}; \sin \theta = 2 \text{ (reject)}$$

$$\text{roots : } \pi + \frac{\pi}{6}, 2\pi - \frac{\pi}{6}, -\frac{\pi}{6}, -\pi + \frac{\pi}{6}$$

$$\Rightarrow \text{sum of values} = 2\pi$$

86. Let the mid point be S (h, k)

$\therefore P(2h, 0)$ and $Q(0, 2k)$ equation of

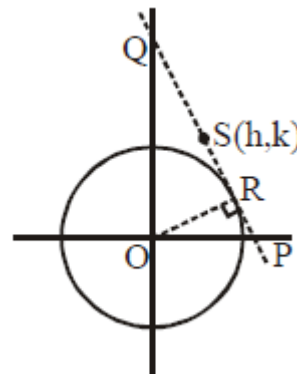
$$PQ: \frac{x}{2h} + \frac{y}{2k} = 1$$

$\therefore PQ$ is tangent to circle at R (say)

$$\therefore OR = 1 \Rightarrow \frac{-1}{\sqrt{\left(\frac{1}{2h}\right)^2 + \left(\frac{1}{2k}\right)^2}} = 1$$

$$\Rightarrow \frac{1}{4h^2} + \frac{1}{4k^2} = 1$$

$$\Rightarrow x^2 + y^2 - 4x^2y^2 = 0$$



87. Let persons be A, B, C, D

$P(\text{Hit}) = 1 - P(\text{none of them hits})$

$$= 1 - P(\bar{A} \cap \bar{B} \cap \bar{C} \cap \bar{D})$$

$$= 1 - P(\bar{A}) \cdot P(\bar{B}) \cdot P(\bar{C}) \cdot P(\bar{D})$$

$$= 1 - \frac{1}{2} \cdot \frac{2}{3} \cdot \frac{3}{4} \cdot \frac{7}{8}$$

$$= \frac{25}{32}$$

88. $x^2 \leq y \leq x + 2$

$x^2 = y; y = x + 2$

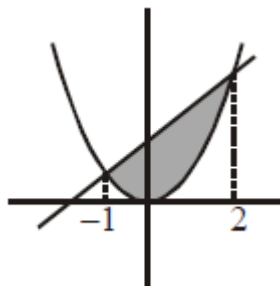
$x^2 = x + 2$

$x^2 - x - 2 = 0$

$(x - 2)(x + 1) = 0$

$x = 2, -1$

Area = $\int_{-1}^2 (x + 2) - x^2 dx = \frac{9}{2}$



89. Roots of the equation $x^2 + x + 1 = 0$ are $\alpha = \omega$ and $\beta = \omega^2$ where ω, ω^2 are complex cube roots of unity

$\therefore \Delta = \begin{vmatrix} y + 1 & \omega & \omega^2 \\ \omega & y + \omega^2 & 1 \\ \omega^2 & 1 & y + \omega \end{vmatrix}$

$R_1 \rightarrow R_1 + R_2 + R_3$

$\Rightarrow \Delta = y \begin{vmatrix} 1 & 1 & 1 \\ \omega & y + \omega^2 & 1 \\ \omega^2 & 1 & y + \omega \end{vmatrix}$

Expanding along R_1 , we get

$\Delta = y \cdot y^2 \Rightarrow D = y^3$

Or

If $\alpha = \omega^2, \beta = \omega$ we get same value or on expansion using $\alpha + \beta = -1, \alpha\beta = 1$ we get value y^3 .

90. \therefore function should be continuous at $x = \frac{\pi}{4}$

$\therefore \lim_{x \rightarrow \frac{\pi}{4}} f(x) = f\left(\frac{\pi}{4}\right)$

$\Rightarrow \lim_{x \rightarrow \frac{\pi}{4}} \frac{\sqrt{2} \cos x - 1}{\cot x - 1} = k$

$\Rightarrow \lim_{x \rightarrow \frac{\pi}{4}} \frac{-\sqrt{2} \sin x}{-\operatorname{cosec}^2 x} = k$ (Using L Hospital Rule)

$\lim_{x \rightarrow \frac{\pi}{4}} \sqrt{2} \sin^3 x = k$

$\Rightarrow k = \sqrt{2} \left(\frac{1}{\sqrt{2}}\right)^3 = \frac{1}{2}$