FIITJEE

Solutions to JEE (Main)-2019

JEE–Main–2019 –Apr–10–Second–Shift
PHYSICS, CHEMISTRY & MATHEMATICS

Time Allotted: 3 Hours **Maximum Marks: 360**

- Do not open this Test Booklet until you are asked to do so.
- Please read the instructions carefully. You are allotted 5 minutes specifically for this purpose.

Important Instructions:

1. Immediately fill in the particulars on this page of the Test Booklet with *Blue / Black Ball Point Pen. Use of pencil is strictly prohibited.*
2. The Answer Sheet is kept inside this Test Booklet. When you are directed to open the Test Booklet, take out the Answer Sheet and fill in the particulars carefully.
3. The test is of **3 hours** duration.
4. The Test Booklet consists of **90** questions. The maximum marks are **360**.
5. There are ***three*** parts in the question paper A, B, C consisting of **Physics, Chemistry** and **Mathematics** having 30 questions in each part of equal weightage. Each question is allotted **4 (four)** marks for correct response.
6. *Candidates will be awarded marks as stated above in instruction No.5 for correct response of each question. One mark will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.*
7. There is only one correct response for each question. Filling up more than one response in any question will be treated as wrong response and marks for wrong response will be deducted accordingly as per instruction 6 above.
8. Use ***Blue / Black Ball Point Pen only*** for writing particulars / marking responses on ***Side-1*** and ***Side-2*** of the Answer Sheet. ***Use of pencil is strictly prohibited.***
9. No candidate is allowed to carry any textual material, printed or written, bits of papers, pager, mobile phone, any electronic device, etc. except the Admit Card inside the examination hall / room.
10. On completion of the test, the candidate must hand over the Answer Sheet to the Invigilator on duty in the Room / Hall. ***However, the candidates are allowed to take away this Test Booklet with them.***
11. **Do not fold or make any stray marks on the Answer Sheet.**

Name of the Candidate (in Capital Letters) :_____

Roll Number :_____

Candidate's Signature: _____

PART –A (PHYSICS)

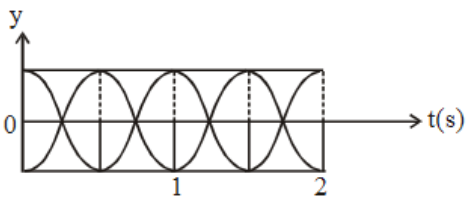
1. One mole of an ideal gas passes through a process where pressure and volume obey the relation $P = P_o\left[1-\frac{1}{2}\left(\frac{V_o}{V}\right)^2\right]$. Here P_o and V_o are constants. Calculate the change in the temperature of the gas if its volume change from V_o to $2V_o$

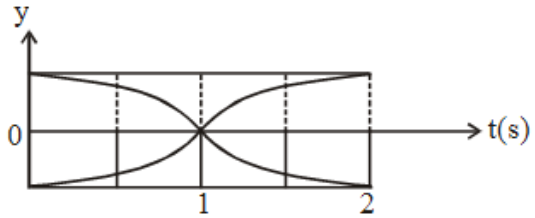
(A) $\frac{1}{4}\frac{P_oV_o}{R}$ (B) $\frac{1}{2}\frac{P_oV_o}{R}$ (C) $\frac{5}{4}\frac{P_oV_o}{R}$ (D) $\frac{3}{4}\frac{P_oV_o}{R}$

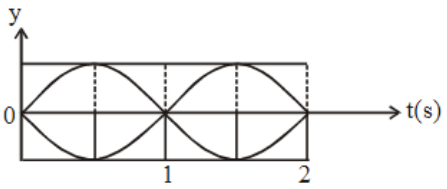
2. A solid sphere of mass M and radius R is divided into two unequal parts. The first part has a mass of $\frac{7M}{8}$ and is converted into a uniform disc of radius 2R. The second part is converted into a uniform solid sphere. Let I_1 be the moment of inertia of the disc about its axis and I_2 be the moment of inertia of the new sphere about its axis. The ratio of I_1/I_2 is given by:

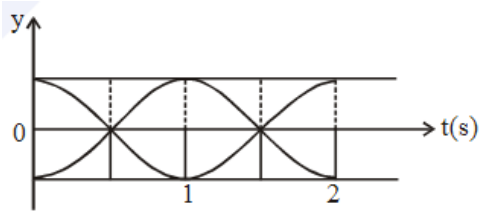
(A) 285 (B) 185
(C) 65 (D) 140

3. The correct figure that shows, schematically, the wave pattern produced by superposition of two waves of frequencies 9 Hz and 11 Hz,

(A) 

(B) 

(C) 

(D) 

4. In an experiment, brass and steel wires of length 1 m each with areas of cross section 1 mm^2 are used. The wires are connected in series and one end of the combined wire is connected to a rigid support and other end is subjected to elongation. The stress requires to produced a new elongation of 0.2 mm is

[Given, the Young's Modulus for steel and brass are respectively 120×10^9 N/m^2 and 60×10^9 N/m^2]

(A) 1.8×10^6 N/m^2 (B) 0.2×10^6 N/m^2
(C) 1.2×10^6 N/m^2 (D) 4.0×10^6 N/m^2

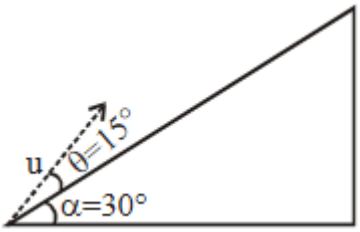
5. When heat Q is supplied to a diatomic gas of rigid molecules at constant volume its temperature increases by ΔT. The heat required to produce the same change in temperature, at constant pressure is

(A) $\frac{3}{2}Q$ (B) $\frac{5}{3}Q$
(C) $\frac{7}{5}Q$ (D) $\frac{2}{3}Q$

6. A bullet of mass 20 g has an initial speed of 1 ms^{-1} just before it starts penetrating a mud wall of thickness 20 cm. If the wall offers a mean resistances of 2.5×10^{-2} N, the speed of the bullet after emerging from the other side of the wall is close to
(A) 0.7 ms^{-1} (B) 0.3 ms^{-1}
(C) 0.1 ms^{-1} (D) 0.4 ms^{-1}

7. The elastic limit of brass is 379 MPa. What should be the minimum diameter of a brass rod if it is to support a 400 N load without exceeding its elastic limit?
(A) 1.00 mm (B) 1.16 mm
(C) 0.90 mm (D) 1.36 mm

8. A plane is inclined at an angle $\alpha = 30^o$ with respect to the horizontal. A particle is projected with a speed u = 2 ms^{-1}, from the base of the plant, making an angle $\theta = 15^o$ with respect to the plane as shown in the figure. The distance from the base at which the particle hits the plane is close to
(Take g = 10 ms^2)

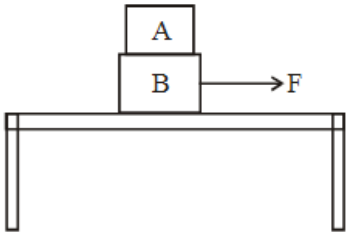


(A) 18 cm (B) 14 cm
(C) 26 cm (D) 20 cm

9. The magnitude of the magnetic field at the centre of an equilateral triangular loop of side 1 m which is carrying a current of 10 A is: [Take $\mu_o = 4\pi \times 10^{-7}$ NA^{-2}]
(A) 9μT (B) 1μT
(C) 3μT (D) 18μT

10. Two radioactive substances A and B have decay constants 5λ and λ respectively. At t = 0, a sample has the same number of the two nuclei. The time taken for the ratio of the number of nuclei to become $\left(\frac{1}{e}\right)^2$ will be
(A) 1/λ (B) 1/4λ
(C) 2/λ (D) 1/2λ

11. Two blocks A and B of masses m_A = 1 kg and m_B = 3 kg are kept on the table as shown in figure. The coefficient of friction between A and B is 0.2 and between B and the surface of the table is also 0.2. The maximum force F that can be applied on B horizontal, so that the block A does not slide over the block B is:
[Take g = 10 m/s^2]

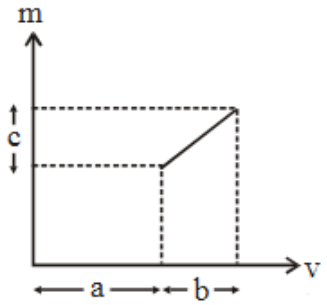


(A) 8 N (B) 16 N
(C) 12 N (D) 40 N

12. The formula $X = 5YZ^2$ X and Z have dimensions of capacitance and magnetic field respectively. What are the dimensions of Y in SI units?
(A) $[M^{-2} L^0 T^{-4} A^{-2}]$ (B) $[M^{-3} L^{-2} T^8 A^{-1}]$
(C) $[M^{-2} L^{-2} T^6 A^3]$ (D) $[M^{-1} L^{-2} T^4 A^2]$

13. In Li^{++}, electron in first Bohr orbit is excited to a level by a radiation of wavelength λ. When the ion gets deexcited to the ground state in all possible ways(including intermediate emission) a total of six spectral lines are observed. What is the value of λ?
(Given: $h = 6.63 \times 10^{34}$ js; $e = 3 \times 10^8$ ms^{-1})
(A) 10.8 nm (B) 11.4 nm
(C) 9.4 nm (D) 12.3 nm

14. The graph shows how the magnification m produced by a thin lens varies with image distance ν. What is the focal length of the lens used?



(A) $\frac{b^2}{ac}$ (B) $\frac{a}{c}$
(C) $\frac{b^2c}{a}$ (D) $\frac{b}{c}$

15. A spaceship orbits around a planet at a height of 20 km from its surface. Assuming that only gravitational field of the plant acts on the spaceship. What will be the number of complete revolutions made by the spaceship in 24 hours around the plane?
[Given: Mass of plane = 8×10^{22} kg, Radius of planet = 2×10^6 m, Gravitational constant $G = 6.67 \times 10^{-}11$ Mn^2/kg^2]
(A) 9 (B) 11
(C) 13 (D) 17

16. Light is incident normally on a completely absorbing surface with an energy flux of 25 W cm^{-2}. If the surface has an area of 25 cm^2, the maximum transferred to the surface in 40 min time duration will be
(A) 6.3×10^{-4} Ns (B) 3.5×10^{-6} Ns
(C) 5.0×10^{-3} Ns (D) 1.4×10^{-6} Ns

17. The time dependence of the position of a particle of mass m = 2 is given by $\vec{r}(t) = 2t\hat{i} - 3t^2\hat{j}$
Its angular momentum with respect to the origin at time t = 2 is .
(A) $-48\hat{k}$ (B) $48(\hat{i} + \hat{j})$
(C) $36\hat{k}$ (D) $-34(\hat{k} - \hat{i})$

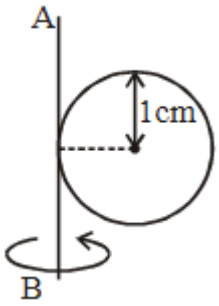
18. Water from a tap emerges vertically downwards with an initial speed of 1.0 ms^{-1}. The cross-sectional area of the tap is $10^{-4}m^2$. Assume that the pressure is constant throughout the stream of water and that flow is streamlined. The cross-sectional area of the stream, 0.15 m below the tap would be:
(take g = 110 ms^{-2})
(A) 5×10^{-4} m^2 (B) 5×10^{-5} m^2
(C) 1×10^{-5} m^2 (D) 2×10^{-5} m^2

19. Space between two concentric conducting spheres of radii a and b (b >a) is filled with a medium of resistivity ρ. The resistance between the two spheres will be

(A) $\frac{\rho}{2\pi}\left(\frac{1}{a}+\frac{1}{b}\right)$ (B) $\frac{\rho}{2\pi}\left(\frac{1}{a}-\frac{1}{b}\right)$

(C) $\frac{\rho}{4\pi}\left(\frac{1}{a}+\frac{1}{b}\right)$ (D) $\frac{\rho}{4\pi}\left(\frac{1}{a}-\frac{1}{b}\right)$

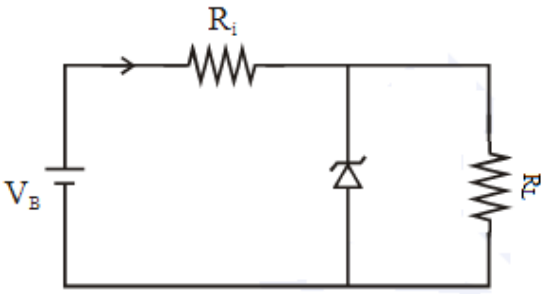
20. A metal coin of mass 5 g and radius 1 cm is fixed to a thin stick AB of negligible mass as shown in the figure. The system is initially at rest. The constant torque, that will make the system rotate about AB at 25 rotations per second is 5 s is close to



(A) 2.0×10^{-5} Nm (B) 4.0×10^{-6} Nm

(C) 1.6×10^{-5} Nm (D) 7.9×10^{-6} Nm

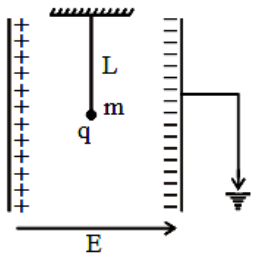
21. The figure represents a voltage regulator circuit using a Zener diode. The breakdown voltage of the Zener diode is 6 V and the load resistance is R_L= 4kΩ. The series resistance of the circuit is R_i = 1kΩ. If the battery voltage V_8 varies from 8 V to 16 V, what are the minimum and maximum values of the current through Zener diode?



(A) 0.5 mA; 0.6 mA (B) 1 mA; 8.5 mA

(C) 1.5 mA; 8.5 mA (D) 0.5 mA; 8.5 mA

22. A simple pendulum of length L is placed between the plates of a parallel plate capacitor having electric field E, as shown in figure. Its bob has mass m and charge q. the time period of the pendulum is given by



(A) $2\pi\sqrt{\frac{L}{\sqrt{g^2+\left(\frac{qE}{m}\right)^2}}}$ (B) $2\pi\sqrt{\frac{L}{\left(g+\frac{qE}{m}\right)}}$

(C) $2\pi\sqrt{\frac{L}{\left(g-\frac{qE}{m}\right)}}$ (D) $2\pi\sqrt{\frac{L}{\sqrt{g^2-\frac{q^2E^2}{m^2}}}}$

23. In free space, a particle A of charge 1 μC is held fixed at a point P. Another particle B of the same charge and mass 4 μg is kept at a distance of 1 mm from P. If B is released, then its velocity at a distance of 9 mm from P is

$\left[\text{Take } \frac{1}{4\pi\varepsilon_o} = 9\times10^9\ \text{Nm}^2\text{C}^{-2}\right]$

(A) 1.5×10^2 m/s
(B) 2.0×10^3 m/s
(C) 1.0 m/s
(D) 3.0×10^4 m/s

24. A 2 mW laser operates at a wavelength of 500 nm. The number of photons that will be emitted per second is
[Given Planck's constant h = 6.6×10^{-34} Js, speed of light c = 3.0×10^8 m/s]
(A) 1×10^{16}
(B) 1.5×10^{16}
(C) 2×10^{16}
(D) 5×10^{15}

25. A coil of self inductance 10 mH and resistance 0.1 Ω is connected through a switch to a battery of internal resistance 0.9 Ω. After the switch is closed the time taken for the current to attain 80% of the saturation values is: [take ln 5 = 1.6]
(A) 0.016 s
(B) 0.324 s
(C) 0.002 s
(D) 0.103 s

26. A submarine experiences a pressure of 5.05×10^6 Pa at a depth of d_1 in a sea. When it goes further to a depth of d_2, it experiences a pressure of 8.08×10^6 Pa. Then $d_2 - d_1$ is approximately (density of water = 10^3 kg/m^3 and acceleration due to gravity = 10 ms^{-2})
(A) 400 m
(B) 500 m
(C) 600 m
(D) 300 m

27. A cubical block of side 0.5 m floats on water with 30% of its volume under water. What is the maximum weight that can be put on the block without fully submerging it under water?
[Take density of water = 10^3 kg/m^3]
(A) 46.3 kg
(B) 65.4 kg
(C) 30.1 kg
(D) 87.5 kg

28. In a Young's double slit experiment the ratio of the slit's width is 4 : 1. The ratio of the intensity of maxima to minima, close to central fringe on the screen will be
(A) $\left(\sqrt{3}+1\right)^4 : 16$
(B) 25 : 9
(C) 9 : 1
(D) 4:1

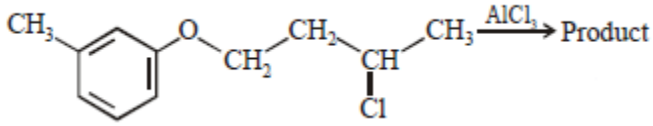
29. A source of sound S is moving with the velocity of 50 m/s towards a stationary observer. The observer measures the frequency of the sound as 1000 Hz. What will be the apparent frequency of the source when it is moving away from the observer after crossing him? (Take velocity of sound in air is 350 m/s)
(A) 1143 Hz
(B) 857 Hz
(C) 750 Hz
(D) 807 Hz

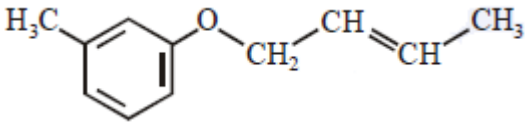
30. A square loop is carrying a steady current I and the magnitude of its magnetic dipole moment is m. If this square loop is changed to a circular loop and it carries the same current, the magnitude of the magnetic dipole moment of circular loop will be
(A) $\frac{m}{\pi}$
(B) $\frac{3m}{\pi}$
(C) $\frac{4m}{\pi}$
(D) $\frac{2m}{\pi}$

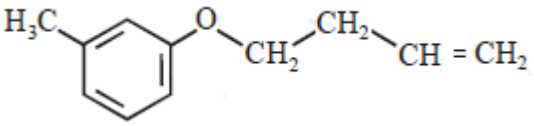
PART –B (CHEMISTRY)

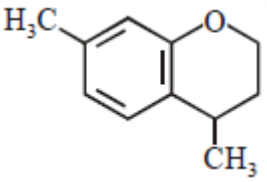
31. The difference between ΔH and ΔU (ΔH - ΔU), when the combustion of one mole of heptane(I) is carried out a temperature T is equal to
(A) -4 RT (B) -3 RT
(C) 3 RT (D) 4 RT

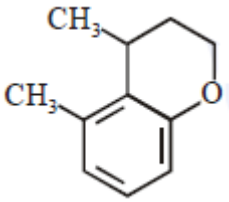
32. The major product obtained in the given reaction is



(A) 

(B) 

(C) 

(D) 

33. The ratio of the shortest wavelength of two spectral series of hydrogen spectrum is found to be about 9. The spectral series are:
(A) Lyman and Paschen (B) Brackett and Pfund
(C) Paschen and Pfund (D) Balmer and Brackett

34. The correct order of the first ionization enthalpies is
(A) Mn < Ti < Zn < Ni (B) Zn < Ni < Mn < Ti
(C) Ti < Mn < Zn < Ni (D) Ti < Mn < Ni < Zn

35. The correct statements among (a) to (b) are:
(a) saline hydrides produce H_2 gas when reacted with H_2O.
(b) reaction of $LiAH_4$ with BF_3 leads to B_2H_6.
(c) PH_3 and CH_4 are electron - rich and electron-precise hydrides, respectively.
(d) HF and CH_4 are called as molecular hydrides.
(A) (c) and (d) only (B) (a), (b) and (c) only
(C) (a), (b), (c) and (d) (D) (a), (c) and (d) only

36. Air pollution that occurs in sunlight is:
(A) oxidising smog (B) acid rain
(C) reducing smog (D) fog

37. For the reaction of H_2 with I_2, the rate constant is 2.5×10^{-4} dm^3 mol^{-1} s^{-1} at 327°C and 1.0 dm^3 mol^{-1} s^{-1} at 527°C. The activation energy for the reaction, in kJ mol^{-1} is:
(R = 8.314 J K^{-1} mol^{-1})
(A) 72 (B) 166
(C) 150 (D) 59

38. In chromatography, which of the following statements is INCORRECT for R_f?

(A) R_f value depends on the type of chromatography.

(B) The value of R_f can not be more than one.

(C) Higher R_f value means higher adsorption.

(D) R_f value is dependent on the mobile phase.

39. A hydrated solid X on heating initially gives a monohydrated compound Y. Y upon heating above 373K leads to an anhydrous whitepowder Z. X and Z, respectively, are:
(A) Washing soda and soda ash.
(B) Washing soda and dead burnt plaster.
(C) Baking soda and dead burnt plaster.
(D) Baking soda and soda ash.

40. The INCORRECT statement is:
(A) the spin-only magnetic moments of $[Fe(H_2O)_6]^{2+}$ and $[Cr(H_2O)_6]^{2+}$ are nearly similar.
(B) the spin-only magnetic moment of $[Ni(NH_3)_4(H_2O)_2]^{2+}$ is 2.83 BM.
(C) the gemstone, ruby, has Cr^{3+} ions occupying the octahedral sites of beryl.
(D) the color of $[CoCl(NH_3)_5]^{2+}$ is violet as it absorbs the yellow light.

41. Which of these factors does not govern the stability of a conformation in acyclic compounds?
(A) Torsional strain
(B) Angle strain
(C) Steric interactions
(D) Electrostatic forces of interaction

42. The correct statement is:
(A) zincite is a carbonate ore
(B) aniline is a froth stabilizer
(C) zone refining process is used for the refining of titanium
(D) sodium cyanide cannot be used in the metallurgy of silver

43. For the reaction,
$2SO_2(g) + O_2(g) \longrightarrow 2SO_3(g)$
$\Delta_H = -57.2$ kJ mol^{-1} and
$K_C = 1.7 \times 10^{16}$
Which of the following statement is INCORRECT?
(A) The equilibrium constant is large suggestive of reaction going to completion and so no catalyst is required.
(B) The equilibrium will shift in forward direction as the pressure increase.
(C) The equilibrium constant decreases as the temperature increases.
(D) The addition of inert gas at constant volume will not affect the equilibrium constant.

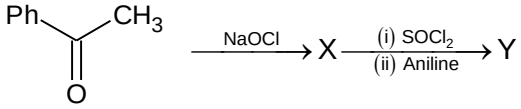
44. The increasing order of nucleophilicity of the following nucleophiles is :
(a) $CH_3CO_2^-$
(b) H_2O
(c) $CH_3SO_3^-$
(d) $\bar{O}H$
(A) (b) < (c) < (a) < (d)
(B) (a) < (d) < (c) < (b)
(C) (d) < (a) < (c) < (b)
(D) (b) < (c) < (d) < (a)

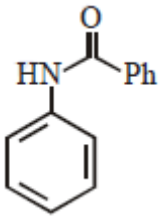
45. The correct match between Item-I and Item-II is:

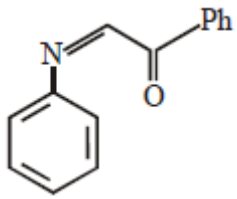
	Item-I		Item-II
(a)	High density polythene	(I)	Peroxide catalyst
(b)	Polyacrylonitrile	(II)	Condensation at high temperature & pressure
(c)	Novolac	(III)	Ziegler-Natta Catalyst
(d)	Nylon 6	(IV)	Acid or base catalyst

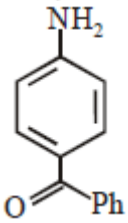
(A) (a) → (III), (b)→(I), (c)→(II), (d)→(IV)
(B) (a)→(IV), (b)→(II), (c)→(I), (d)→(III)
(C) (a)→(II), (b)→(IV), (c)→(I), (d)→(III)
(D) (a)→(III), (b)→(I), (c)→(IV), (d)→(II)

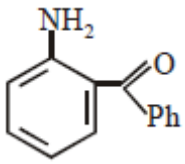
46. The major product 'Y' in the following reaction is:-



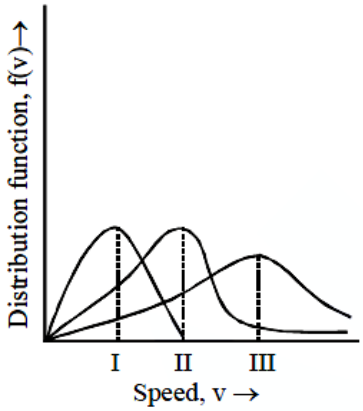
(A) 

(B) 

(C) 

(D) 

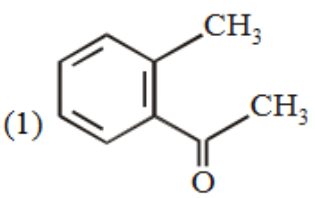
47. Points I, II and III in the following plot respectively correspond to (V_{mp} : most probable velocity)

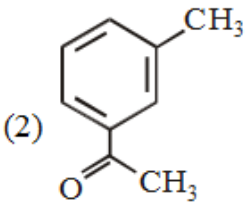


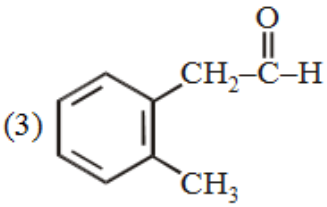
(A) V_{mp} of N_2 (300K); V_{mp} of H_2(300K); V_{mp} of O_2(400K)
(B) V_{mp} of H_2 (300K); V_{mp} of N_2(300K); V_{mp} of O_2(400K)
(C) V_{mp} of O_2 (400K); V_{mp} of N_2(300K); V_{mp} of H_2(300K)
(D) V_{mp} of N_2 (300K); V_{mp} of O_2(400K); V_{mp} of H_2(300K)

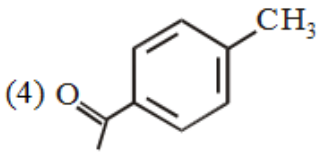
48. The highest possible oxidation states of uranium and plutonium, respectively, are
(A) 6 and 4 (B) 7 and 6
(C) 4 and 6 (D) 6 and 7

49. Compound A ($C_9H_{10}O$) shows positive iodoform test. Oxidation of A with $KMnO_4$/KOH gives acid B($C_8H_6O_4$). Anhydride of B is used for the preparation of phenolphthalein. Compound A is:-

(1) 

(2) 

(3) 

(4) 

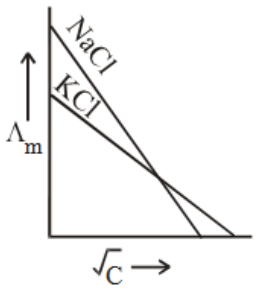
50. The noble gas that does NOT occur in the atmosphere is:
(A) He (B) Ra
(C) Ne (D) Kr

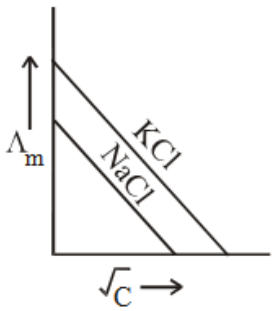
51. The pH of a 0.02 M NH_4Cl solution will be
[given K_b (NH_4OH) = 10^{-5} and log 2 = 0.301]
(A) 2.65 (B) 5.35
(C) 4.35 (D) 4.65

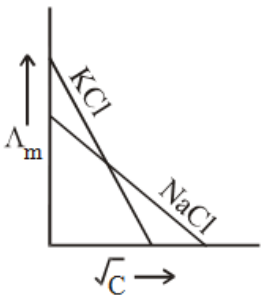
52. The crystal field stabilization energy (CFSE) of $[Fe(H_2O)_6]Cl_2$ and $K_2[NiCl_4]$, respectively, are :-
(A) $-0.4\Delta_o$ and $-0.8\Delta_t$ (B) $-0.4\Delta_o$ and $-1.2\Delta_t$
(C) $-2.4\Delta_o$ and $-1.2\Delta_t$ (D) $-0.6\Delta_o$ and $-0.8\Delta_t$

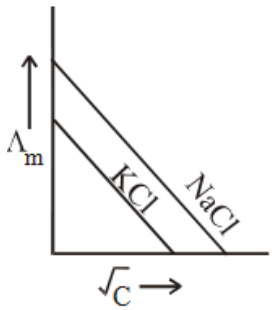
53. The correct option among the following is:
(A) Colloidal particles in lyophobic sols can be precipitated by electrophoresis.
(B) Brownian motion in colloidal solution is faster the viscosity of the solution is very high.
(C) Colloidal medicines are more effective because they have small surface area.
(D) Addition of alum to water makes it unfit for drinking.

54. Which one of the following graphs between molar conductivity (Λ_m) versus $\sqrt{C}$ is correct?

(A) 

(B) 

(C) 

(D) 

55. 1 g of non-volatile non-electrolyte solute is dissolved in 100g of two different solvents A and B whose ebullioscopic constants are in the ratio of 1 : 5. The ratio of the elevation in their boiling points, $\frac{\Delta T_b(A)}{\Delta T_b(B)}$ is:
(A) 5 : 1 (B) 10 : 1
(C) 1 : 5 (D) 1 : 0.2

56. Which of the following is NOT a correct method of the preparation of benzylamine from cyanobenzene ?

(A) (i) HCl/H_2O (ii) $NaBH_4$

(B) (i) $LiAlH_4$ (ii) H_3O^+

(C) (i) $SnCl_2$ + HCl(gas) (ii) $NaBH_4$

(D) H_2/Ni

57. The number of pentagons in C_{60} and trigons (triangles) in white phosphorus, respectively, are:

(A) 12 and 3 (B) 20 and 4

(C) 12 and 4 (D) 20 and 3

58. The minimum amount of $O_2(g)$ consumed per gram of reactant is for the reaction :

(Given atomic mass : Fe = 56, O = 16, Mg = 24, P = 31, C = 12, H = 1)

(A) $C_3H_8(g) + 5O_2(g) \rightarrow 3\,CO_2(g) + 4\,H_2O(l)$

(B) $P_4(s) + 5O_2(g) \rightarrow P_4O_{10}(s)$

(C) $4Fe(s) + 3O_2(g) \rightarrow 2\,Fe_2O_3(s)$

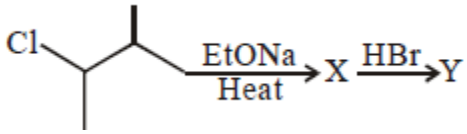
(D) $2\,Mg(s) + O_2(g) \rightarrow 2\,MgO(s)$

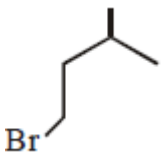
59. Number of stereo centers present in linear and cyclic structures of glucose are respectively

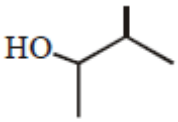
(A) 4 & 5 (B) 5 & 5

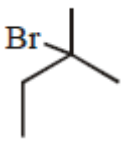
(C) 4 & 4 (D) 5 & 4

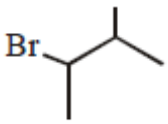
60. The major product 'Y' in the following reaction is:



(A) 

(B) 

(C) 

(D) 

PART–C (MATHEMATICS)

61. If $\lim\limits_{x\to 1}\dfrac{x^2-ax+b}{x-1}=3$, then a + b is equal to

(A) 5 (B) 1
(C) -4 (D) -7

62. The sum of the real roots of the equation
$\begin{vmatrix} x & -6 & -1 \\ 2 & -3x & x-3 \\ -3 & 2x & x=2 \end{vmatrix}=0$ is equal to

(A) -4 (B) 0
(C) 6 (D) 1

63. Lines are drawn parallel to the line 4x – 3y + 2 = 0 at a distance $\dfrac{3}{5}$ from the origin. Then which one of the following points lies on any of these lines?

(A) $\left(-\dfrac{1}{4},\dfrac{2}{3}\right)$ (B) $\left(\dfrac{1}{4},\dfrac{1}{3}\right)$
(C) $\left(\dfrac{1}{4},-\dfrac{1}{3}\right)$ (D) $\left(-\dfrac{1}{4},-\dfrac{2}{3}\right)$

64. If the tangent to the curve $y=\dfrac{x}{x^2-3}, x\in R, \left(x\neq\pm\sqrt{3}\right)$ at a point $(\alpha, \beta)\neq(0, 0)$ on it is parallel to the line 2x + 6y – 11 = 0 then

(A) $|2\alpha+6\beta|=11$ (B) $|2\alpha+6\beta|=19$
(C) $|6\alpha+2\beta|=19$ (D) $|6\alpha+2\beta|=9$

65. The distance of the point having position vector $-\hat{i}+2\hat{j}+6\hat{k}$ from the straight line passing through the point (2, 3, -4) and parallel to the vector $6\hat{i}+3\hat{j}-4\hat{k}$ is

(A) 7 (B) $4\sqrt{3}$
(C) $2\sqrt{13}$ (D) 6

66. If the line ax + y = c, touches both the curves $x^2 + y^2 = 1$ and $y^2-4\sqrt{2}x$, then |c| is equal to

(A) $\dfrac{1}{\sqrt{2}}$ (B) $\sqrt{2}$
(C) $\dfrac{1}{2}$ (D) 2

67. Let $f(x) = \log_e(\sin x)$, $(0 < x < \pi)$ and $g(x) = \sin^{-1}(e^{-x})$, $(x \geq 0)$. If α is a positive real number such that $a = (fog)'(\alpha)$ and $b = (fog)(\alpha)$, then

(A) $a\alpha^2 + b\alpha - a = 2\alpha^2$ (B) $a\alpha^2 - b\alpha - a = 0$
(C) $a\alpha^2 - b\alpha - a = 1$ (D) $a\alpha^2 + b\alpha + a = 0$

68. If 5x + 9 = 0 is the directrix of the hyperbola $16x^2 - 9y^2 = 144$, then its corresponding focus is

(A) (5, 0) (B) $\left(\dfrac{5}{3},0\right)$
(C) (-5, 0) (D) $\left(-\dfrac{5}{3},0\right)$

69. If $\cos^{-1}x - \cos^{-1}\frac{y}{2} = \alpha$, where $-1 \le x \le 1, -2 \le y \le 2, x \le \frac{y}{2}$, then for all x, y, $4x^2 - 4xy\cos\alpha + y^2$ is equal to

(A) $4\sin^2\alpha - 2x^2y^2$ (B) $4\cos^2\alpha + 2x^2y^2$

(C) $2\sin^2\alpha$ (D) $4\sin^2\alpha$

70. The locus of the centres of the circles, which touch the circle, $x^2 + y^2 = 1$ externally, also touch the y-axis and lie in the first quadrant is

(A) $x = \sqrt{1+2y}, y \ge 0$ (B) $y = \sqrt{1+4x}, x \ge 0$

(C) $x = \sqrt{1+4y}, y \ge 0$ (D) $y = \sqrt{1+2x}, x \ge 0$

71. Let $a_1, a_2, a_3, \ldots\ldots$ be and A.P with $a_6 = 2$. Then the common difference of this A.P., which maximizes the product $a_1a_4a_5$ is

(A) $\frac{3}{2}$ (B) $\frac{8}{5}$

(C) $\frac{2}{3}$ (D) $\frac{6}{5}$

72. The smallest natural number n, such that the coefficient of x in the expansion of $\left(x^2 + \frac{1}{x^3}\right)^n$ is ${}^nC_{23}$ is

(A) 38 (B) 58

(C) 23 (D) 35

73. Suppose that 20 pillars of the same height have been erected along the boundary of a circular stadium. If the top of each pillar has been connected by beams with the top of all its non-adjacent pillars, then the total number of beams is

(A) 210 (B) 180

(C) 170 (D) 190

74. A spherical iron ball of radius 10 cm is coated with a layer of ice of uniform thickness that melts at a rate of 50 cm^3/min. When the thickness of the ice is 5 cm, then the rate at which the thickness (in cm/min) of ice decreases is

(A) $\frac{1}{36\pi}$ (B) $\frac{5}{6\pi}$

(C) $\frac{1}{9\pi}$ (D) $\frac{1}{18\pi}$

75. If both the means and the standard deviation of 50 observations $x_1, x_2, \ldots\ldots, x_{50}$ are equal to 16, then the mean of $(x_1 - 4)^2, (x_2 - 4)^2, \ldots, (x_{50} - 4)^2$ is

(A) 400 (B) 380

(C) 525 (D) 480

76. The number of real roots of the equation $5 + |2^x - 1| = 2^x(2^x - 2)$ is

(A) 4 (B) 3

(C) 2 (D) 1

77. The tangent and normal to the ellipse $3x^2 + 5y^2 = 32$ at the point P(2, 2) meet the x-axis at Q and R, respectively. Then the area(in sq. units) of the triangle PQR is

(A) $\frac{34}{15}$ (B) $\frac{68}{15}$

(C) $\frac{14}{3}$ (D) $\frac{16}{3}$

78. A perpendicular is drawn from a point on the line $\frac{x-1}{2}=\frac{y+1}{-1}=\frac{z}{1}$ to the plane x + y + z = 3 such that the foot of the perpendicular Q also lies on the plane x – y + z = 3. Then the co-ordinates of Q are

(A) (2, 0, 1) (B) (-1, 0, 4)
(C) (1, 0, 2) (D) (4, 0, -1)

79. The integral $\int_{\pi/6}^{\pi/3}\sec^{2/3}x\,\mathrm{cosec}^{4/3}x\,dx$ is equal to

(A) $3^{5/6}-3^{2/3}$ (B) $3^{5/3}-3^{1/3}$
(C) $3^{7/6}-3^{5/6}$ (D) $3^{4/3}-3^{1/3}$

80. The angles A, B and C of a triangle ABC are in A.P and a : b = 1 : $\sqrt{3}$. If c = 4 cm, then the area (in sq. cm) of this triangle is

(A) $2\sqrt{3}$ (B) $\frac{4}{\sqrt{3}}$
(C) $4\sqrt{3}$ (D) $\frac{2}{\sqrt{3}}$

81. Let a, b and c be in G.P with common ratio r, where $a \neq 0$ and $0 < r \leq \frac{1}{2}$. If 3a, 7b and 15c are the first three terms of an A.P., then the 4th term of this A.P is

(A) $\frac{2}{3}a$ (B) $\frac{7}{3}a$
(C) 5a (D) a

82. Let y = y(x) be the solution of the differential equation $\frac{dy}{dx}+y\tan x=2x+x^2\tan x,\ x\in\left(-\frac{\pi}{2},\frac{\pi}{2}\right)$, such that y(0) = 1. Then

(A) $y'\left(\frac{\pi}{4}\right)+y'\left(\frac{-\pi}{4}\right)=-\sqrt{2}$ (B) $y'\left(\frac{\pi}{4}\right)-y'\left(\frac{-\pi}{4}\right)=\pi-2$
(C) $y\left(\frac{\pi}{4}\right)-y\left(-\frac{\pi}{4}\right)=\sqrt{2}$ (D) $y\left(\frac{\pi}{4}\right)+y\left(-\frac{\pi}{4}\right)=\frac{\pi^2}{2}+2$

83. If the plane 2x – y + 2z + 3 = 0 has the distances $\frac{1}{3}$ and $\frac{2}{3}$ units from the planes 4x – 2y + 4z + λ = 0 and 2x – y + 2z + μ = 0, respectively, then the maximum value of $\lambda+\mu$ us equal to

(A) 15 (B) 13
(C) 5 (D) 9

84. The area(in sq. units) of the region bounded by the curves $y = 2^x$ and y = |x +1| in the first quadrant is

(A) $\frac{3}{2}$ (B) $\log_e 2+\frac{3}{2}$
(C) $\frac{3}{2}-\frac{1}{\log_e 2}$ (D) $\frac{1}{2}$

85. Let λ be a real number for which the system of linear equations
x + y + z = 6
4x + λy - λz = λ - 2
3x + 2y – 4z = -5
Has indefinitely many solutions. Then λ is a root of the quadratic equation

(A) $\lambda^2 - \lambda - 6 = 0$ (B) $\lambda^2 - 3\lambda - 4 = 0$
(C) $\lambda^2 + 3\lambda - 4 = 0$ (D) $\lambda^2 + \lambda - 6 = 0$

86. The sum $1+\frac{1^3+2^3}{1+2}+\frac{1^3+2^3+3^3}{1+2+3}+.....+\frac{1^3+2^3+3^3+.....+15^3}{1+2+3+.....+15}-\frac{1}{2}(1+2+3+.....+15)$ is equal to

(A) 620
(B) 1860
(C) 1240
(D) 660

87. Minimum number of times a fair coin must be tossed so that the probability of getting at least one head is more than 99% is

(A) 8
(B) 6
(C) 7
(D) 5

88. The negation of the Boolean expression $\sim s\vee(\sim r\wedge s)$ is equivalent to

(A) $s\vee r$
(B) $\sim s\wedge\sim r$
(C) r
(D) $s\wedge r$

89. If $\int x^5e^{-x^2}dx=g(x)e^{-x^2}+c$, where c is a constant of integration, then g(-1) is equal to

(A) -1
(B) 1
(C) $-\frac{5}{2}$
(D) $-\frac{1}{2}$

90. If z and w are two complex numbers such that |zw| = 1 and arg(z) – arg(w) = $\frac{\pi}{2}$, then

(A) $\bar{z}w=i$
(B) $z\bar{w}=\frac{-1+i}{\sqrt{2}}$
(C) $z\bar{w}=\frac{1-i}{\sqrt{2}}$
(D) $\bar{z}w=-i$

JEE (Mains) – 2019

ANSWERS

PART A – PHYSICS

1.	**D**	2.	**D**	3.	**A**	4.	**None**
5.	**C**	6.	**A**	7.	**B**	8.	**D**
9.	**C**	10.	**D**	11.	**B**	12.	**B**
13.	**A**	14.	**D**	15.	**B**	16.	**C**
17.	**A**	18.	**B**	19.	**D**	20.	**A**
21.	**D**	22.	**D**	23.	**None**	24.	**D**
25.	**A**	26.	**D**	27.	**D**	28.	**C**
29.	**C**	30.	**C**				

PART B – CHEMISTRY

31.	**A**	32.	**C**	33.	**A**	34.	**D**
35.	**C**	36.	**A**	37.	**B**	38.	**C**
39.	**A**	40.	**C**	41.	**B**	42.	**B**
43.	**A**	44.	**A**	45.	**D**	46.	**A**
47.	**D**	48.	**D**	49.	**A**	50.	**C**
51.	**B**	52.	**A**	53.	**A**	54.	**B**
55.	**C**	56.	**A**	57.	**C**	58.	**C**
59.	**A**	60.	**C**				

PART C – MATHEMATICS

61.	**D**	62.	**B**	63.	**A**	64.	**C**
65.	**A**	66.	**B**	67.	**C**	68.	**C**
69.	**D**	70.	**D**	71.	**B**	72.	**A**
73.	**C**	74.	**D**	75.	**A**	76.	**D**
77.	**B**	78.	**A**	79.	**C**	80.	**A**
81.	**D**	82.	**B**	83.	**B**	84.	**C**
85.	**A**	86.	**A**	87.	**C**	88.	**D**
89.	**C**	90.	**D**				

HINTS AND SOLUTIONS

PART A – PHYSICS

1. n = 1 mole

$$P = P_o\left\{1-\frac{1}{2}\left(\frac{V_o}{V}\right)^2\right\} \quad ; \quad PV = nRT = RT$$

$$P = \frac{RT}{V}$$

$$\frac{RT}{V} = P_o\left\{1-\frac{V_o^2}{2V^2}\right\}$$

$$T = \frac{P_oV}{R}\left\{1-\frac{V^2}{2V^2}\right\} = \frac{P_o}{R}\left\{V-\frac{V_o^2}{2V^2}\right\}$$

$$\Delta T = \frac{P_o}{R}\left\{(2V_o - V_o) - \frac{V_o^2}{2}\left(\frac{1}{2V_o}-\frac{1}{V_o}\right)\right\}$$

$$= \frac{P_o}{R}\left\{V_o - \frac{V_o^2}{2}\right\}$$

$$\Delta T = \frac{P_o}{R}\left\{(2V_o - V_o) - \frac{V_o^2}{2}\left(\frac{1}{2V_o}-\frac{1}{V_o}\right)\right\}$$

$$= \frac{P_o}{R}\left\{V_o - \frac{V_o^2(1-2)}{2\times 2V_o}\right\}$$

$$= \frac{P_o}{R}\left\{V_o - \frac{V_o}{4}\right\} = \frac{3}{4}\frac{P_oV_o}{R}$$

2. $$I_1 = \frac{\left(\frac{7M}{8}\right)(ZR)^2}{2} = \frac{7M\times 4R^2}{2\times 8} = \frac{7MR^2}{4}$$

$$I_2 = \frac{2}{5}\frac{M}{8}\left(\frac{R}{2}\right)^2 = \frac{2M}{5\times 8}\frac{R^2}{4} = \frac{MR^2}{80}$$

$$\frac{I_1}{I_2} = \frac{7MR^2\times 80}{4MR^2} = 140$$

3. By looking into graph.

4. ℓ = 1 M

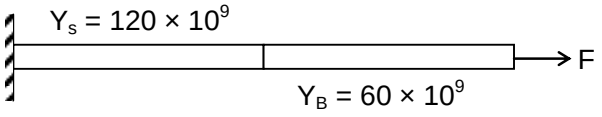
$A = 10^{-6}\ M^2$

$$\text{Stress} = \frac{F}{A} \qquad Y_S = 120\times 10^9$$

$$\text{Stress} = \frac{\text{Stress}}{Y}$$

$$\Delta\ell = \frac{\ell\times F}{AY}$$

$$\Delta\ell_1 + \Delta\ell_2 = \frac{\ell_1 F}{AY_1} + \frac{\ell_2 F}{AY_2} = 0.2\times 10^{-3}$$



$$\frac{F}{A} = \frac{0.2\times10^{-3}}{\frac{\ell}{Y_1}+\frac{\ell}{Y_2}}$$

$$= \frac{0.2\times10^{-3}}{\frac{1}{120\times10^9}+\frac{1}{60\times10^9}} = \frac{0.2\times10^{-3}\times10^9\times120}{1+2}$$

$$= \frac{0.2\times10^6\times120}{3} = 8\times10^6$$

5. $Q = C_V\Delta T$

$Q' = C_P\Delta T$

$$Q' = \frac{C_P}{C_V}Q = \left(1+\frac{2}{5}\right)Q = \frac{7}{5}Q$$

6. $2.5\times10^{-2}\times0.2 = \frac{1}{2}\times20\times10^{-3}\left\{-V^2+1^2\right\}$

$5\times10^{-3} = 10\times10^{-3}(1-V^2)$

$1-V^2 = \frac{1}{2}$; $V^2 = \frac{1}{2}$; $V = \frac{1}{\sqrt{2}} = 0.7$

7. $$\frac{400}{\frac{\pi}{4}d^2} = 379\times10^6$$

$$d^2 = \frac{4\times400\times10^{-6}}{\pi\times379} = 0.336\times10^{-6}\times4$$

$$d = 2\sqrt{0.336}\times10^{-3}\ M \simeq 1.16\ mm$$

8. $$T = \frac{2u\sin\theta}{g\cos\alpha}$$

$$R = u\cos\theta\, T - \frac{1}{2}g\sin\alpha\, T^2$$

$$= \frac{u\cos\theta\, 2u\sin\theta}{g\cos\alpha} - \frac{g\sin\alpha}{2}\frac{4u^2\sin^2\theta}{g^2\cos^2\alpha}$$

$$= \frac{u^2\sin^2\theta}{g\cos\alpha} - \frac{u^2\sin\alpha}{g\cos^2\alpha}\{1-\cos2\theta\}$$

$$= \frac{4\times\frac{1}{2}}{10\times\frac{\sqrt{3}}{2}} - \frac{u^2\sin\alpha}{g\cos^2\alpha}\left\{1-\frac{\sqrt{3}}{2}\right\}$$

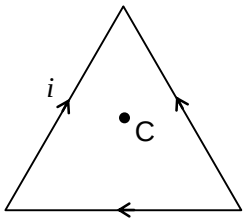
$$= \frac{4}{10\sqrt{3}} - \frac{8}{30}\left\{1-\frac{\sqrt{3}}{2}\right\}$$

$$= \frac{4}{5\sqrt{3}} - \frac{8}{30} = \frac{8\sqrt{3}-8}{30} = \frac{8(\sqrt{3}-1)}{30} = 20\ cm$$

9. $i = 10$ A

$\ell = 1$ m

$\mu_o = 4\pi \times 10^{-7} \ \frac{N}{A^2}$



$$B = \frac{\frac{\mu_o i}{4\pi\sqrt{3}\,\ell}}{2} \times 3$$

$$= \frac{\mu_o i\sqrt{3}}{2\pi\ell} = \frac{4\pi\times10^{-7}\times10\times\sqrt{3}}{2\pi\times1} = 20\sqrt{3}\times10^{-7}$$

$= 3\ \mu T$

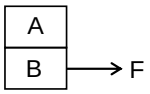
10. $$\frac{1}{e^2} = e^{\lambda t - 5\lambda t}$$

$$t = \frac{1}{2\lambda}$$

11. $M_A = 1$ kg, $M_B = 3$ kg

$\mu_{AB} = 0.2$

$\mu_B = 0.2$



$F_{max} = (M_A + M_B) \times 0.2 \times 10 + (M_A + M_B) \times 0.2 \times 10$

$= 4 \times 2 + 4 \times 2 = 16$

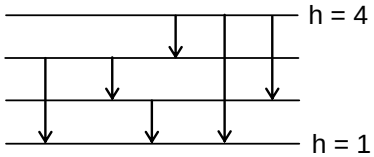
12. $X = 5YZ^2$

$Y = \frac{X}{5Z^2} = M^{-3} L^{-2} T^8 A^4$

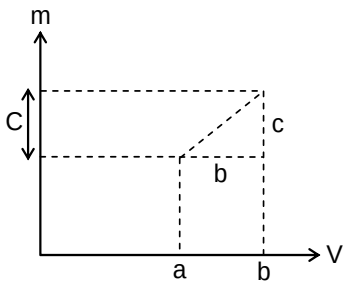
13. $$\frac{hc}{\lambda} = 13.6 \text{ eV(g)} \left\{1 - \frac{1}{16}\right\}$$

$$\frac{1240 \text{ eV}}{\lambda} = \frac{15}{16} \times 9 \times 13.6 \text{ eV}$$

$$\lambda = \frac{1240\times16}{15\times9\times13.6} = 10.8 \text{ nm}$$



14. $$f = \frac{b}{c}$$



15. $$\frac{mV^2}{r} = \frac{GMm}{r^2}$$

$$V = \sqrt{\frac{GM}{r}}$$

$$n = \frac{VT}{2\pi r} = \sqrt{\frac{GM}{r}}\ \frac{T}{2\pi r}$$

$$= \left(\sqrt{\frac{GM}{r^3}}\right) \times \frac{T}{2\pi} = \sqrt{\frac{6.67\times10^{-11}\times8\times10^{22}}{(202\times10^4)^3}} \times \frac{T}{2\pi}$$

$$= \frac{24\times3600}{2\times3.14}\sqrt{\frac{6.67\times8\times10^{11}}{(202)^3\times10^{12}}} = \frac{24\times3600}{2\times3.14\times1242.8} = \frac{24\times3600}{78.51} \simeq 11$$

16. $I = 25\dfrac{W}{cm^2} = 25\times10^4\ W/m^2$

$P = 25 \times 25$; $W = 625$ W

$$\frac{hc}{\lambda}\frac{dn}{dt} = P$$

$$F = \frac{h}{\lambda}\frac{dn}{dt} = \frac{P}{C} = \frac{625}{3\times10^8}$$

Momentum = $\dfrac{625\times40\times60}{3\times10^8} = 5 \times 10^{-3}$ Ns

17. $\vec{v} = 2\hat{i} - 6 + \hat{j}$

At t = 2

$\vec{v} = 2\hat{i} - 12\hat{j}$

$\vec{P} = m\vec{v} = 4i - 24\hat{j}$

At t = 2

$\vec{r} = 4\hat{i} - 12\hat{j}$

$$\vec{L} = \vec{r}\times\vec{P} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 4 & -12 & 0 \\ 4 & -24 & 0 \end{vmatrix}$$

$$= \{4(-24) + 4\times12\}\,\hat{k}$$

$$= (-96 + 48)\,\hat{k}$$

$$= (-)\,48\,\hat{k}$$

18. $10^{-4}\times1 = \sqrt{(1)^2 + 2\times10\times0.15}\times A$

$A = \dfrac{10^{-4}}{2} = 5 \times 10^{-5}$

19. $$R = \int_a^b \frac{\rho\,dx}{4\pi x^2}$$

$$= \frac{\rho}{4\pi}\left(\frac{1}{a} - \frac{1}{b}\right)$$

20. $m = 5 \times 10^{-3}$ kg, $r = 10^{-2}$ m

$\omega = 25 \times 2\pi$ rad/5

$= 50\ \pi$ rad/sec

$$\omega = \frac{\tau}{I}t$$

$$\tau = \frac{I\omega}{t} = \frac{5mr^2}{4}\times\frac{\omega}{t}$$

$$= \frac{5\times5\times10^{-3}\times10^{-4}\times50\,\pi}{4\times5}$$

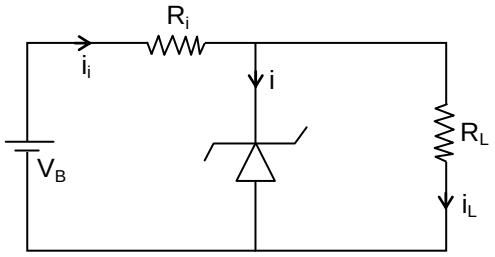
$$= \frac{25\pi}{4}\times10^{-6} = 2 \times 10^{-5}$$

21. $V_{breakdwon} = 6V,\ R_L = 4k\Omega,\ R_i = 1\ k\Omega$

$i_L = \frac{6}{4}\times10^{-3} = 1.5\times10^{-3}$ = 1.5 mA

$i_i = 2 \times 10^{-3}$

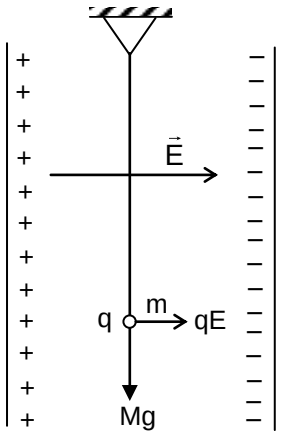
$i = i_1 - i_L = 0.5$ mA – minimum current



$i_i = 10 \times 10^{-3} = 10$ mA

$i_{max} = 8.5$ mA

22. $T = 2\pi\sqrt{\frac{L}{\sqrt{g^2 + \frac{q^2E^2}{M^2}}}}$



23. $q_A = 1\ \mu c$; $q_B = 1\ \mu c$, $m_B = 4 \times 10^{-9}$ kg, $r_{AB} = 10^{-3}$ m

$$\frac{1}{2}M_B V^2 = k\, q_A q_B \left\{\frac{1}{10^{-3}} - \frac{1}{9\times10^{-3}}\right\}$$

$$\frac{1}{2}4\times10^{-9}V^2 = 9\times10^9\times10^{-6}\times10^{-6}\times\frac{8}{9}\times10^3$$

$$V^2 = \frac{8}{2}\times10^9 = 4\times10^9$$

24. $2\times10^{-3} = \frac{hc}{\lambda}\frac{dn}{dt}$

$$\frac{dn}{dt} = \frac{2\times10^{-3}\lambda}{hc}$$

$$= \frac{2\times10^{-3}\times500\times10^{-9}}{6.6\times10^{-34}\times3\times10^8}$$

$$= \frac{1000}{6.6\times3}\times10^{14} = 5 \times 10^{15}$$

25. $L = 10 \times 10^{-3}$ H, $r_1 = 0.1\ \Omega$

$i = \varepsilon\left\{1 - e^{-t/2}\right\}$

$i_{saturation} = \varepsilon$

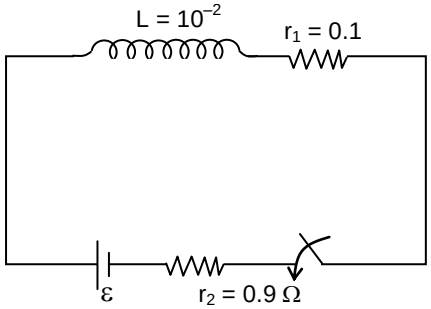
80% $i_{saturation} = 0.8\ \varepsilon$

$0.8\ \varepsilon = \varepsilon\left\{1 - e^{-t/2}\right\}$

$0.8 = 1 - e^{-t/2}$; $e^{-t/2} = 0.2$

$e^{t/L} = 5$

$t = L \ln 5 = 10 \times 10^{-3} \times 1.6 = 16 \times 10^{-3}$

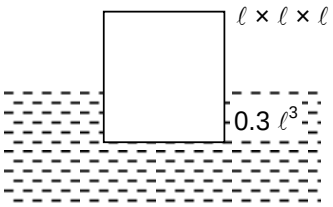


26. $P_1 = 5.05 \times 10^6$; $P_2 = 8.08 \times 10^6$

$P_2 - P_1 = \rho g(d_2 - d_1)$

$d_2 - d_1 = \dfrac{3.03\times10^6}{10^3\times10} = 3.03 \times 10^2 = 303$

27. $0.3\ \ell^3\ \rho_\omega = \ell^3\ \rho$



$\rho = 300\dfrac{kg}{m^3}$

$m + \ell^3\rho = \ell^3\rho_\omega$

$M = \ell^3(\rho_w - \rho) = (5)^3\ \{1000 - 300\} = 700 \times (5)^3$

$= 87.5$ kg

28. $\dfrac{I_{Max}}{I_{Min}} = \dfrac{9}{1}$

29. $f_a = \dfrac{V}{V - V_s} f_o = 1000$ Hz

S ⟶ V = 50 m/s

$f_a' = \dfrac{V}{V + V_s} f_o$

$\dfrac{f_a'}{f_a} = \dfrac{V - V_s}{V + V_s} = \dfrac{350 - 50}{350 + 50} = \dfrac{300}{400} = \dfrac{3}{4}$

$f_a' = \dfrac{3}{4}\times1000 = 750$ Hz

30. $m = I\ell^2$ $\qquad$ $2\pi r = 4\ell$

$m' = \dfrac{I4\ell^2}{\pi}$ $\qquad$ $r = \dfrac{2\ell}{\pi}$

$\dfrac{m'}{m} = \dfrac{4}{\pi}$ $\qquad$ $\pi r^2 = \dfrac{\pi 4\ell^2}{\pi^2} = \dfrac{4\ell^2}{\pi}$

$m' = \dfrac{4}{\pi}m$

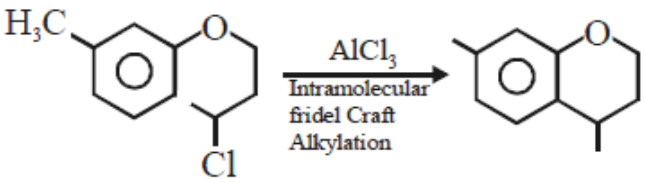
PART B – CHEMISTRY

31. $C_7H_{16}(\ell) + 11O_2(g) \longrightarrow 7CO_2(g) + 8H_2O(\ell)$

$\Delta n_g = n_p - n_r = 7 - 11 = -4$

$\because \Delta H = \Delta U + \Delta n_g RT$

$\therefore \Delta H - \Delta U = -4\ RT$

32. 

33. $$\frac{\frac{1}{\lambda_2} = R_H\left(\frac{1}{n_1^2} - \frac{1}{n_2^2}\right)Z^2}{\frac{1}{\lambda_1} = R_H\left(\frac{1}{n_1^1} - \frac{1}{n_2^1}\right)Z^2}$$

As for shortest wavelength both n_1 and n_2^1 are ∞

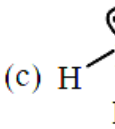
$$\therefore \frac{\lambda_1}{\lambda_2} = \frac{9}{1} = \frac{n_1^1}{n_1^2}$$

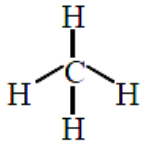
Now if $n_1^1 = 3$ and n_1 is 1 it will justify the statement hence Lyman and Paschen is correct.

34. As Zn is fully filled and left to right in group IP increases.

35. (a) $\underset{\text{Ionic hydride}}{\overset{\oplus\ \ominus}{M}H} + HOH \longrightarrow MOH + H_2$

(b) $4BF_3 + 3LiAlH_4 \longrightarrow 2B_2H_6 + 3LiF + 3AlF_3$

(c)  → phosphorous is electron rich hydride due to presence of lone pair

 → It is electron precise hydride.

(d) HF & CH_4 are molecular hydride due to they are covalent molecules.

36. Fact based

37. $H_2(g) + I_2(g) \rightarrow 2HI(g)$

Apply Arrhenius equation

$$\log\frac{K_2}{K_1} = \frac{E_a}{2.303R}\left(\frac{1}{600} - \frac{1}{800}\right)$$

$$\log\frac{1}{2.5\times10^{-4}} = \frac{E_a}{2.303\times8.31}\left(\frac{200}{600\times800}\right)$$

$\therefore\ E_a \approx 166 kJ/mol$

38. R_f value can't measure the extent of adsorption.

39. $Na_2CO_3.10H_2O(s) \xrightarrow{\Delta} Na_2CO_3.H_2O$

washing soda (X) → (Y)

(Y) $\xrightarrow{\Delta,\ T > 373k}$ Na_2CO_3 (soda ash) (Z)

40. In gemstone, ruby has Cr^{3+} ion occupying the octahedral sites of aluminium oxide (Al_2O_3) normally occupied by Al^{3+}ion.

41. Angle strain govern stability in cyclic compound.

42. Fact based.

43. In option (B)- Δn_g is –ve therefore increase in pressure will bring reaction in forward direction.
In option (C)- as the reaction is exothermic therefore increase in temperature will decrease the equilibrium constant.
In option (D)- Equilibrium constant changes only with temperature. Hence, option (B), (C) and (D) are correct therefore option (1) is incorrect choice.

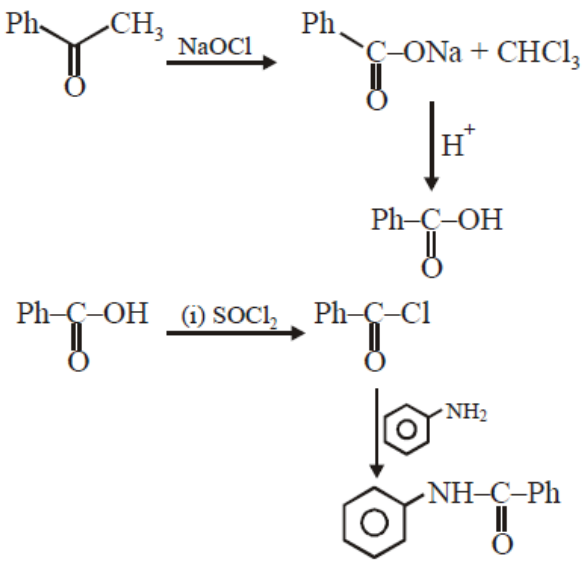
44. $\underbrace{\bar{O}H > CH_3-\overset{\overset{O}{\|}}{C}-O^- > CH_3-\overset{\overset{O}{\|}}{\underset{\underset{O}{\|}}{S}}-O^-}_{\text{Charged ion}} > \underbrace{H_2O}_{\text{neutral system}}$

ione pair donating tendency on oxygen is reduced, nucleophilicity reduced b < c < a < d

45

(a)	High density	(III)	Ziegler-Natta Catalyst
(b)	Polyacrylonitrile	(I)	Peroxide catalyst
(c)	Novolac	(IV)	Acid or base catalyst
(d)	Nylon 6	(II)	Condensation at high temperature & pressure

46.



47.

$$V_{mp} = \sqrt{\frac{2RT}{M}} \Rightarrow V_{mp} \propto \sqrt{\frac{T}{M}}$$

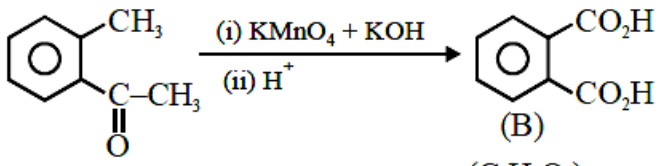
For N_2, O_2, H_2

$$\sqrt{\frac{300}{28}} < \sqrt{\frac{400}{32}} < \sqrt{\frac{300}{2}}$$

$$V_{mp} \text{ of } N_2(300K) < V_{mp} \text{ of } O_2(400K) < V_{mp} \text{ of } H_2(300K)$$

48. The highest oxidation state of U and Pu is 6+ and 7+ respectively.

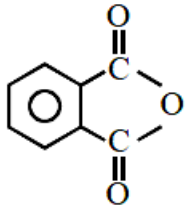
49.



(B)

$(C_8H_6O_4)$ Phthalic acid

+ve iodoform test



Phthalic anhydride

is used for prepareation of phenolphthalein indicator

50. Fact based.

51. For the salt of strong acid and weak base

$$H^+ = \sqrt{\frac{K_w \times C}{K_b}}$$

$$\left[H^+\right] = \sqrt{\frac{10^{-14} \times 2 \times 10^{-2}}{10^{-5}}}$$

$$-\log\left[H^+\right] = 6 - \frac{1}{2}\log 20$$

$$\therefore \quad pH = 5.35$$

52. CFSE = $[-0.4n_{t2g} + 0.6\, n_{eg}]\, \Delta_o$

53. In electrophoresis precipitation occurs at the electrode which is oppositely charged therefore (A) is correct.

54. Both NaCl and KCl are strong electrolytes and as Na^+(aq.) has less conductance than K^+ (aq.) due to more hydration therefore the graph of option (B) is correct.

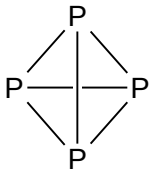
55. $$\Delta T_b = K_b \times m$$

$$\therefore \quad \frac{\Delta T_{b(A)}}{\Delta T_{b(B)}} = \frac{K_{b(A)}}{K_{b(B)}} \text{ as } m_A = m_B$$

$$\therefore \quad \frac{\Delta T_{b(A)}}{\Delta T_{b(B)}} = \frac{1}{5}$$

56. Benzylamine will not give cyanobenzene with HCl/H_2O & $NaBH_4$.

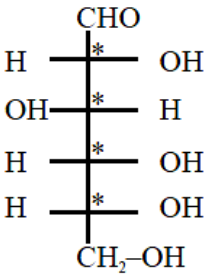
57. Refer structure of C_{60} & P_4



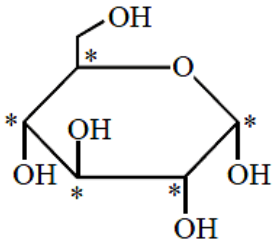
58. 4 mol of Fe require 3×32 gram

$\frac{1}{56}$ mol of Fe require $= \frac{3 \times 32}{4} \times \frac{1}{56} = 0.428$ g

59.



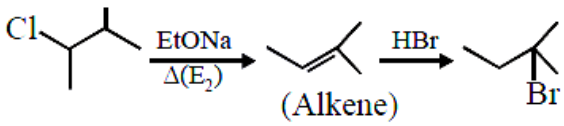
D–Glucose
(Linear structure)



α-D–Glucose
(cyclic structure)

∗ :- Stereocenter

60.



(Alkene)
(Saytzeff prod.)

PART C – MATHEMATICS

61. $\lim\limits_{x\to1}\dfrac{x^2-ax+b}{x-1}=5$

$1-a+b=0$ ……..(i)

$2-a=5$. ……..(ii)

$\Rightarrow a+b=-7$

62. By expansion, we get

$-5x^3+30x-30+5x=0$

$\Rightarrow -5x^3+35x-30=0$

$\Rightarrow x^3-7x+6=0$, All roots area real

So, sum of roots = 0

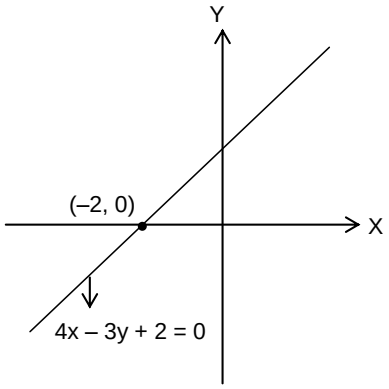
63. Required line is $4x-3y+\lambda=0$

$\left|\dfrac{\lambda}{5}\right|=\dfrac{3}{5}$

$\Rightarrow \lambda=\pm3$

So, required equation of line is $4x-3y+3=0$ and $4x-3y-3=0$

(1) $4\left(-\dfrac{1}{4}\right)-3\left(\dfrac{2}{3}\right)+3=0$



64. $\left.\dfrac{dy}{dx}\right|_{(\alpha,\beta)}=\dfrac{-\alpha^2-3}{\left(\alpha^2-3\right)^2}$

Given that :

$\dfrac{-\alpha^2-3}{\left(\alpha^2-3\right)^2}=-\dfrac{1}{3}$

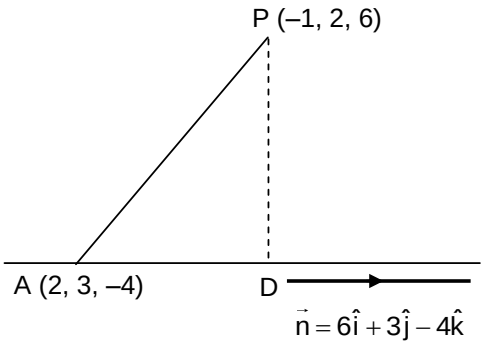
$\Rightarrow \alpha=0,\pm3 \qquad (\alpha\neq0)$

$\Rightarrow \beta=\pm\dfrac{1}{2}. \qquad (\beta\neq0)$

$|6\alpha+2\beta|=19$

65. $AD=\left|\dfrac{\overrightarrow{AP}.\vec{n}}{|\vec{n}|}\right|=\sqrt{61}$

$\Rightarrow PD=\sqrt{AP^2-AD^2}=\sqrt{110-61}=7$



66. Tangent to $y^2=4\sqrt{2}x$ is $y=mx+\dfrac{\sqrt{2}}{m}$ it is also tangent to $x^2+y^2=1$

$\Rightarrow \left|\dfrac{\sqrt{2}/m}{\sqrt{1+m^2}}\right|=1\Rightarrow m=\pm1$

$\Rightarrow$ Tangent will be $y=x+\sqrt{2}$ or $y=-x-\sqrt{2}$ compare with $y=-ax+C$

$\Rightarrow a=\pm1$ and $C=\pm\sqrt{2}$

67. $fog(x) = (-x) \Rightarrow (fg(\alpha)) = -\alpha = b$

$(fg(x))' = -1 \Rightarrow (fg(\alpha))' = -1 = a$

68. $\frac{x^2}{9} - \frac{y^2}{16} = 1$

$a = 3, b = 4$ and $e = \sqrt{1 + \frac{16}{9}} = \frac{5}{3}$

corresponding focus will be (–ae, 0) i.e. $(-5, 0)$.

69. $\cos^{-1} x - \cos^{-1} \frac{y}{2} = \alpha$

$\cos\left(\cos^{-1} x - \cos^{-1} \frac{y}{2}\right) = \cos\alpha$

$\Rightarrow x \times \frac{y}{2} + \sqrt{1-x^2}\sqrt{1-\frac{y^2}{4}} = \cos\alpha$

$\Rightarrow \left(\cos\alpha - \frac{xy}{2}\right)^2 = (1-x^2)\left(1-\frac{y^2}{4}\right)$

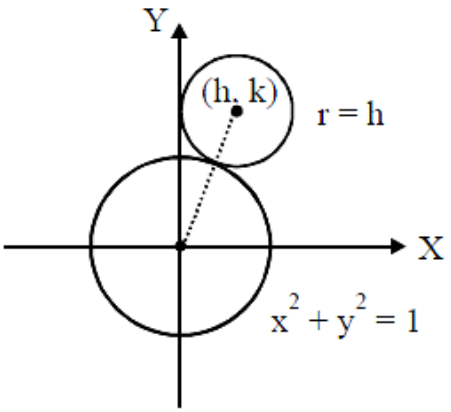
$x^2 + \frac{y^2}{4} - xy\cos\alpha = 1 - \cos^2\alpha = \sin^2\alpha$

70. $\sqrt{h^2 + k^2} = |h| + 1$

$\Rightarrow x^2 + y^2 = x^2 + 1 + 2x$

$\Rightarrow y^2 = 1 + 2x$

$\Rightarrow y = \sqrt{1+2x};\ x \geq 0$



71. Let a is first term and d is common difference then, $a + 5d = 2$ (given) ……(1)

$f(d) = (2-5d)(2-2d)(2-d)$

$f'(x) = 0 \Rightarrow d = \frac{2}{3}, \frac{8}{5}$

$f''(d) < 0$ at $d = \frac{8}{5}$

$\Rightarrow d = \frac{8}{5}$

72. $T_{r+1} = \sum_{r=0}^{n} {}^nC_r\, x^{2n-2r}.x^{-3r}$

$2n - 5r = 1 \Rightarrow 2n = 5r + 1$ for $r = 15, n = 38$ smallest value of n is 38.

73. Total cases = number of diagonals in 20 sided polygon.

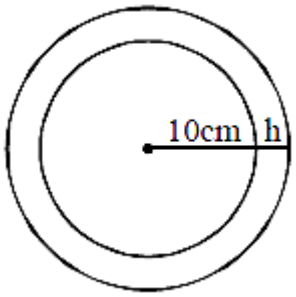
$= {}^{20}C_2 - 20 = 170$

74. $V=\frac{4}{3}\pi\left((10+h)^3-10^3\right)$

$\frac{dV}{dt}=4\pi(10+h)^2\frac{dh}{dt}$

$-50=4\pi(10+5)^2\frac{dh}{dt}$

$\Rightarrow\frac{dh}{dt}=-\frac{1}{18\pi}\frac{cm}{min}$



e

75. Mean $(\mu)=\frac{\sum x_i}{50}=16$

Standard deviation $(\sigma)=\sqrt{\frac{\sum_i^2}{50}-(\mu)^2}=16$

$\Rightarrow(256)\times2=\frac{\sum x_i^2}{50}$

$\Rightarrow$ New mean

$=\frac{\sum(x_i-4)^2}{50}=\frac{\sum x_i^2+16\times50-8\sum x_i}{50}$

$=(256)\times2+16-8\times16=400$

76. Let $2^x=t$

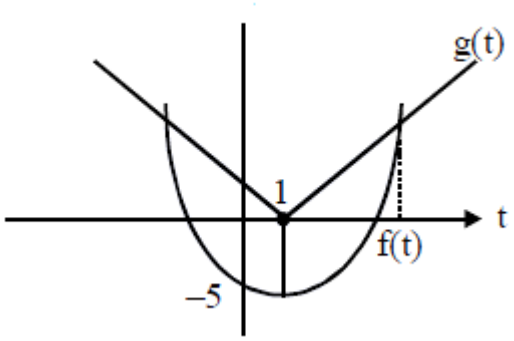
$5+|t-1|=t^2-2t$

$\Rightarrow|t-1|=(t^2-2t-5)$

$g(t)$ $f(t)$

From the graph

So, number of real root is 1.



77. $3x^2+5y^2=32$

$\left.\frac{dy}{dx}\right|_{(2,2)}=-\frac{3}{5}$

Tangent : $y-2=-\frac{3}{5}(x-2)\Rightarrow Q\left(\frac{16}{3},0\right)$

Normal : $y-2=\frac{5}{3}(x-2)\Rightarrow R\left(\frac{4}{5},0\right)$

Area is $=\frac{1}{2}(QR)\times2=QR=\frac{68}{15}$

78. Let point P on the line is $(2\lambda+1,-\lambda-1,\lambda)$ foot of perpendicular Q is given by

$\frac{x-2\lambda-1}{1}=\frac{y+\lambda+1}{1}=\frac{z-\lambda}{1}=\frac{-(2\lambda-3)}{3}$

$\because$ Q lies on $x+y+z=3$ and $x-y+z=3$

$\Rightarrow x+z=3$ and $y=0$

$y=0\Rightarrow\lambda+1=\frac{-2\lambda+3}{3}\Rightarrow\lambda=0$

$\Rightarrow$ Q is (2, 0, 1)

79. $I=\int \frac{1}{\cos^{2/3} x \sin^{1/3} x . \sin x} dx$

$=\int \frac{\tan^{2/3} x}{\tan^2 x} . \sec^2 x . dx$

$=\int \frac{\sec^2 x}{\tan^{4/3} x} . dx \qquad \left\{\tan x = t,\ \sec^2 x\, dx = dt\right\}$

$=\int \frac{dt}{\tan^{4/3}} = \frac{t^{-1/3}}{-1/3} = -3\left(t^{-1/3}\right)$

$\Rightarrow 1 = -3\tan\left(x\right)^{-1/3}$

$\Rightarrow I = \frac{3}{\left(\tan x\right)^{1/3}}\Big|_{\pi/6}^{\pi/3} = -3\left(\frac{1}{\left(\sqrt{3}\right)^{1/3}} - \left(\sqrt{3}\right)^{1/3}\right)$

$=3^{7/6} - 3^{5/6}$

80. $\angle B = \frac{\pi}{3}$, by sine Rule

$\sin A = \frac{1}{2}$

$\Rightarrow A = 30^o, a = 2,\ b = 2\sqrt{3},\ c = 4$

$\Delta = \frac{1}{2} \times 2\sqrt{3} \times 2 = 2\sqrt{3}$ sq.cm

81. $b = ar$

$c = ar^2$

$3a, 7b$ and $15c$ are in A.P.

$\Rightarrow 14b = 3a + 15c$

$\Rightarrow 14\left(ar\right) = 3a + 15ar^2$

$\Rightarrow 14r = 3 + 15r^2$

$\Rightarrow 15r^2 - 14r + 3 = 0 \qquad \Rightarrow \left(3r-1\right)\left(5r-3\right) = 0$

$r = \frac{1}{3}, \frac{3}{5}$

Only acceptable value is $r = \frac{1}{3}$, because $r \in \left(0, \frac{1}{2}\right]$

$\therefore c.d = 7b - 3a = 7ar - 3a = \frac{7}{3}a - 3a = -\frac{2}{3}a$

$\therefore$ 4^{th} term $= 15c - \frac{2}{3}a = \frac{15}{9}a - \frac{2}{3}a = a$

82. $\frac{dy}{dx} + y\left(\tan x\right) = 2x + x^2 \tan x$

I.F. $= e^{\pm\int \tan x dx} = e^{\ln.\sec x} = \sec x$

$\therefore y.\sec x = \int \left(2x + x^2 \tan x\right)\sec x . dx$

$= \int 2x \sec x\, dx + \int x^2 \left(\sec x . \tan x\right) dx$

$y \sec x = x^2 \sec x + \lambda$

$\Rightarrow y = x^2 + \lambda \cos x$

$y\left(0\right) = 0 + \lambda = 1 \qquad \Rightarrow \lambda = 1$

$$y = x^2 + \cos x$$
$$y\left(\frac{\pi}{4}\right) = \frac{\pi^2}{16} + \frac{1}{\sqrt{2}}$$
$$y\left(-\frac{\pi}{4}\right) = \frac{\pi^2}{16} + \frac{1}{\sqrt{2}}$$
$$y'(x) = 2x - \sin x$$
$$y'\left(\frac{\pi}{4}\right) = \frac{\pi}{2} - \frac{1}{\sqrt{2}}$$
$$y'\left(\frac{-\pi}{4}\right) = \frac{-\pi}{2} + \frac{1}{\sqrt{2}}$$
$$y'\left(\frac{\pi}{4}\right) - y'\left(\frac{-\pi}{4}\right) = \pi - \sqrt{2}$$

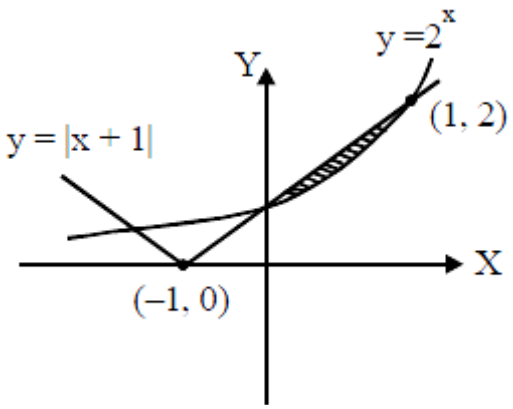
83. $4x - 2y + 4z + 6 = 0$

$$\frac{|\lambda - 6|}{\sqrt{16+4+16}} = \left|\frac{\lambda - 6}{6}\right| = \frac{1}{3}$$
$$|\lambda - 6| = 2$$
$$\lambda = 8, 4$$
$$\frac{|\mu - 3|}{\sqrt{4+4+1}} = \frac{2}{3}$$
$$|\mu - 3| = 2$$
$$\mu = 5, 1$$

$\therefore$ Maximum value of $(\mu + \lambda) = 13$.

84. Required Area

$$\int_0^1 \left((x+1) - 2^x\right) dx$$
$$= \left(\frac{x^2}{2} + x - \frac{2^x}{\ln 2}\right)_0^1$$
$$= \left(\frac{1}{2} + 1 - \frac{2}{\ln 2}\right) - \left(0 + 0 - \frac{1}{\ln 2}\right)$$
$$= \frac{3}{2} - \frac{1}{\ln 2}$$



85. $D = 0$

$$\begin{vmatrix} 1 & 1 & 1 \\ 4 & \lambda & \lambda \\ 3 & 2 & -4 \end{vmatrix} = 0 \Rightarrow \lambda = 3$$

86. $$\text{Sum} = \sum_{n=1}^{15} \frac{1^3 + 2^3 + ...n^3}{1 + 2 + ... + n} - \frac{1}{2}.\frac{15.16}{2}$$
$$= \sum_{n=1}^{15} \frac{n(n+1)}{2} - 60$$
$$= \sum_{n=1}^{15} \frac{n(n+1)(n+2-(n-1))}{6} - 60$$

$$= \frac{15.16.17}{6} - 60 = 620$$

87. $$1 - \left(\frac{1}{2}\right)^n > \frac{99}{100}$$

$$\Rightarrow \left(\frac{1}{2}\right)^n < \frac{1}{100}$$

$$\Rightarrow n = 7$$

88. $$\sim\left(\sim s \vee \left(\sim \wedge s\right)\right)$$

$$s \wedge \left(r \vee \sim s\right)$$

$$\left(s \wedge r\right) \vee \left(s \wedge \sim s\right)$$

$$\left(s \wedge r\right) \vee \left(\phi\right)$$

$$\left(s \wedge r\right)$$

89. Let $x^2 = t \qquad 2xdx = dt$

$$\Rightarrow \frac{1}{2}\int t^2.e^{-t}dt = \frac{1}{2}\left[-t^2.e^{-t} + \int 2t.e^{-t}, dt\right]$$

$$= \frac{1}{2}\left(-t^2.e^{-t}\right) + \left(-t.e^{-t} + \int 1.e^{-t}.dt\right)$$

$$= -\frac{t^2e^{-t}}{2} - te^{-t} - e^{-t} = \left(-\frac{t^2}{2} - t - 1\right)e^{-t}$$

$$= \left(-\frac{x^4}{2} - x^2 - 1\right)e^{-x^2} + C$$

for $k = 0$

$$g(-1) = -1 - 1 - \frac{1}{2} = -\frac{5}{2}$$

90. $|z|.|w| = 1 \qquad z = re^{i\left(\theta + \frac{\pi}{2}\right)}$ and $w = \frac{1}{r}e^{i\theta}$

$$\bar{z}.w = e^{-i\left(\theta + \frac{\pi}{2}\right)}.e^{i\theta} = e^{-i\left(\frac{\pi}{2}\right)} = -i$$

$$z.\bar{w} = e^{i\left(\theta + \frac{\pi}{2}\right)}.e^{-i\theta} = e^{i\left(\frac{\pi}{2}\right)} = i$$