FIITJEE

Solutions to JEE (Main)-2020

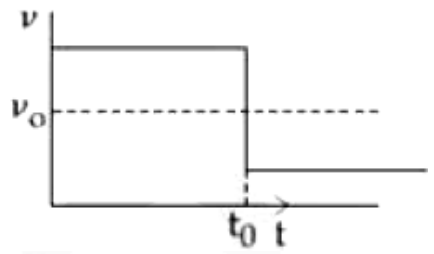
JEE–Main–2020 –Sept–6–First–Shift
PHYSICS, CHEMISTRY & MATHEMATICS

PART –A (PHYSICS)

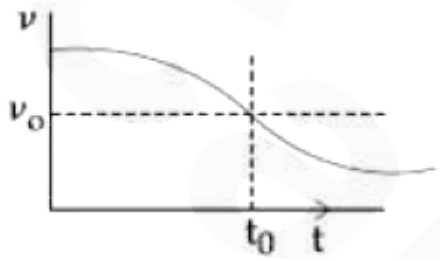
1. A screw gauge has 50 divisions on its circular scale. The circular scale is 4 units ahead of the pitch scale marking, prior to use. Upon one complete rotation of the circular scale, a displacement of 0.5 mm is noticed on the pitch scale. The nature of zero error involved, and the least count of the screw gauge, are respectively:
(A) Negative, $2\,\mu m$ (B) Positive, $10\,\mu m$
(C) Positive, 0.1 mm (D) Positive, $0.1\,\mu m$

2. A sound source S is moving along a straight track with speed v, and is emitting sound of frequency ν_0 (see figure). An observer is standing at a finite distance, at the point O, from the track. The time variation of frequency heard by the observer is best represented by:
(t_0 represents the instant when the distance between the source and observer is minimum)

(A)



(B)



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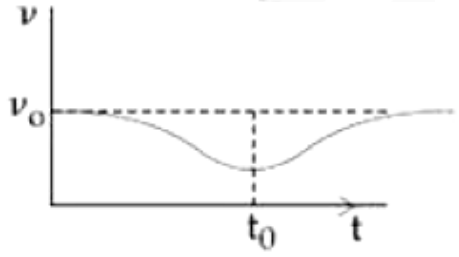

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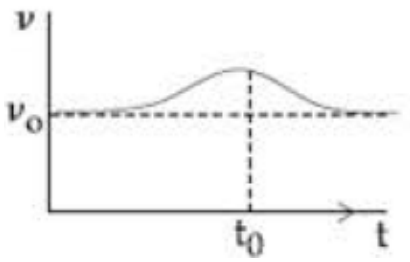
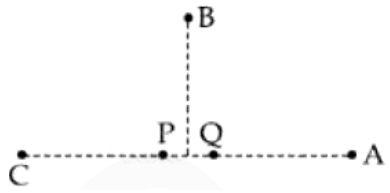


3. In the figure below, P and Q are two equally intense coherent sources emitting radiation of wavelength 20 m. The separation between P and Q is 5 m and the phase of P is ahead of that of Q by 90^o. A, B and C are three distinct points of observation, each equidistant from the midpoint of PQ. The intensities of radiation at A, B, C will be in the ratio:



(A) 0 : 1 : 4
(B) 2 : 1 : 0
(C) 0: 1 : 2
(D) 4 : 1 : 0

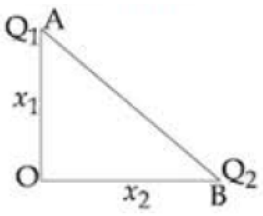
4. If the potential energy between two molecules in given by $U = \frac{A}{r^6} + \frac{B}{r^{12}}$' then at equilibrium, separation between molecules, and the potential energy are:

(A) $\left(\frac{B}{2A}\right)^{1/6}, -\frac{A^2}{2B}$
(B) $\left(\frac{B}{A}\right)^{1/6}, 0$
(C) $\left(\frac{2B}{A}\right)^{1/6}, -\frac{A^2}{4B}$
(D) $\left(\frac{2B}{A}\right)^{1/6}, -\frac{A^2}{2B}$

5. An AC circuit has $R = 100\,\Omega, C = \mu F$ and L = 80 mH, connected in series. The quality factor of the circuit is:

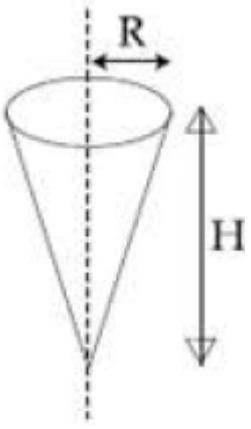
(A) 2
(B) 0.5
(C) 20
(D) 400

6. Charge Q_1 and Q_2 are at point A and B of a right angle triangle OAB (see figure). The resultant electric field at point O is perpendicular to the hypotenuse, then $\frac{Q_1}{Q_2}$ is proportional to:



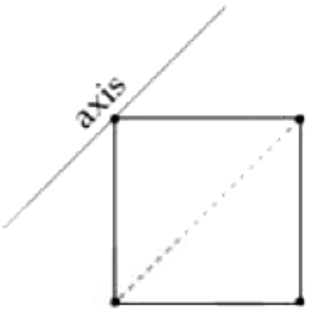
(A) $\frac{x_1^3}{x_2^3}$
(B) $\frac{x_2}{x_1}$
(C) $\frac{x_1}{x_2}$
(D) $\frac{x_2^2}{x_1^2}$

7. Shown in the figure is a hollow icecream cone (it is open at the top). If its mass is M, radius of its top, R and height, H, then its moment of inertia about its axis is:



(A) $\frac{MR^2}{2}$
(B) $\frac{M\left(R^2 + H^2\right)}{4}$
(C) $\frac{MH^2}{3}$
(D) $\frac{MR^2}{3}$

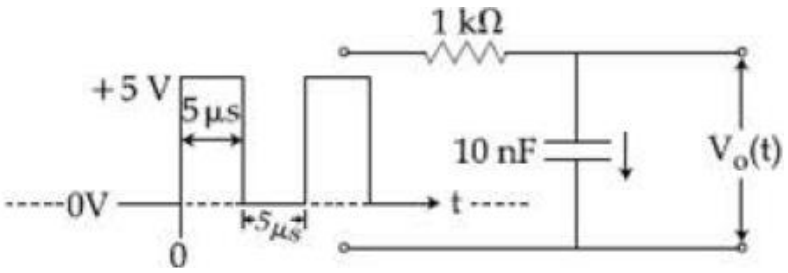
8. Four point masses, each of mass m, are fixed at the corners of a square of side l. The square is rotating with angular frequency ω, about an axis passing through one of the corners of the square and parallel to its diagonal, as shown in the figure. The angular momentum of the square about this axis is:



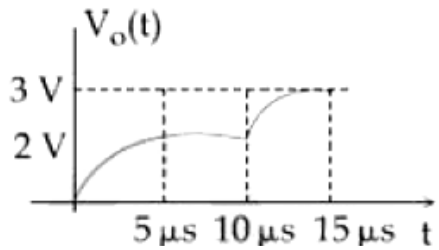
(A) $ml^2\omega$ (B) $5ml^2\omega$

(C) $3ml^2\omega$ (D) $2ml^2\omega$

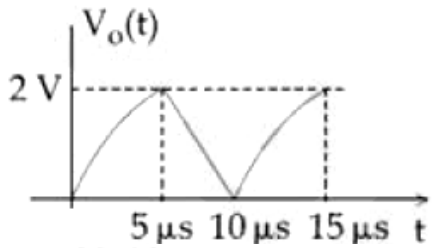
9. For the given input voltage waveform $V_{in}(t)$, the output voltage waveform $V_0(t)$, across the capacitor is correctly depicted by:



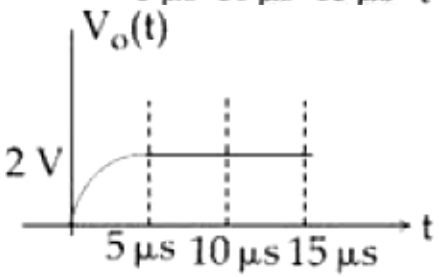
(A)



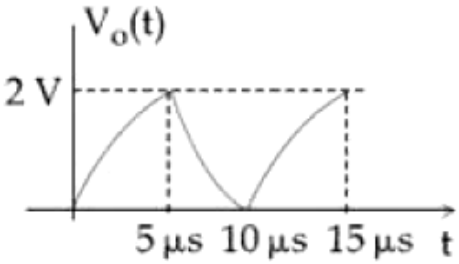
(B)



(C)



(D)



10. A particle of charge q and mass m is moving with a velocity $-v\hat{i}\left(v \neq 0\right)$ towards a large screen placed in the Y – Z plane at a distance d. If there is a magnetic field $\vec{B} = B_0\hat{k}$, the minimum value of v for which the particle will not hit the screen is:

(A) $\frac{qdB_0}{3m}$ (B) $\frac{2qdB_0}{m}$

(C) $\frac{qdB_0}{m}$ (D) $\frac{qdB_0}{2m}$

11. An insect is at the bottom of a hemispherical ditch or radius 1 m. It crawls up the ditch but starts slipping after it is at height h from the bottom. If the coefficient of friction between the ground and the insect is 0.75, then h is: $\left(g = 10 ms^{-2}\right)$

(A) 0.20 m (B) 0.45 m

(C) 0.60 m (D) 0.80 m

12. A satellite is in an elliptical orbit around a planet P. It is observed that the velocity of the satellite when it is farthest from the planet is 6 times less than that when it is closest to the planet. The ratio of distances between the satellite and the planet at closest and farthest points is:

(A) 1 : 6 (B) 1 : 3

(C) 1 : 2 (D) 3 : 4

13. An electron, a doubly ionized helium ion $\left(He^{++}\right)$ and a proton are having the same kinetic energy. The relation between their respective de – Broglie wavelength λ_e, λ_{He++} and λ_p is:

(A) $\lambda_e > \lambda_{He++} > \lambda_P$ (B) $\lambda_e < \lambda_{He++} = \lambda_P$

(C) $\lambda_e > \lambda_P > \lambda_{He++}$ (D) $\lambda_e < \lambda_P < \lambda_{He++}$

14. A clock has a continuously moving second's hand of 0.1 m length. The average acceleration of the tip of the hand (in units of ms^{-2}) is of the order of:

(A) 10^{-3} (B) 10^{-4}

(C) 10^{-2} (D) 10^{-1}

15. You are given that Mass of ${}^{7}_{2}Li = 7.0160u$ Mass of ${}^{4}_{2}He = 4.0026u$ and ${}^{1}_{1}H = 1.0079u$. When 20 g of ${}^{7}_{3}Li$ is converted into ${}^{4}_{2}He$ by proton capture, the energy liberated, (in kWh), is [Mass of nucleon = $\frac{1Gev}{c^2}$]

(A) 4.5×10^{5} (B) 8×10^{6}

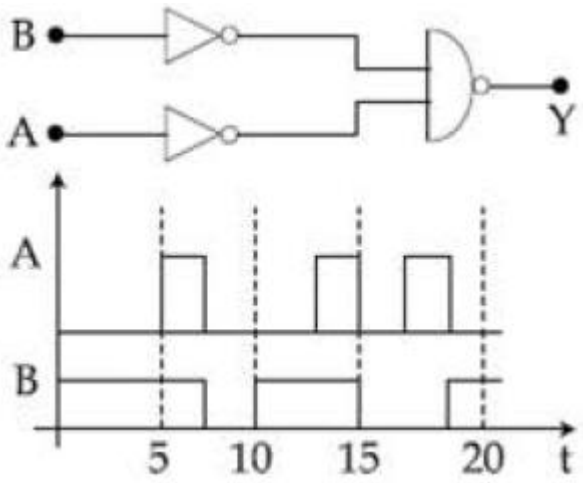
(C) 6.82×10^{5} (D) 1.33×10^{6}

16. A point like object is placed at a distance of 1 m in front of convex lens of focal length 0.5 m. A plane mirror is placed at a distance of 2m behind the lens. The position and nature of the final image formed by the system is:

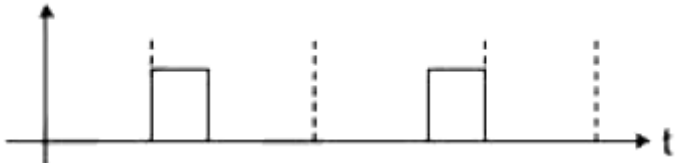
(A) 2.6 m from the mirror, real (B) 1 m from the mirror, virtual

(C) 1 m from the mirror, real (D) 2.6 m from the mirror, virtual

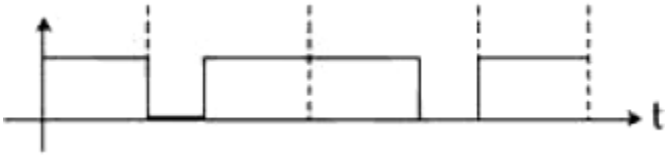
17. Identify the correct output signal Y in the given combination of gates (as shown) for the given inputs A and B.



(A)



(B)



(C)

(D)

18. Molecules of an ideal gas are known to have three translational degrees of freedom and two rotational degrees of freedom. The gas is maintained at a temperature of T.

The total internal energy, U of a mole of this gas, and the value of $\gamma\left(=\frac{C_P}{C_v}\right)$ are given, respectively, by:

(A) $U=\frac{5}{2}RT$ and $\gamma=\frac{6}{5}$

(B) $U=5RT$ and $\gamma=\frac{7}{5}$

(C) $U=\frac{5}{2}RT$ and $\gamma=\frac{7}{5}$

(D) $U=5RT$ and $\gamma=\frac{6}{5}$

19. An object of mass m is suspended at the end of a massless wire of length L and area of cross – selection, A. Young modulus of the material of the wire is Y. If the mass is pulled down slightly its frequency of oscillation along the vertical direction is:

(A) $f=\frac{1}{2\pi}\sqrt{\frac{mL}{YA}}$

(B) $f=\frac{1}{2\pi}\sqrt{\frac{YA}{mL}}$

(C) $f=\frac{1}{2\pi}\sqrt{\frac{mA}{YL}}$

(D) $f=\frac{1}{2\pi}\sqrt{\frac{YL}{mA}}$

20. An electron is moving along + x direction with a velocity of $6\times10^{6}\text{ms}^{-1}$. It enters a region of uniform electric field of 300 V/cm pointing along + y direction. The magnitude and direction of the magnetic field set up in this region such that the electron keeps moving along the x direction will be:

(A) $3\times10^{-4}\text{T}$, along + z direction (B) $5\times10^{-3}\text{T}$, along – z direction

(C) $5\times10^{-3}\text{T}$, along + z direction (D) $3\times10^{-4}\text{T}$, along – z direction

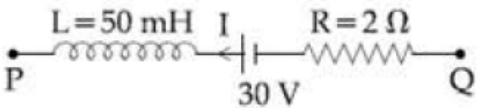
21. The density of a solid metal sphere is determined by measuring its mass and its diameter. The maximum error in the density of the sphere is $\left(\frac{x}{100}\right)\%$. If the relative errors in measuring the mass and the diameter are 6.0% and 1.5% respectively, the value of x is _____.

22. Two bodies of the same mass are moving with the same speed, but in different directions in a plane. They have a completely inelastic collision and move together thereafter with a final speed which is half of their initial speed. The angle between the initial velocities of the two bodies (in degree) is _____.

23. Suppose that intensity of a laser is $\left(\frac{315}{\pi}\right)\text{W/m}^2$. The rms electric field, in units of V/m associated with this source is close to the nearest integer is _____.
$\left(\varepsilon_0 = 8.86\times10^{-12}\,\text{C}^2\text{Nm}^{-2}; c = 3\times10^{8}\,\text{ms}^{-1}\right)$

24. Initially a gas of diatomic molecules is contained in a cylinder of volume V_1 at a pressure P_1 and temperature 250 K. Assuming that 25% of the molecules get dissociated causing a change in number of moles. The pressure of the resulting gas at temperature 2000 K, when contained in a volume $2V_1$ is given by P_2. The ratio $\frac{P_2}{P_1}$ is _____.

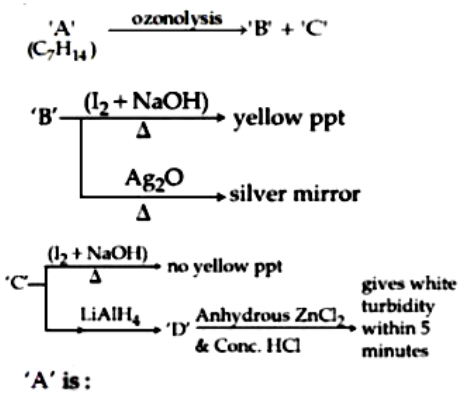
25. A part of complete circuit is shown in the figure. At some instant, the value of current I is 1 A and it is decreasing at a rate of $10^2\,\text{A s}^{-1}$. The value of the potential difference $V_P - V_Q$, (in volts) at that instant, is _____.



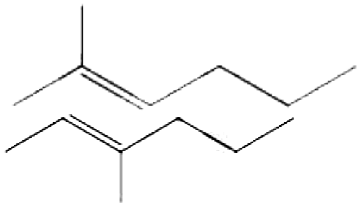
PART –B (CHEMISTRY)

26. The correct statement with respect to dinitrogen is:
(A) N_2 is paramagnetic in nature
(B) It can combine with dioxygen at 25° C.
(C) Liquid dinitrogen is not used in cryosurgery
(D) It can be used as an inert diluent for reactive chemicals

27. Consider the following reactions:

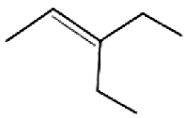


'A' is:

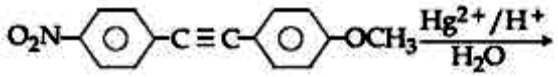
(A) 

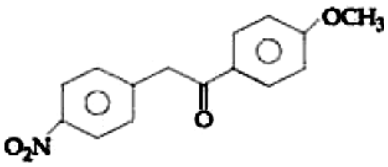
(B) 

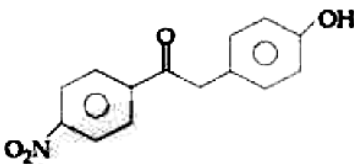
(C)

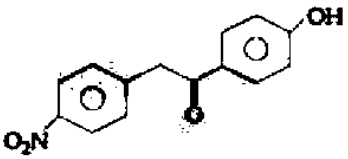
(D) 

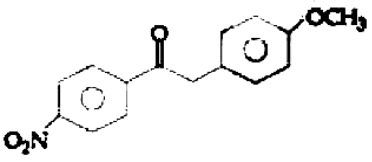
28. The major product obtained from the following reaction is:



(A) 

(B) 

(C) 

(D) 

29. A solution of two components containing n_1 moles of the 1st component and n^2 moles of the 2nd component is prepared. M_1 and M_2 are the molecular weights of component 1 and 2 respectively. If d is the density of the solution in gmL^{-1}, C_2 is the molarity and x_2 is the mole fraction of the 2nd component, then C_2 can be expressed as:

(A) $C_2 = \dfrac{1000x_2}{M_1 + x_2(M_2 - M_1)}$

(B) $C_2 = \dfrac{dx_2}{M_2 + x_2(M_2 - M_1)}$

(C) $C_2 = \dfrac{1000\,dx_2}{M_1 + x_2(M_2 - M_1)}$

(D) $C_2 = \dfrac{dx_1}{M_2 + x_2(M_2 - M_1)}$

30. The INCORRECT statement is:
(A) bronze is an alloy of copper and tin
(B) cast iron is used to manufacture wrought iron
(C) german silver is an alloy of zinc, copper and nickel
(D) brass is an alloy of copper and nickel.

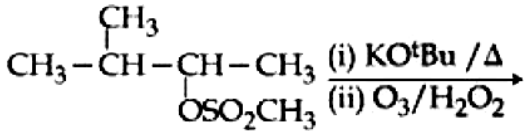
31. Consider the Assertion and Reason given below.
Assertion (A): Ethene polymerized in the presence of Ziegler Natta Catalyst at high temperature and pressure is used to make buckets and dustbins.
Reason (R): High density polymers are closely packed and are chemically inert.
Choose the correct answer from the following:
(A) (A) is correct but (R) is wrong
(B) Both (A) and (R) are correct but (R) is not the correct explanation of (A)
(C) Both (A) and (R) are correct and (R) is the correct explanation of (A)
(D) (A) and (R) both are wrong.

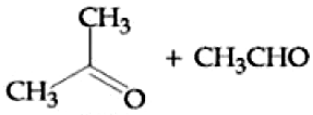
32. Arrange the following solutions in the decreasing order of pOH
(1) 0.01 M HCl (2) 0.01 M NaOH
(3) 0.01 M CH_3COONa (4) 0.01 M NaCl

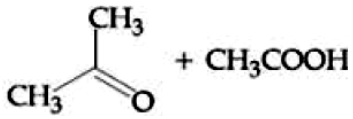
(A) (1) > (3) > (4) > (2) (B) (1) > (4) > (3) > (2)
(C) (2) > (3) > (4) > (1) (D) (2) > (4) > (3) > (1)

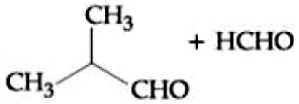
33. Among the sulphates of alkaline earth metals, the solubilities of $BeSO_4$ and $MgSO_4$ in water, respectively, are:
(A) poor and poor (B) high and poor
(C) high and high (D) poor and high

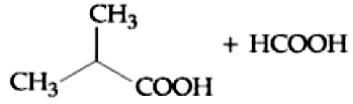
34. The major products of the following reaction are:



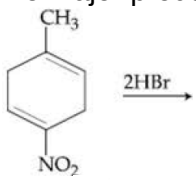
(A) 

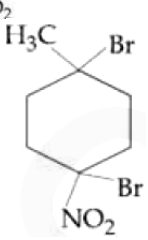
(B) 

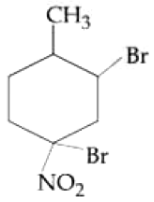
(C) 

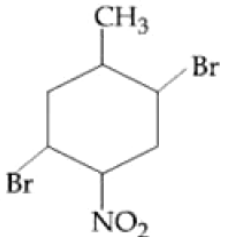
(D) 

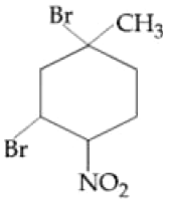
35. The major product of the following reaction is:



(A) 

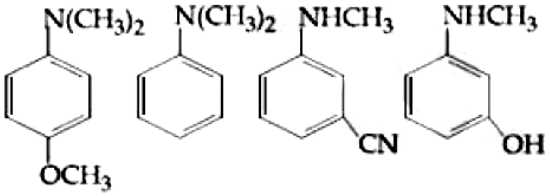
(B) 

(C) 

(D) 

36. The present of soluble fluoride ion upto 1 ppm concentration in drinking water, is:
(A) harmful for teeth
(B) harmful to skin
(C) harmful to bones
(D) safe for teeth

37. The increasing order of pK_b values of the following compounds is:



I II III IV

(A) II < IV < III < I
(B) I < II < IV < III
(C) II < I < III < IV
(D) I < II < III < IV

38. Which of the following compounds shows geometrical isomerism?
(A) 2 – methylpent 2 – ene
(B) 4 – methylpent 2 – ene
(C) 4 – methylpent – 1 – ene
(D) 2 – methylpent –1 – ene

39. The set that contains atomic numbers of only transition elements, is
(A) 37, 42, 50, 64
(B) 21, 25, 42, 72
(C) 9, 17, 34, 38
(D) 21, 32, 53, 64

40. The variation of equilibrium constant with temperature is given below:

Temperature	Equilibrium Constant
$T_1 = 25^oC$	$K_1 = 10$
$T_2 = 100^oC$	$K_2 = 100$

The value of $\Delta H^o, \Delta G^o$ at T_1 and ΔG^o at T_2

(in $kJ\,mol^{-1}$) respectively, are close to

[Use $R = 8.314 JK^{-1}mol^{-1}$]

(A) 28.7, – 7.14 and – 5.71
(B) 0.64 – 7.14 and – 5.71
(C) 28.4, – 5.71 and – 14.29
(D) 0.64, – 5.71 and –14.29

41. Kraft temperature is the temperature:
(A) below which the aqueous solution of detergents starts freezing
(B) below which the formation of micelles takes place
(C) above which the aqueous solution of detergents starts boiling
(D) above which the formation of micelles takes place.

42. For the reaction

$$Fe_2N(s) + \frac{3}{2}H_2(g) = 2Fe(s) + NH_3(g)$$

(A) $K_c = K_p(RT)$
(B) $K_c = K_P(RT)^{-1/2}$
(C) $K_c = K_P(RT)^{1/2}$
(D) $K_c = K_P(RT)^{3/2}$

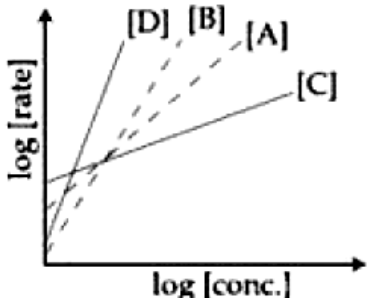
43. The species that has a spin – only magnetic moment of 5.9 BM, is:
(T_d = tetrahedral)

(A) $\left[Ni(CN)_4\right]^{2-}$ (square planar) (B) $\left[NiCl_4\right]^{2-}(T_d)$

(C) $Ni(CO)_4(T_d)$ (D) $\left[MnBr_4\right]^{2-}(T_d)$

44. The lanthanoid that does NOT show +4 oxidation state is:
(A) Dy (B) Ce
(C) Eu (D) Tb

45. Consider the following reactions
$A \rightarrow P1; B \rightarrow P2; C \rightarrow P3; D \rightarrow P4,$
The order of the above reactions are a, b, c and d, respectively. The following graph is obtained when log[rate] vs. log[conc.] are plotted:



Among the following, the correct sequence for the order of the reactions is:
(A) d > a > b > c (B) a > b > c > d
(C) c > a > b > d (D) d > b > a > c

46. In an estimation of bromine by Carius method, 1.6 g of an organic compound gave 1.88 g of AgBr. The mass percentage of bromine in the compound is _____
(Atomic mass, Ag = 108, Br = 80 g mol^{-1})

47. Potassium chlorate is prepared by the electrolysis of KCl in basic solution
$6HO^- + Cl^- \rightarrow ClO_3^- + 3H_2O + 6e^-$
If only 60% of the current is utilized in the reaction, the time (rounded to the nearest hour) required to produce 10 g of $KClO_3$ using a current of 2A is _____.
(Given : F = 96, 500 C mol^{-1}; molar mass of $KClO_3$ = 122 g mol^{-1})

48. The number of Cl = O bonds in perchloric acid is," _____".

49. The elevation of boiling point of 0.10 m aqueous $CrCl_3xNH_3$ solution is two times that of 0.05 m aqueous $CaCl_2$ solution. The value of x is _____
[Assume 100% ionisation of the complex and $CaCl_2$, coordination number of Cr as 6, and that all NH_3 molecules are present inside the coordination sphere]

50. A spherical balloon of radius 3 cm containing helium gas has a pressure of 48×10^{-3} bar. At the same temperature, the pressure, of a spherical balloon of radius 12 cm containing the same amount of gas will be _____ $\times10^{-6}$ bar.

PART–C (MATHEMATICS)

51. If α and β be two roots of the equation $x^2 - 64x + 256 = 0$. Then the value of $\left(\frac{\alpha^3}{\beta^5}\right)^{1/8} + \left(\frac{\beta^3}{\beta^5}\right)^{1/8}$ is:

(A) 2
(B) 3
(C) 1
(D) 4

52. The area (in sq. units) of the region $A = \left\{(x,y) : |x| + |y| \le 1,\ 2y^2 \ge |x|\right\}$ is:

(A) $\frac{1}{3}$
(B) $\frac{7}{6}$
(C) $\frac{1}{6}$
(D) $\frac{5}{6}$

53. The general solution of the differential equation $\sqrt{1+x^2+y^2+x^2y^2} + xy\frac{dy}{dx} = 0$ is:
(where C is a constant of integration)

(A) $\sqrt{1+y^2} + \sqrt{1+x^2} = \frac{1}{2}\log_e\left(\frac{\sqrt{1+x^2}+1}{\sqrt{1+x^2}-1}\right) + C$

(B) $\sqrt{1+y^2} - \sqrt{1+x^2} = \frac{1}{2}\log_e\left(\frac{\sqrt{1+x^2}+1}{\sqrt{1+x^2}-1}\right) + C$

(C) $\sqrt{1+y^2} - \sqrt{1+x^2} = \frac{1}{2}\log_e\left(\frac{\sqrt{1+x^2}+1}{\sqrt{1+x^2}-1}\right) + C$

(D) $\sqrt{1+y^2} + \sqrt{1+x^2} = \frac{1}{2}\log_e\left(\frac{\sqrt{1+x^2}-1}{\sqrt{1+x^2}+1}\right) + C$

54. Let L_1 be a tangent to the parabola $y^2 = 4(x+1)$ and L_2 be a tangent to the parabola $y^2 = 8(x+2)$ such that L_1 and L_2 intersect at right angles. Then L_1 and L_2 meet on the straight line:

(A) $x + 3 = 0$
(B) $2x + 1 = 0$
(C) $x + 2 = 0$
(D) $x + 2y = 0$

55. If $f(x+y) = f(x)f(y)$ and $\sum_{x=1}^{\infty} f(x) = 2, x, y \in N$ where N is the set of all natural numbers, then the value of $\frac{f(4)}{f(2)}$ is:

(A) $\frac{2}{3}$
(B) $\frac{1}{9}$
(C) $\frac{1}{3}$
(D) $\frac{4}{9}$

56. If $I_1 = \int_0^1 \left(1-x^{50}\right)^{100} dx$ and $I_2 = \int_0^1 \left(1-x^{50}\right)^{101} dx$ such that $I_2 = \alpha I_1$ then α equals to:

(A) $\frac{5049}{5050}$ (B) $\frac{5050}{5049}$

(C) $\frac{5050}{5051}$ (D) $\frac{5051}{5050}$

57. Out of 11 consecutive natural numbers if three numbers are selected at random (without repetition), then the probability that they are in A.P. with positive common difference, is:

(A) $\frac{15}{101}$ (B) $\frac{5}{101}$

(C) $\frac{5}{33}$ (D) $\frac{10}{99}$

58. A ray of light coming from the point $\left(2, 2\sqrt{3}\right)$ is incident at an angle 30^o on the line $x = 1$ at the point A. The ray gets reflected on the line x = 1 and meets x – axis at the point B. Then, the line AB passes through the point:

(A) $\left(3, -\frac{1}{\sqrt{3}}\right)$ (B) $\left(4, -\frac{\sqrt{3}}{2}\right)$

(C) $\left(3, -\sqrt{3}\right)$ (D) $\left(4, -\sqrt{3}\right)$

59. Which of the following points lies on the locus of the foot of perpendicular drawn upon any tangent to the ellipse, $\frac{x^2}{4} + \frac{y^2}{2} = 1$ from any of its foci?

(A) $\left(-2, \sqrt{3}\right)$ (B) $\left(-1, \sqrt{2}\right)$

(C) $\left(-1, \sqrt{3}\right)$ (D) (1, 2)

60. The region represented by $\left\{z = x + iy \in C : |z| - Re(z) \le 1\right\}$ is also given by the inequality:

(A) $y^2 \ge 2(x+1)$ (B) $y^2 \le 2\left(x + \frac{1}{2}\right)$

(C) $y^2 \le x + \frac{1}{2}$ (D) $y^2 \ge x + 1$

61. The position of a moving car at time t is given by $f(t) = at^2 + bt + c,\ t > 0$, where a, b and c are real numbers greater than 1. Then the average speed of the car over the time interval $[t_1, t_2]$ is attained at the point:

(A) $\frac{(t_2 - t_1)}{2}$ (B) $a(t_2 - t_1) + b$

(C) $\frac{(t_1 + t_2)}{2}$ (D) $2a(t_1 + t_2) + b$

62. $\lim\limits_{x\to1}\left(\dfrac{\int_0^{(x-1)^2} t\cos\left(t^2\right)dt}{(x-1)\sin(x-1)}\right)$

(A) is equal to $\dfrac{1}{2}$ (B) is equal to 1

(C) is equal to $-\dfrac{1}{2}$ (D) does not exist

63. If $\sum\limits_{i=1}^{n}(x_i-a)=n$ and $\sum\limits_{i=1}^{n}(x_i-a)^2=na$, $(n,a>1)$ then the standard deviation of n observations $x_1,x_2,.....,x_n$ is:

(A) a – 1 (B) $n\sqrt{a-1}$

(C) $\sqrt{n(a-1)}$ (D) $\sqrt{a-1}$

64. If {p} denotes the fractional part of the number p, then $\left\{\dfrac{3^{200}}{8}\right\}$, is equal to

(A) $\dfrac{5}{8}$ (B) $\dfrac{7}{8}$

(C) $\dfrac{3}{8}$ (D) $\dfrac{1}{8}$

65. The shortest distance between the lines $\dfrac{x-1}{0}=\dfrac{y+1}{-1}=\dfrac{z}{1}$ and $x+y+z+1=0, 2x-y+z+3=0$ is:

(A) 1 (B) $\dfrac{1}{\sqrt{3}}$

(C) $\dfrac{1}{\sqrt{2}}$ (D) $\dfrac{1}{2}$

66. The negation of the Boolean expression $p\vee(\sim p\wedge q)$ is equivalent to:

(A) $p\wedge\sim q$ (B) $\sim p\wedge\sim q$

(C) $\sim p\vee\sim q$ (D) $\sim p\vee q$

67. Two families with three members each and one family with four members are to be seated in a row. In how many ways can they be seated so that the same family members are not separated?

(A) 2!3!4! (B) $(3!)^3.(4!)$

(C) $(3!)^2.(4!)$ (D) $3!(4!)^3$

68. Let m and M be respectively the minimum and maximum values of $\begin{vmatrix}\cos^2x & 1+\sin^2x & \sin2x\\ 1+\cos^2x & \sin^2x & \sin2x\\ \cos^2x & \sin^2x & 1+\sin2x\end{vmatrix}$. Then the ordered pair (m, M) is equal to:

(A) (–3, 3) (B) (–3, –1)

(C) (–4, –1) (D) (1, 3)

69. Let a, b, c, d and p be any non zero distinct real numbers such that $\left(a^2+b^2+c^2\right)p^2-2(ab+bc+cd)p+\left(b^2+c^2+d^2\right)=0$. Then:

(A) a, c, p are in A.P. (B) a, c, p are in G.P.
(C) a, b, c, d are in G.P. (D) a, b, c, d are in A.P.

70. The value of λ and μ for which the system of linear equations

$$x+y+z=2$$
$$x+2y+3z=5$$
$$x+3y+\lambda z=\mu$$

has infinitely many solutions are, respectively:

(A) 6 and 8 (B) 5 and 7
(C) 5 and 8 (D) 4 and 9

71. Set A has m elements and Set B has n elements. If the total number of subsets of A is 112 more than the total number of subsets of B, then the value of m.n is _____.

72. Let $f:R\to R$ be defined as $f(x)=\begin{cases} x^5\sin\left(\frac{1}{x}\right)+5x^2, & x<0 \\ 0, & x=0 \\ x^5\cos\left(\frac{1}{x}\right)+\lambda x^2, & x>0 \end{cases}$

The value of λ for which $f''(0)$ exists, is _____

73. If $\vec{a}$ and $\vec{b}$ are unit vectors, then the greatest value of $\sqrt{3}\left|\vec{a}+\vec{b}\right|+\left|\vec{a}-\vec{b}\right|$ is _____

74. Let AD and BC be two vertical poles at A and b respectively on a horizontal ground. If AD = 8 m, BC = 11 m and AB = 10 m; then the distance (in meters) of a point M on AB from the point A such that MD^2+MC^2 is minimum is _____.

75. The angle of elevation of the top of a hill from a point on the horizontal plane passing through the foot of the hill is found to be 45^o. After walking a distance of 80 meters towards the top, up a slope inclined at an angle of 30^o to the horizontal plane, the angle of elevation of the top of the hill becomes 75^o. Then the height of the hill (in metres) is _____.